



KING EDWARD VI  
HANDSWORTH GRAMMAR  
SCHOOL FOR BOYS



KING EDWARD VI  
ACADEMY TRUST  
BIRMINGHAM

**2023**      **Year 10**      **2024**  
**Mathematics**  
**Unit 16 Tasks**

**DO NOT WRITE INSIDE**

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# 1 Recurring Decimals

## Intelligent Practice

Write the following out fully:

- 1)  $0.\dot{5}$
- 2)  $0.4\dot{5}$
- 3)  $0.\dot{4}5$
- 4)  $0.34\dot{5}$
- 5)  $0.\dot{3}45$
- 6)  $0.2\dot{3}45$
- 7)  $0.\dot{2}345$
- 8)  $1.\dot{2}345$

Write the following using dot notation:

- 1)  $0.666 \dots$
- 2)  $0.7666 \dots$
- 3)  $0.767676 \dots$
- 4)  $0.8767676 \dots$
- 5)  $0.876876876 \dots$
- 6)  $0.9876876876 \dots$
- 7)  $0.987698769876 \dots$
- 8)  $10.987698769876 \dots$

## Fluency Practice

Question 1: Use division to convert these fractions to recurring decimals.

(a)  $\frac{1}{3}$       (b)  $\frac{2}{3}$       (c)  $\frac{4}{9}$       (d)  $\frac{7}{9}$       (e)  $\frac{1}{6}$       (f)  $\frac{5}{6}$

(g)  $\frac{3}{11}$       (h)  $\frac{8}{15}$       (i)  $\frac{5}{22}$       (j)  $\frac{1}{7}$       (k)  $\frac{1}{30}$       (l)  $\frac{6}{7}$

**Extension**

$$\frac{1}{81}$$

## Extension

### changing a fraction into a decimal

(1) work out what these fractions are as decimals by division (without using a calculator)

(a)  $\frac{2}{5}$  (b)  $\frac{3}{8}$  (c)  $\frac{7}{8}$  (d)  $\frac{4}{5}$  (e)  $\frac{3}{25}$  (f)  $\frac{7}{20}$  (g)  $\frac{3}{80}$

why do you think these fractions as decimals terminate?

(2) work out what these fractions are as decimals by division (without using a calculator)

(a)  $\frac{1}{6}$  (b)  $\frac{5}{6}$  (c)  $\frac{1}{9}$  (d)  $\frac{2}{9}$  (e)  $\frac{1}{11}$  (f)  $\frac{2}{11}$  (g)  $\frac{1}{22}$

(3) work out what these fractions are as decimals by division (without using a calculator)

(a)  $\frac{1}{7}$  (b)  $\frac{2}{7}$  (c)  $\frac{3}{7}$  (d)  $\frac{4}{7}$  (e)  $\frac{5}{7}$  (f)  $\frac{6}{7}$

$$2 \times 7 = 14 \quad 6 \times 7 = 42$$

$$3 \times 7 = 21 \quad 7 \times 7 = 49$$

$$4 \times 7 = 28 \quad 8 \times 7 = 56$$

$$5 \times 7 = 35 \quad 9 \times 7 = 63$$

what patterns can you find in the recurring decimal values of sevenths?

## Extension

### changing a fraction into a decimal

(1) work out what these fractions are as decimals by division (without using a calculator)

(a)  $\frac{1}{25}$  (b)  $\frac{1}{40}$  (c)  $\frac{1}{80}$  (d)  $\frac{1}{16}$  (e)  $\frac{1}{32}$  why do you think these fractions as decimals terminate?

(2) work out what these fractions are as decimals by division (without using a calculator)

(a)  $\frac{1}{13}$  (b)  $\frac{2}{13}$  (c)  $\frac{3}{13}$  (d)  $\frac{4}{13}$  (e)  $\frac{5}{13}$

$2 \times 13 = 26$	$6 \times 13 = 78$
$3 \times 13 = 39$	$7 \times 13 = 91$
$4 \times 13 = 52$	$8 \times 13 = 104$
$5 \times 13 = 65$	$9 \times 13 = 117$

(3) work out which fraction is bigger (with a calculator)

(a)  $\frac{5}{9}$  or  $\frac{6}{11}$

(b)  $\frac{7}{8}$  or  $\frac{17}{20}$

(c)  $\frac{2}{11}$  or  $\frac{3}{17}$

(d)  $\frac{4}{17}$  or  $\frac{15}{62}$

(4) without a calculator

$$\frac{27}{40} = 0.675$$

$$\frac{29}{40} = 0.725$$

what are:

(a)  $\frac{31}{40}$

(b)  $\frac{37}{40}$

(5) without a calculator

$$\frac{29}{32} = 0.90625$$

what are:

(a)  $\frac{29}{320}$

(b)  $\frac{290}{32}$

(c)  $\frac{13}{32}$

(d)  $\frac{21}{32}$

## Fluency Practice

By writing the denominator as a product of its prime factors, decide if each of these fractions would convert to a terminating or recurring decimal.

- (a)  $\frac{1}{8}$  (b)  $\frac{1}{25}$  (c)  $\frac{1}{15}$   
(d)  $\frac{1}{14}$  (e)  $\frac{1}{50}$  (f)  $\frac{1}{16}$   
(g)  $\frac{1}{30}$  (h)  $\frac{1}{12}$  (i)  $\frac{1}{40}$

Write out the following recurring decimals to show the first 10 decimal places.

- (a)  $0.\dot{4}$  (b)  $0.\dot{7}$   
(c)  $0.\dot{1}4$  (d)  $0.\dot{2}3$   
(e)  $0.\dot{1}2\dot{3}$  (f)  $0.\dot{4}6\dot{1}$   
(g)  $0.0\dot{5}$  (h)  $0.1\dot{7}2$

Use your calculator to convert the following fractions into terminating or recurring decimals.

- (a)  $\frac{4}{9}$  (b)  $\frac{2}{5}$  (c)  $\frac{3}{10}$   
(d)  $\frac{7}{11}$  (e)  $\frac{5}{16}$  (f)  $\frac{1}{8}$   
(g)  $\frac{4}{7}$  (h)  $\frac{29}{100}$  (i)  $\frac{3}{35}$

Use your calculator to convert the following fractions into recurring decimals.

- (a)  $\frac{1}{9}$  (b)  $\frac{2}{9}$  (c)  $\frac{3}{9}$

Can you spot a pattern?

Use your calculator to convert the following fractions into recurring decimals.

- (a)  $\frac{12}{99}$  (b)  $\frac{13}{99}$  (c)  $\frac{14}{99}$

Can you spot a pattern?



## Fluency Practice

For each of the following values of  $x$ , find

- a)  $10x$
- b)  $100x$
- c)  $1000x$
- d)  $2x$
- e)  $20x$

- 1)  $x = 0.\dot{1}$
- 2)  $x = 0.0\dot{1}$
- 3)  $x = 0.00\dot{1}$
- 4)  $x = 0.\dot{2}$
- 5)  $x = 0.\dot{3}$
- 6)  $x = 0.\dot{2}\dot{5}$
- 7)  $x = 0.\dot{7}\dot{2}$
- 8)  $x = 0.0\dot{2}\dot{5}$
- 9)  $x = 0.1\dot{2}\dot{5}$
- 10)  $x = 1.34\dot{2}\dot{4}$
- 11)  $x = 0.\dot{2}\dot{2}\dot{4}$
- 12)  $x = 0.0\dot{2}\dot{2}\dot{4}$
- 13)  $x = 0.2\dot{2}\dot{2}\dot{4}$
- 14)  $x = 1.01\dot{1}0\dot{1}$

## Fluency Practice

Question 3: Convert the following recurring decimals to fractions.  
Give each answer in its simplest form.

(a)  $0.\dot{2}$

(b)  $0.\dot{8}$

(c)  $0.\dot{1}\dot{8}$

(d)  $0.\dot{5}\dot{3}$

(e)  $0.\dot{7}\dot{5}$

(f)  $0.\dot{6}\dot{3}$

(g)  $0.\dot{1}\dot{1}\dot{2}$

(h)  $0.\dot{3}\dot{3}\dot{9}$

(i)  $0.\dot{1}\dot{7}\dot{1}$

## Fluency Practice

Question 5: Convert the following recurring decimals to fractions.  
Give each answer in its simplest form.

(a)  $0.2\dot{8}$

(b)  $0.0\dot{3}$

(c)  $0.9\dot{6}$

(d)  $0.5\dot{2}\dot{1}$

(e)  $0.3\dot{9}\dot{0}$

(f)  $0.1\dot{2}\dot{3}\dot{5}$

(g)  $0.12\dot{6}$

(h)  $0.50\dot{3}\dot{5}$

Question 7: Convert the following recurring decimals to fractions.  
Give each answer in its simplest form.

(a)  $1.\dot{2}$

(b)  $1.\dot{6}\dot{4}$

(c)  $1.9\dot{2}$

(d)  $2.0\dot{3}$

(e)  $3.6\dot{5}\dot{9}$

(f)  $8.6\dot{7}\dot{9}$

## Extension

Given that  $0.333\dots = \frac{1}{3}$

Write these as fractions:

a)  $1.333\dots$

b)  $0.4333\dots$

c)  $0.35333\dots$

d)  $3.333\dots$

## Fluency Practice

Which if the following fractions is equivalent to a recurring decimal?

(a)  $\frac{7}{10}$

(b)  $\frac{7}{9}$

(c)  $\frac{7}{100}$

(d)  $\frac{7}{11}$

(e)  $\frac{7}{20}$

(f)  $\frac{7}{30}$

Using an algebraic method, write the following recurring decimals as a fraction.

(a)  $0.\dot{4}$

(b)  $0.\dot{8}$

(c)  $0.\dot{1}\dot{3}$

(d)  $0.\dot{4}\dot{5}$

(e)  $0.\dot{5}\dot{7}$

(f)  $0.\dot{4}\dot{1}\dot{2}$

(g)  $0.\dot{1}\dot{2}\dot{7}$

(h)  $0.\dot{6}\dot{7}\dot{5}$

Using an algebraic method, write the following recurring decimals as a fraction.

(a)  $0.0\dot{4}$

(b)  $0.0\dot{6}$

(c)  $0.\dot{2}\dot{3}$

(d)  $0.\dot{1}\dot{6}$

(e)  $0.\dot{2}\dot{1}\dot{7}$

(f)  $0.00\dot{4}\dot{5}$

(g)  $0.0\dot{1}\dot{5}\dot{5}$

(h)  $0.3\dot{6}\dot{9}\dot{5}$

Use an algebraic method to show that:

(a)  $0.\dot{1}\dot{5} = \frac{5}{33}$

(b)  $0.\dot{1}\dot{4}\dot{4} = \frac{16}{111}$

(c)  $0.\dot{7}\dot{1} = \frac{32}{45}$

Using an algebraic method, find  $0.\dot{9}$  as a fraction.

## Fluency Practice

<p><b>A1</b> State the conditions under which a fraction can be written as a <b>terminating</b> decimal.</p>	<p><b>A2</b> State the conditions under which a fraction can be written as a <b>recurring</b> decimal.</p>	<p><b>A3</b> Which of the following can be written as <b>terminating</b> decimals:</p> $\frac{2}{3} \quad \frac{3}{4} \quad \frac{4}{9} \quad \frac{5}{6} \quad \frac{5}{8} \quad \frac{3}{7} \quad \frac{3}{5}$	<p><b>A4</b> Which of the following can be written as <b>recurring</b> decimals:</p> $\frac{5}{12} \quad \frac{7}{25} \quad \frac{3}{14} \quad \frac{5}{16} \quad \frac{5}{32} \quad \frac{5}{11}$
<p><b>B1</b> Show that <math>0.\dot{5} = \frac{5}{9}</math></p>	<p><b>B2</b> Show that <math>0.7\dot{3} = \frac{11}{15}</math></p>	<p><b>B3</b> Show that <math>0.61\dot{6} = \frac{37}{60}</math></p>	<p><b>B4</b> Show that <math>3.5\dot{2} = 3\frac{47}{90}</math></p>
<p><b>C1</b> Show that <math>0.2\dot{7} = \frac{3}{11}</math></p>	<p><b>C2</b> Show that <math>0.2\dot{5}\dot{7} = \frac{17}{66}</math></p>	<p><b>C3</b> Show that <math>0.44\dot{7} = \frac{149}{333}</math></p>	<p><b>C4</b> Show that <math>2.5\dot{1} = 2\frac{17}{33}</math></p>
<p><b>D1</b> Work out <math>0.2\dot{7} \times 3</math>, writing your answer as a fraction in its simplest terms.</p>	<p><b>D2</b> Work out <math>0.5\dot{7} - 0.2\dot{6}</math>, writing your answer as a fraction in its simplest terms.</p>	<p><b>D3</b> <math>x</math> is a whole number such that <math>1 \leq x \leq 9</math></p> <p>Write the recurring decimal <math>0.1\dot{x}</math> as a fraction in its simplest terms.</p>	<p><b>D4</b> <math>y</math> is a whole number such that <math>1 \leq y \leq 9</math></p> <p>Show that <math>0.\dot{3}y = \frac{y}{33}</math></p>

## Problem Solving

These decimals have one digit recurring:

$$0.\dot{2} = 0.22222222 \dots$$

$$0.07\dot{2} = 0.07222222 \dots$$

- 1) Write three different decimals with one digit recurring.
- 2) Convert you decimals in part one into fractions in their simplest form. Use the algebraic method.
- 3) Find five fractions with different denominators when in simplest form that have one digit recurring.
- 4) Find the prime factors of the denominators. What do you notice?
- 5) Find five fractions with different denominators when in simplest form that have two digits recurring.
- 6) Find the prime factors of the denominators. What do you notice?
- 7) Repeat 5 and 6 for 3 digits recurring.
- 8) Investigate for other decimals with different number of digits recurring.

## More-Same-Less – Recurring Decimals

Instructions: Convert the decimal in the middle box to a fraction, giving your answer in its simplest form. Then fill in the remaining boxes, making the minimum change possible from the middle box.

**Number of digits which recur when expressed as a decimal**

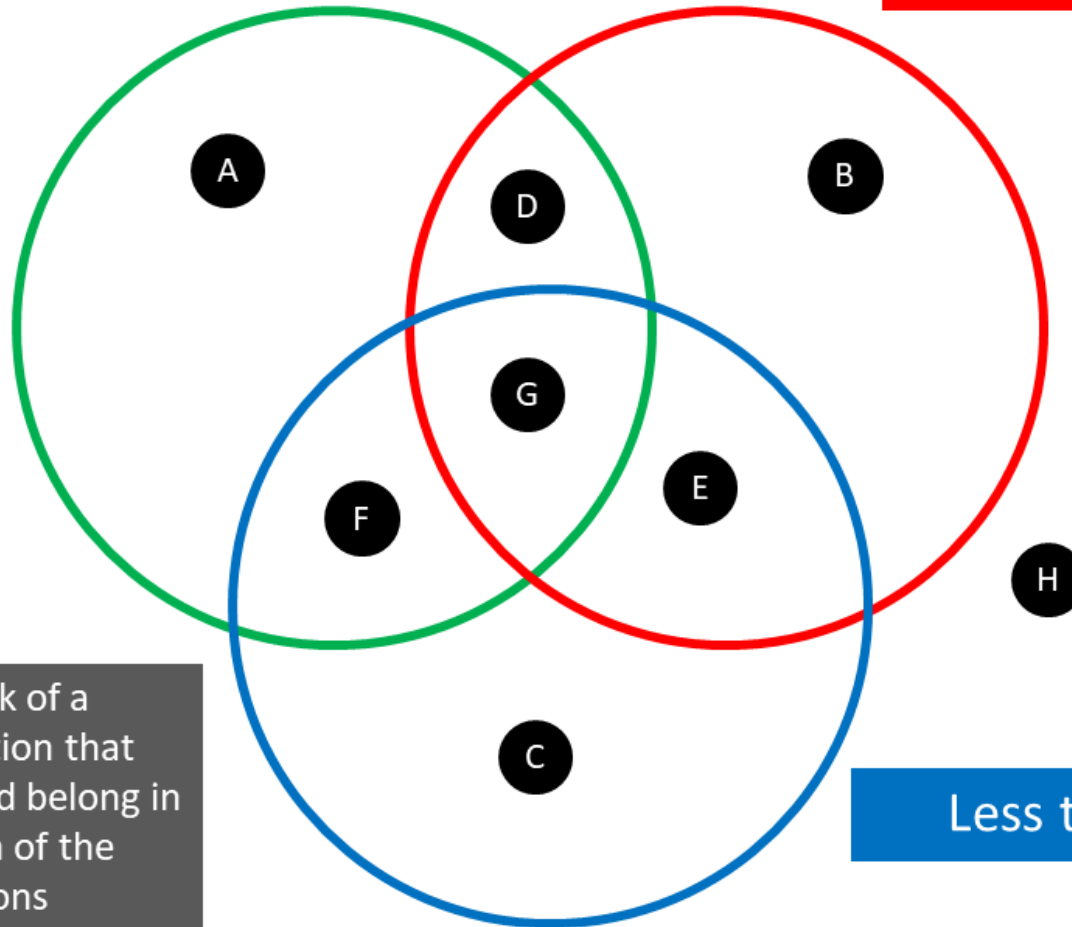
<b>Difference between numerator and denominator when expressed as a fraction in its simplest form</b>		Less	Same	More
	More			
	Same		<b>0.36̇</b>	
	Less			



# Maths Venns

Can be expressed as a  
recurring decimal

Denominator is a  
prime number



If you think a  
region is  
impossible to  
fill, convince  
me why!

Think of a  
fraction that  
could belong in  
each of the  
regions

Less than  $\frac{1}{2}$

## Fluency Practice

Prove each of the following sums using recurring decimals.

Prove that  $0.\dot{1} \times 0.\dot{2}\dot{7} = \frac{1}{33}$

Prove that  $0.\dot{5} \times 0.\dot{8}\dot{1} = \frac{5}{11}$

Prove that  $0.\dot{1}\dot{8} \div 0.\dot{4} = \frac{9}{22}$

Prove that  $0.\dot{8} \div 0.\dot{7}\dot{2} = 1\frac{2}{9}$

Prove that  $0.\dot{1}\dot{2}\dot{6} \div 0.\dot{2} = \frac{5}{8}$

Prove that  $0.\dot{19}\dot{4} \div 0.\dot{4} = \frac{7}{16}$

## Fluency Practice

(a) Using algebra, show that

$$0.\dot{2} + 0.\dot{2}\dot{3} = \frac{5}{11}$$

(b) Using algebra, show that

$$1.\dot{3}\dot{8}\dot{1} - 0.\dot{8}\dot{1} = \frac{31}{55}$$

(a) Using algebra, show that

$$0.5 \times 0.\dot{5}\dot{4} = \frac{10}{33}$$

(b) Using algebra, show that

$$4 \times 0.\dot{8}\dot{5} \times 0.\dot{1}\dot{5} = \frac{14}{27}$$

(a) Using algebra, show that

$$0.\dot{7} \div 0.\dot{2}\dot{1} = 3\frac{13}{19}$$

(b) Using algebra, show that

$$0.\dot{3}\dot{5} \div 1.\dot{2}\dot{7} = \frac{32}{115}$$

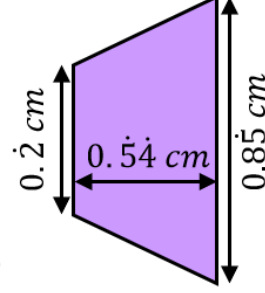
(a) Show that the mean of the three numbers

$$0.8, 0.\dot{8}\dot{1} \text{ and } 0.\dot{8}\dot{1}$$

can be written in its simplest form as a fraction  $\frac{a}{b}$ , where  $a$  and  $b$  are integers to be found.

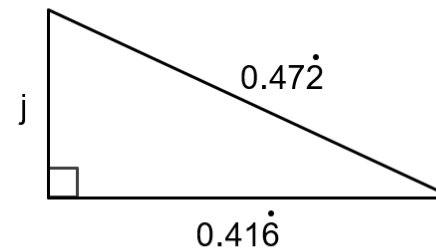
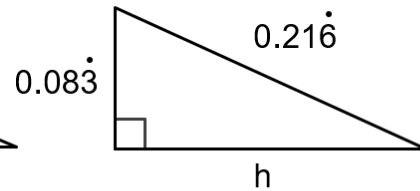
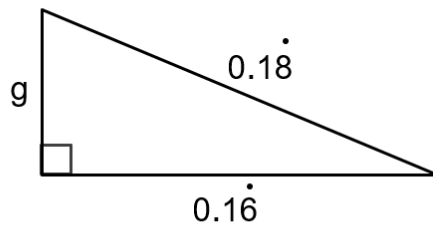
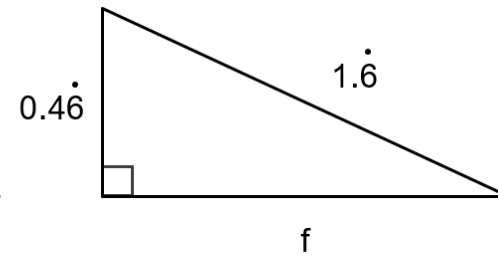
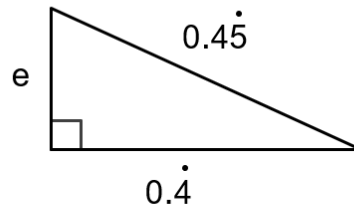
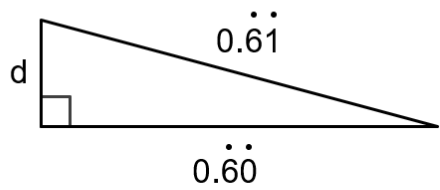
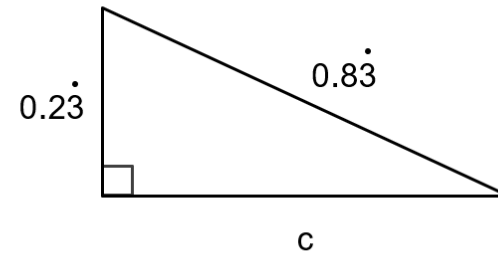
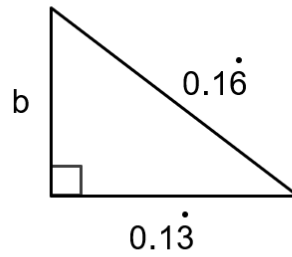
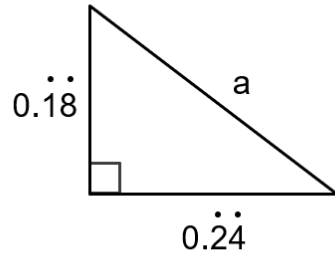
(b) Using algebra, prove that the area of the trapezium shown is

$$\frac{97}{330} \text{ cm}^2$$



## Extension

find the length of the missing side as a fraction in its simplest form



## 2 Parallel and Perpendicular Lines

# Fluency Practice

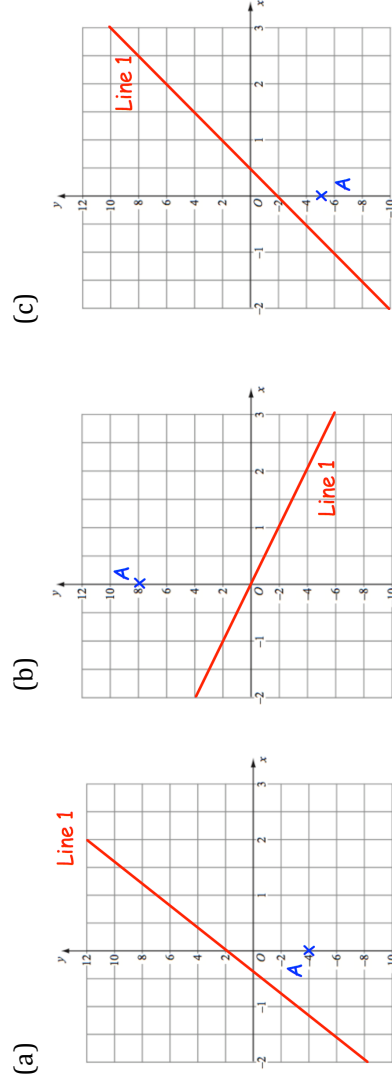
Question 1: Write down the equation of a line parallel to each of the following

- (a)  $y = 2x + 3$       (b)  $y = 5x - 3$       (c)  $y = -3x + 1$       (d)  $y = x - 7$   
 (e)  $y = -7x - 10$       (f)  $y = -x$       (g)  $y = 10x$       (h)  $y = 4$   
 (i)  $x + y = 5$       (j)  $2x + y - 1 = 0$       (k)  $x - 2y + 5 = 0$       (l)  $3x - 4y - 9 = 0$

Question 2: Write down the equation of each of the following lines

- (a) Parallel to  $y = 3x + 5$  and passing through  $(0, 2)$   
 (b) Parallel to  $y = 4x - 1$  and passing through  $(0, 6)$   
 (c) Parallel to  $y = 5x$  and passing through  $(0, -3)$   
 (d) Parallel to  $y = -2x + 10$  and passing through the origin  
 (e) Parallel to  $x + y = 8$  and passing through  $(0, -4)$   
 (f) Parallel to  $x - 2y + 3 = 0$  and passing through  $(0, 5)$

Question 3: Write down the equation of the line parallel to Line 1 and passing through A.



## Intelligent Practice

Write down the equation:

Parallel to the line	Goes through the point	Answer
$y = 3x + 2$	$(0,7)$	
$y = 3x + 2$	$(3,0)$	
$y = 3x + 2$	$(3,7)$	
$y = 3x + 10$	$(3,7)$	
$y = 2x - 2$	$(3,7)$	
$y = 2x - 2$	$(-3,7)$	
$y = 2x - 2$	$(0,0)$	

## Fluency Practice

Question 4: Write down the equation of each of the following lines

- (a) Parallel to  $y = 2x - 1$  and passing through  $(1, 8)$
- (b) Parallel to  $y = 3x + 2$  and passing through  $(1, 1)$
- (c) Parallel to  $y = 5x - 4$  and passing through  $(2, 9)$
- (d) Parallel to  $y = 3x - 7$  and passing through  $(4, 15)$
- (e) Parallel to  $y = 4x$  and passing through  $(-1, 3)$
- (f) Parallel to  $y = -2x + 5$  and passing through  $(-3, 0)$
- (g) Parallel to  $y = 6x + 3$  and passing through  $(10, 5)$
- (h) Parallel to  $y = -\frac{1}{2}x + 1$  and passing through  $(3, 0)$
- (i) Parallel to  $x + y = 10$  and passing through  $(4, 0)$
- (j) Parallel to  $x - 3y - 6 = 0$  and passing through  $(-9, -2)$



## Exam Questions



Line A passes through the points (2, 1) and (5, 10)

Find the equation of the line parallel to A that passes through (2,5)

[3]



Line A passes through the points (2, 1) and (5, 10)

Line B passes through the points (4, 7) and (2, 1)

Show that Line A and Line B are parallel

[4]



Line A passes through the points (3, 6) and (5, -2)

Line B passes through the points (2, 5) and (8, k)

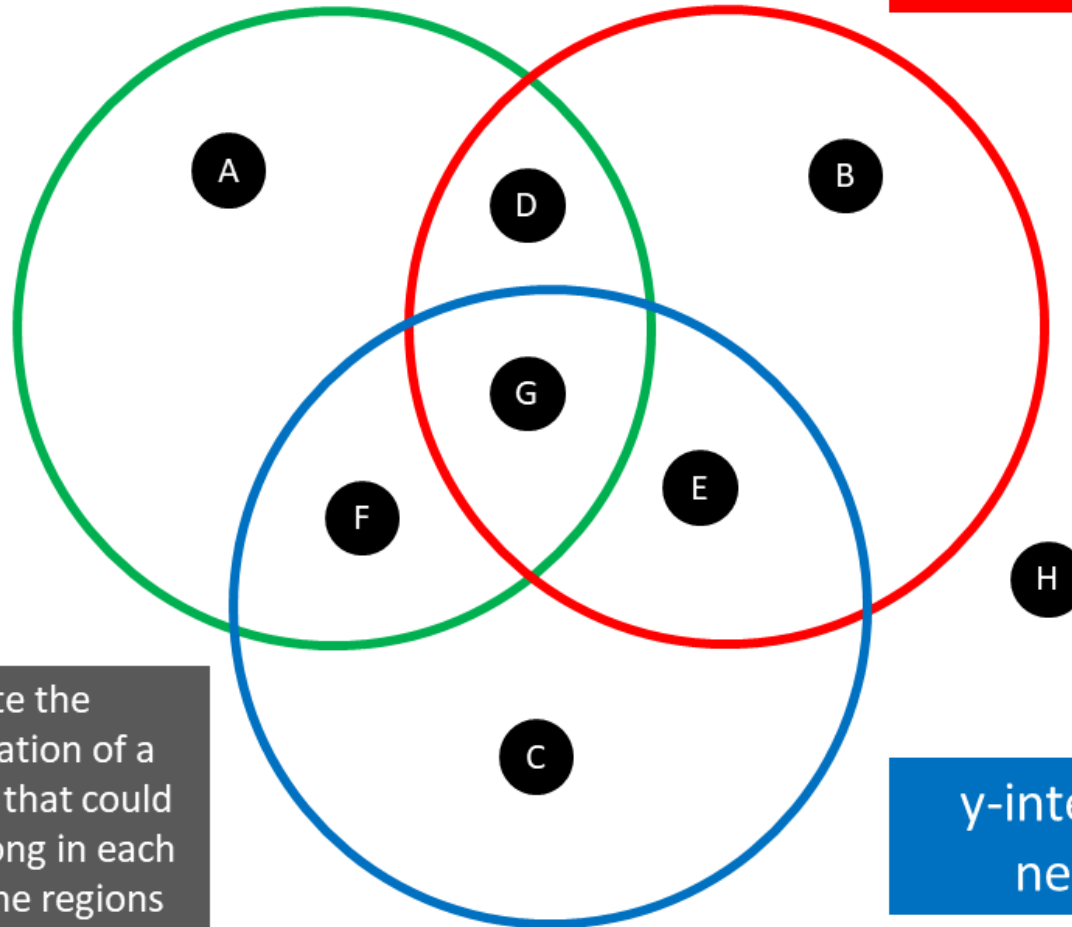
Line A and Line B are parallel. Find the value of k.

[4]

# Maths Venns

Parallel to  $y = 4x$

Passes through  
(2, 5)



If you think a region is impossible to fill, convince me why!

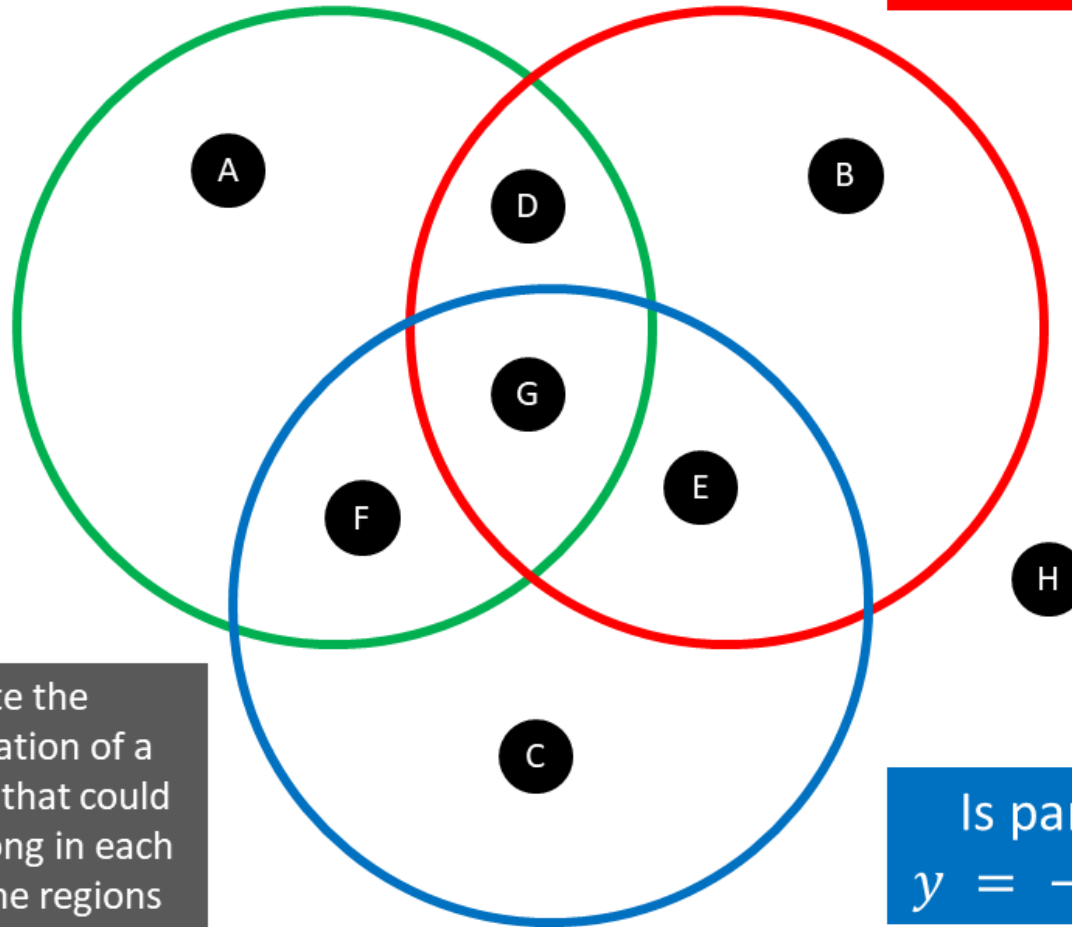
Write the equation of a line that could belong in each of the regions

y-intercept is negative

# Maths Venns

Crosses y-axis at  
 $(0, 4)$

Crosses x-axis at  
 $(2, 0)$



If you think a region is impossible to fill, convince me why!

Write the equation of a line that could belong in each of the regions

Is parallel to  
 $y = -2x + 1$

## Fluency Practice

Question 5: Write down the negative reciprocal of each number below.

(a) 4

(b)  $\frac{2}{3}$

(c)  $-6$

(d) 8

(e)  $\frac{1}{2}$

(f) 1

(g)  $-\frac{1}{3}$

(h)  $-\frac{2}{5}$

(i)  $\frac{4}{7}$

(j)  $1\frac{1}{2}$

(k)  $-1$

(l)  $-1\frac{3}{4}$

# Fluency Practice

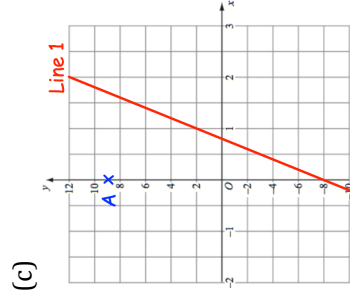
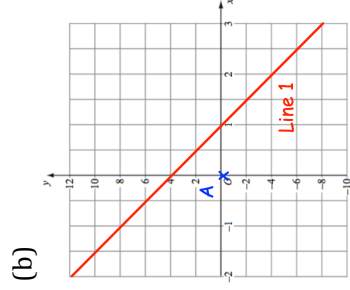
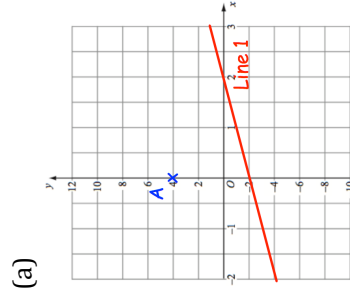
Question 6: Write down the equation of a line perpendicular to each of the following

- (a)  $y = 4x + 2$       (b)  $y = 2x - 7$       (c)  $y = -5x + 2$       (d)  $y = x - 3$   
 (e)  $y = -x + 1$       (f)  $y = \frac{1}{2}x + 3$       (g)  $y = \frac{3}{4}x - 2$       (h)  $y = -\frac{1}{5}x + 1$   
 (i)  $y = -\frac{2}{3}x - 5$       (j)  $x + y = 12$       (k)  $x - 2y + 8 = 0$       (l)  $5x - 3y - 3 = 0$

Question 7: Write down the equation of each of the following lines

- (a) Perpendicular to  $y = 2x + 4$  and passing through  $(0, 3)$   
 (b) Perpendicular to  $y = -3x - 8$  and passing through  $(0, -2)$   
 (c) Perpendicular to  $x + y = 6$  and passing through  $(0, 1)$   
 (d) Perpendicular to  $y = \frac{1}{3}x - 2$  and passing through the origin  
 (e) Perpendicular to  $y = -\frac{1}{5}x + 8$  and passing through  $(0, -2)$   
 (f) Perpendicular to  $y = -\frac{2}{9}x - 10$  and passing through  $(0, 6)$

Question 8: Write down the equation of the line perpendicular to Line 1 & passing through A.



## Intelligent Practice

Write down the equation:

Perpendicular to the line	Goes through the point	Answer
$y = -x + 2$	$(0,7)$	
$y = 2x + 2$	$(0,7)$	
$y = 2x + 2$	$(12,7)$	
$y = 3x + 2$	$(12,7)$	
$y = 3x + 2$	$(10,7)$	
$y = 3x + 2$	$(-12,7)$	
$y = 2x + 2$	$(0,0)$	

## Fluency Practice

Question 9: Write down the equation of each of the following lines

- (a) Perpendicular to  $y = 2x - 1$  and passing through  $(4, 0)$
- (b) Perpendicular to  $y = -3x + 4$  and passing through  $(6, 1)$
- (c) Perpendicular to  $y = 4x$  and passing through  $(-12, 5)$
- (d) Perpendicular to  $y = -\frac{1}{2}x + 1$  and passing through  $(3, -7)$
- (e) Perpendicular to  $y = \frac{2}{3}x + 4$  and passing through  $(-6, -4)$
- (f) Perpendicular to  $y = -\frac{3}{5}x - 2$  and passing through  $(9, 9)$
- (g) Perpendicular to  $x + 4y - 6 = 0$  and passing through  $(1, 8)$

## Extension

Equation of line $l_1$	Two points that $l_1$ passes through.		Equation of a line perpendicular to $l_1$ , through point A, in the form $ax + by + c = 0$
	Point A	Point B	
$2x + 3y - 5 = 0$	$(-5, a)$  $a$	$(b, -5)$  $b =$	
	$(-4, 1)$	$(-3, -2)$	
	$(a, 1)$  $a =$	$(b, 3)$  $b =$	$x + 3y - 3 = 0$
$-x + 6y + 17 = 0$		$(b, -2)$  $b =$	$6x + y - 65 = 0$



## Exam Questions



Write down the equation of a line perpendicular to  $y = 3x + 3$  [1]



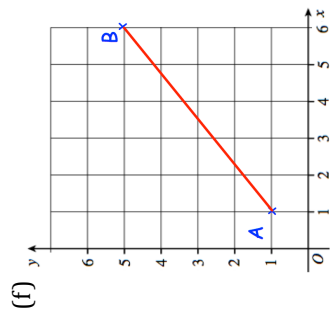
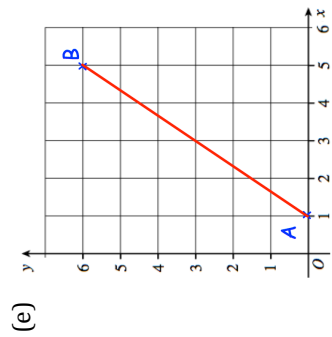
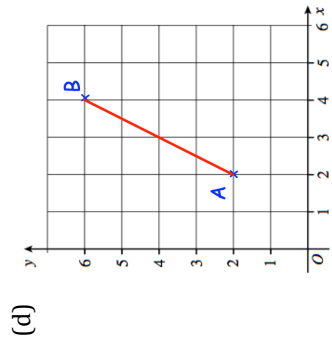
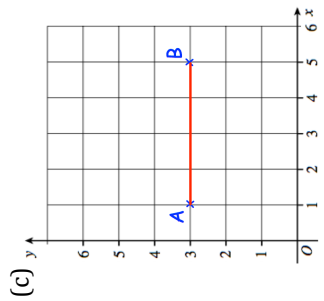
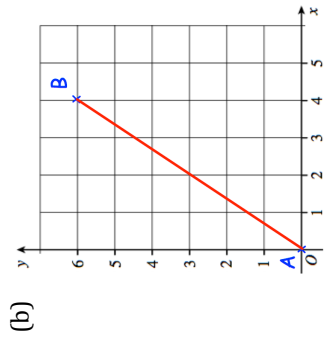
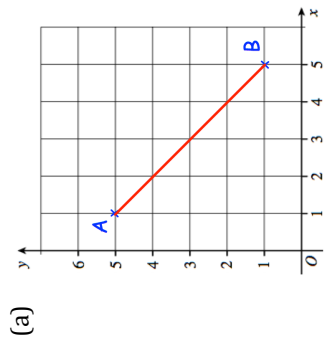
Write down the equation of the line perpendicular to  $y = \frac{1}{2}x + 4$  which passes through (0,7) [2]



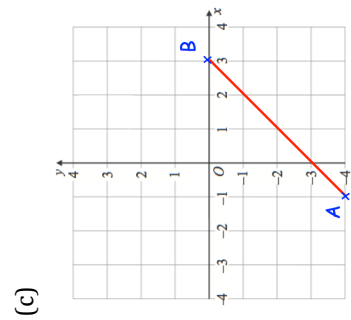
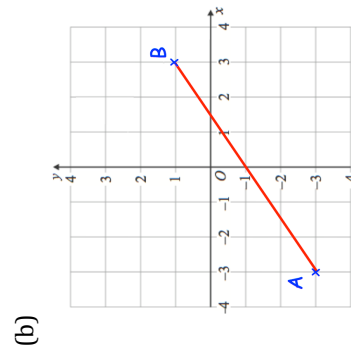
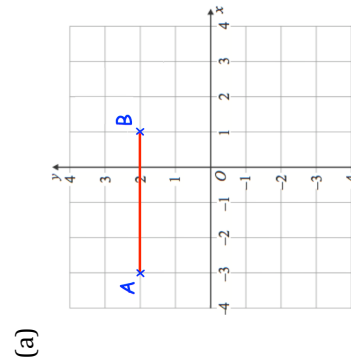
Line A passes through the points (-3, -1) and (-1, 9).  
Line B passes through the points (-2, 1) and (k, 4).  
Line A and Line B are perpendicular.  
Find the value of k. [4]

# Fluency Practice

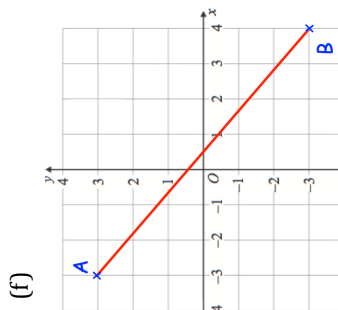
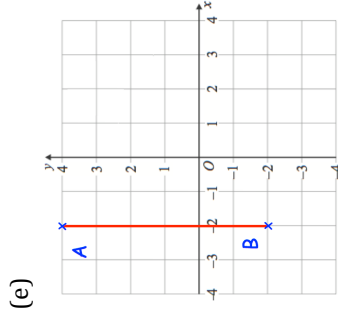
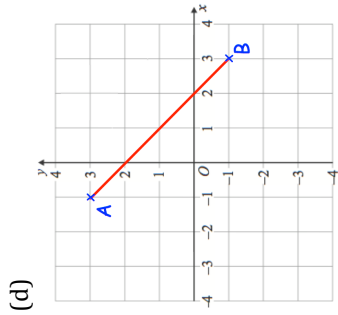
Question 1: Find the coordinates of the midpoints of the following line segments.



Question 2: Find the coordinates of the midpoints of the following line segments.



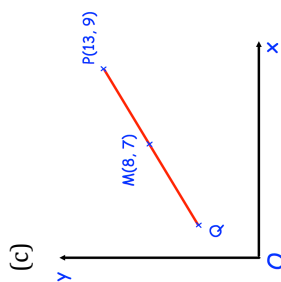
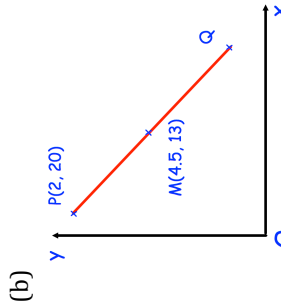
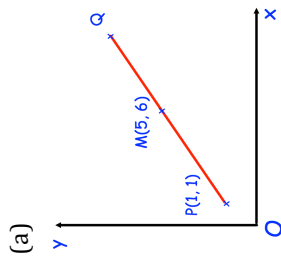
# Fluency Practice



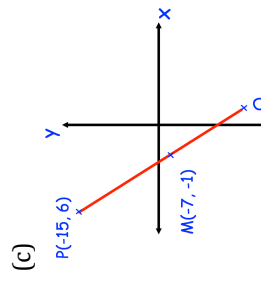
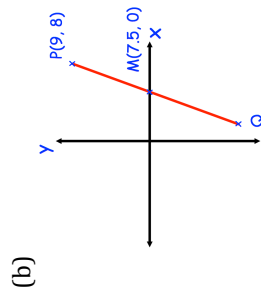
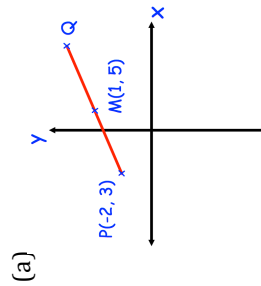
Question 3: Find the midpoint of the line joining these pairs of points

- (a) (2, 4) and (6, 10)
- (b) (1, 4) and (9, 12)
- (c) (0, 7) and (6, 1)
- (d) (-5, 2) and (5, -4)
- (e) (-3, 9) and (7, -1)
- (f) (0, -4) and (9, 0)
- (g) (-10, -6) and (-2, 8)
- (h) (0, 5) and (-11, -10)
- (i) (9, 8) and (4, 8)

Question 4: M is the midpoint of PQ in each diagram below.  
Find the coordinates of Q in each diagram.

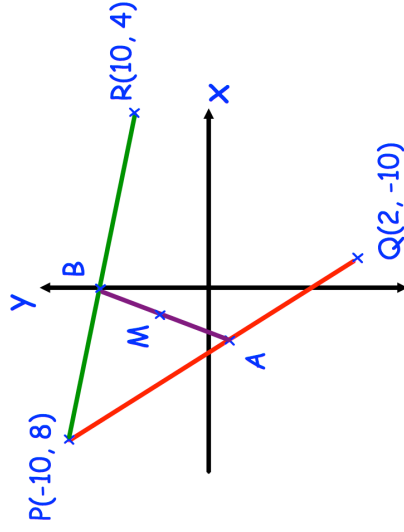


Question 5: M is the midpoint of PQ in each diagram below.  
Find the coordinates of Q in each diagram.



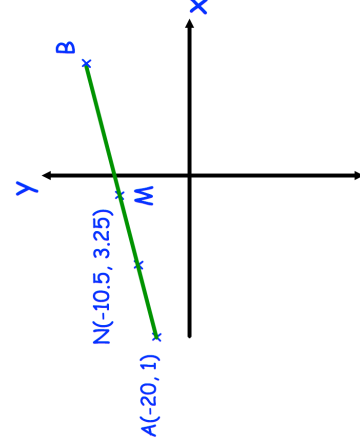
## Extension

- Question 1: A is the midpoint of the line PQ.  
B is the midpoint of the line PR.  
M is the midpoint of the line AB.  
Find the coordinates of the point M



- Question 2: M is the midpoint of the line AB.  
The coordinates of the point M are (7, 2)  
The coordinates of the point B are (11, 8)  
The coordinates of the point C are (7, -4)  
Find the area of triangle ACM.

- Question 3: M is the midpoint of AB.  
N is the midpoint of AM.  
Find the coordinates of the point B.



# Fluency Practice

## Apply

Question 1: Write down the equations of the lines, from the box, that are:

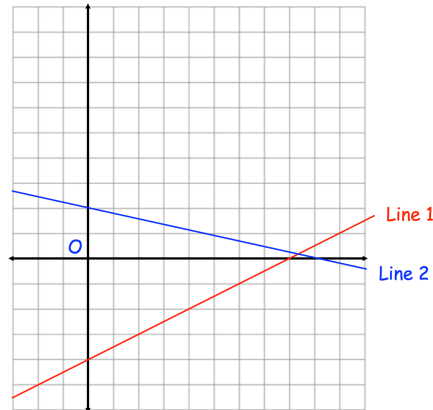
$y = 2x$	$y = \frac{1}{2}x + 1$
$y = 3x + 2$	$y = -5x$
$y = 5x - 4$	$y = -2x + 3$
	$y = 3x - 2$

- (a) parallel      (b) perpendicular      (c) cross the y-axis at (0, 3)  
 (d) pass through the origin      (e) pass through the point (1, 1)

Question 10: Two straight lines are shown.

Line 1 has equation  $y = \frac{3}{2}x - 24$

- (a) Find the equation of Line 2  
 (b) Are the lines perpendicular?

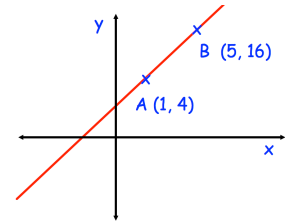


Question 2: Are the lines  $2x + y = 8$  and  $y = 2x + 5$  parallel?

Question 3: Are the lines  $4x - y - 5 = 0$  and  $x + 4y + 1 = 0$  perpendicular?

Question 4: A straight line passes through the points A(1, 4) and B(5, 16).

- (a) Find the equation of the line parallel to AB that passes through (1, 7)  
 (b) Find the equation of the line perpendicular to AB that passes through the midpoint of AB.



Question 5: The line L has equation  $y = 2x + 8$   
 The line L crosses the x-axis at the point A.  
 The line M is perpendicular to Line L and passes through the point A

- (a) Find the coordinates of the point A.  
 (b) Find equation of the Line M.

Question 6: The point A has coordinates (-12, -7) and the point B has coordinates (-8, 1)  
 Find the equation of the line parallel to AB and passing through (2, 5)

Question 7: The line L passes through the points (-2, 1) and (2, 3).  
 The line N passes through the points (4, 7) and (12, 11).

Bryan says that the lines L and N are parallel.  
 Is Bryan correct? Explain your answer.

Question 8: The point C has coordinates (2, -3) and the point D has coordinates (4, 6).  
 Find the equation of the line perpendicular to CD and passing through D.

Question 9: The line Q passes through the points (-10, -2) and (-8, -8)  
 The line R passes through the points (1, 2) and (10, a)

The lines Q and R are perpendicular.

Find a.

## Fluency Practice

In each question you will need to use the formula  $y = mx + c$ .

Find the equation of the line perpendicular to the line  $y = 2x + 3$  and passes through the point  $(4, 11)$

Where does the line cross the  $x$  and  $y$  axis?

Find the equation of the line perpendicular to the line  $y = 3x - 5$  and passes through the point  $(3, 4)$

Where does the line cross the  $x$  and  $y$  axis?

Find the equation of the line perpendicular to the line  $y = -2x + 8$  and passes through the point  $(6, -4)$

Find the equation of the line perpendicular to the line  $y = -3x + 5$  and passes through the point  $(6, -13)$

Find the equation of the line perpendicular to the line  $y = \frac{1}{2}x + 4$  and passes through the point  $(6, 7)$

Find the equation of the line perpendicular to the line  $y = 5x - 9$  and passes through the point  $(10, 41)$

## Extension

perpendiculars

based on CBSE(10) exam questions

- (1) prove that the triangle with vertices:  
 $A(3, 0)$ ,  $B(6, 4)$  and  $C(-1, 3)$   
is right-angled  
show that it is also isosceles
- (2) triangle  $ABC$  is isosceles with  $AC = BC$   
if  $A = (3, -2)$  and  $B = (5, 2)$   
and the coordinates of  $C$  are  $(12, k)$   
a) find the value of  $k$   
b) find the area of triangle  $ABC$
- (3) triangle  $ABC$  has vertices:  
 $A = (3, 3)$ ,  $B = (3, -7)$  and  $C = (6, -6)$   
a) show that the triangle is right-angled  
b) show that the centre of the circle that passes  
through  $A$ ,  $B$  and  $C$  lies on  $AB$   
c) find the area of triangle  $ABC$
- (4) a) which point on the  $y$ -axis is equidistant from  
 $(5, -3)$  and  $(-4, 6)$  ?  
b) which point on the  $x$ -axis is equidistant from  
 $(2, -5)$  and  $(-2, 9)$  ?
- (5) the point  $P(x, y)$  is equidistant from  
 $A(5, 1)$  and  $C(-1, 5)$   
a) prove that  $2y = 3x$   
b) find the other two coordinates of the square  
 $ABCD$
- (6) the point  $P(x, y)$  is equidistant from  
 $E(4, 3)$  and  $G(-3, 4)$   
a) prove that  $y = 7x$   
b) find the other two coordinates of the  
square  $EFGH$   
c) which square,  $ABCD$  (above) or  $EFGH$   
has the larger area?
- (7) the point  $P(x, y)$  is equidistant from  
 $A(a + b, b - a)$  and  
 $B(a - b, a + b)$   
prove that  $ay = bx$
- (8) the triangle with vertices:  
 $A(4, 7)$ ,  $B(t, 6)$  and  $C(8, 1)$   
is right-angled at  $B$   
find the values of  $t$

# Extension

## lines and perpendiculars

based on GCSE exam questions

- (1) the straight line  $L_1$  passes through the points with coordinates  $(4, 8)$  and  $(12, 4)$   
the straight line  $L_2$  passes through the origin  $(O)$  and has gradient  $-3$

the two lines meet at point  $P$   
find the coordinates of  $P$

the perpendicular to  $L_1$  from the origin meets  $L_1$  at  $Q$

establish that  $\triangle OPQ$  is an isosceles right angled triangle

what is its area?

- (2) the point  $P = (3, 4)$  and  $Q = (a, b)$

a line perpendicular to  $PQ$  is:  $3x + 2y = 7$

find an expression for  $b$  in terms of  $a$   
and give four possible coordinates for  $Q$   
[other than  $(3, 4)$ ]

- (3)  $PQR$  is a triangle with vertices  $P, Q$  and  $R$   
 $P = (-3, -6), Q = (1, 4)$  and  $R = (5, -2)$   
 $M$  is the midpoint of  $PQ$   
 $N$  is the midpoint of  $QR$

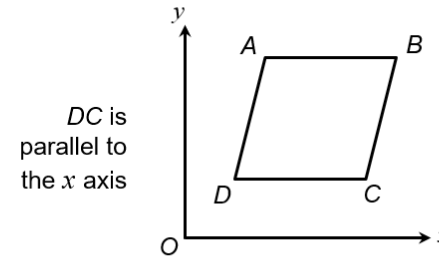
prove that  $MN$  is parallel to  $PR$   
establish that the length  $MN = \frac{1}{2} PR$

- (4)  $ABCD$  is a rhombus with  $A = (5, 11)$   
the equation of the diagonal  $DB$  is  $y = \frac{1}{2}x + 6$

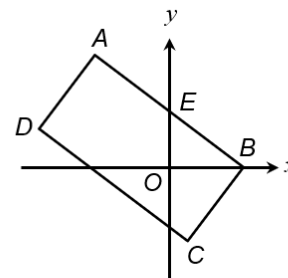
find an equation of the diagonal  $AC$

what are the coordinates of the centre of the rhombus?

what are the coordinates of (i)  $B$  (ii)  $D$  (iii)  $C$ ?



- (5)



$ABCD$  is a rectangle  
the equation of the line  
 $AB$  is  $x + 2y = 12$

$AE = EB$

find an equation for  $AD$

find an equation for  $DC$

what are the coordinates  
of (i)  $A$  (ii)  $D$  (iii)  $C$ ?



# Problem Solving

	<b>All Sides Equal</b>	<b>Has 4 Right Angles</b>	<b>Diagonals Cross at Right Angles</b>
<b>Forms a Parallelogram</b>			
<b>Diagonals not Equal in Length</b>			

Put these cards into the correct part of the table.

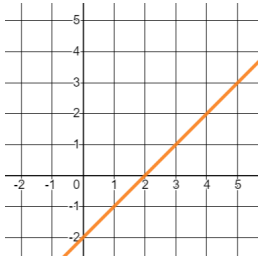
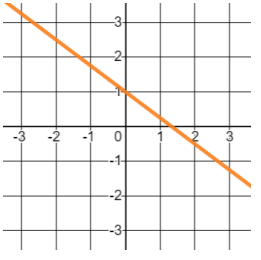
$y = 2x - 1$ $y = 2x - 11$ $2y = 3 - x$ $4y = -(2x - 16)$
--

$y = x + 3$ $y = x - 5$ $7y = -35 - 49x$ $7x = 35 - y$
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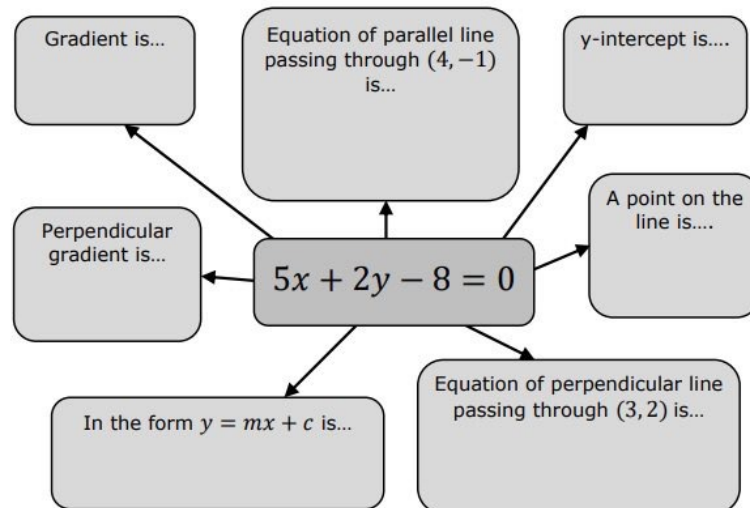
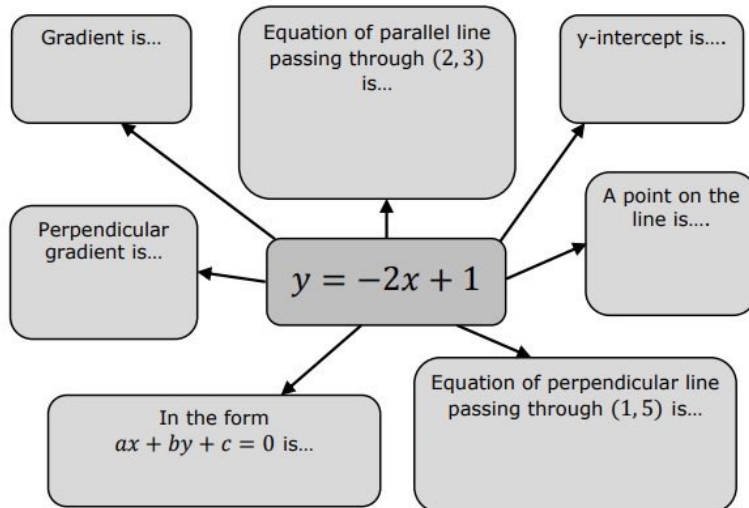
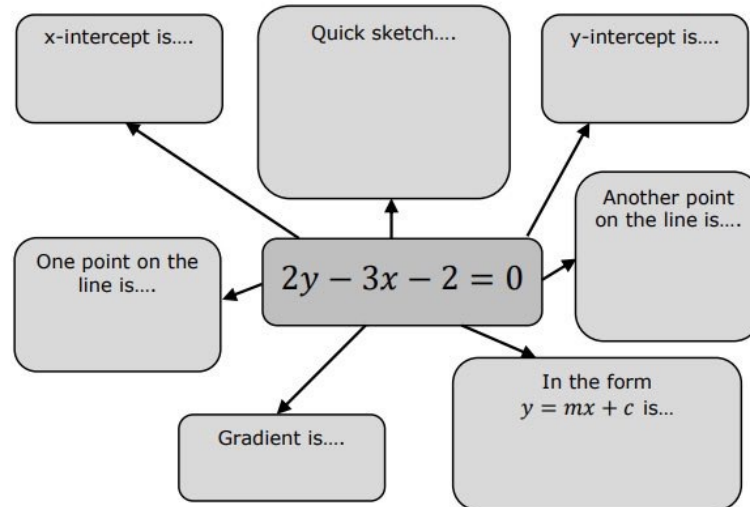
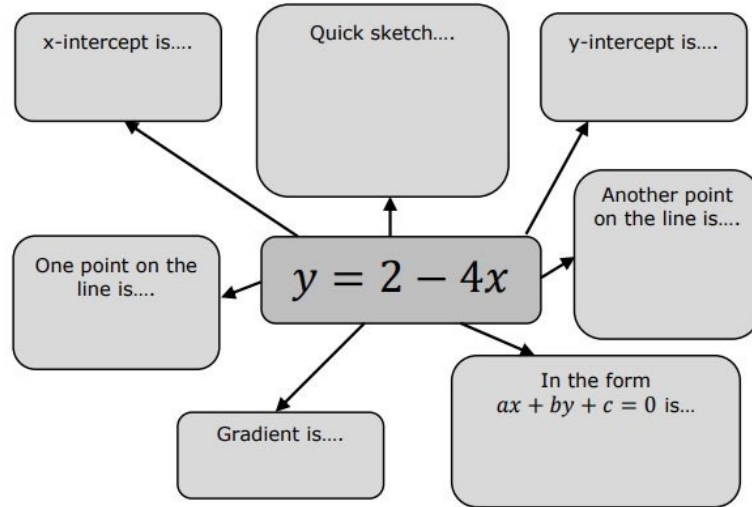
<p><b>IT'S IMPOSSIBLE!</b></p>
------------------------------------

There are 3 missing spaces. Create sets of equations for them.

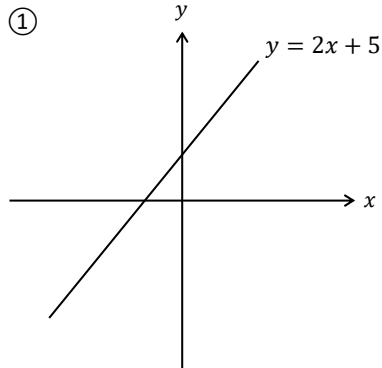
## Fluency Practice

<b>(a)</b>	<b>(b)</b>	<b>(c)</b>	<b>(d)</b>
Write down the gradient and y-intercept of the straight line with equation $y = 5x - 2$	Write down the gradient and y-intercept of the straight line with equation $y = -\frac{1}{2}x + 7$	Write down the gradient and y-intercept of the straight line with equation $3y = 2x - 9$	Find the gradient of the line joining $(2, 5)$ and $(4, 11)$
<b>(e)</b>	<b>(f)</b>	<b>(g)</b>	<b>(h)</b>
Find the equation of the line. 	Find the equation of the line. 	Write down the equation of the line that is parallel to $y = -4x - 9$ and passes through $(0, 2)$	Write down the equation of the line that is perpendicular to $y = -3x$ and passes through the point $(0, -5)$
<b>(i)</b>	<b>(j)</b>	<b>(k)</b>	
Find the equation of the line that has a gradient of 2 and passes through $(4, 3)$	Find the equation of the line that is perpendicular to the line $2y = x - 8$ and passes through $(-1, 9)$	Find the equation of the line that passes through $(2, 9)$ and $(5, 3)$ .	

# Fluency Practice



# Fluency Practice



On the axes, sketch the graphs:

$y = 3x$        $y = 2x - 6$

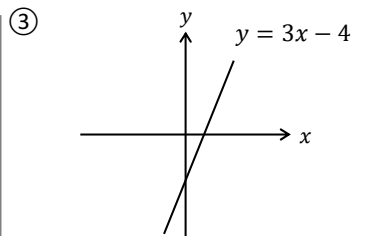
$y = \frac{x}{2} + 5$

②

$y = 3x + 5$   
 Gradient = \_\_\_\_\_  
 y-intercept = \_\_\_\_\_

$y = 8 - 2x$   
 Gradient = \_\_\_\_\_  
 y-intercept = \_\_\_\_\_

$2y + x = 7$   
 Gradient = \_\_\_\_\_  
 y-intercept = \_\_\_\_\_

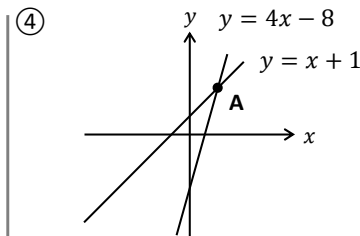


Which coordinates are on this graph?

- (4, 8)      (0, 4)      (-2, -2)

Complete these coordinates for the graph  $2y = 5x + 2$

- (4, y)      (x, 6)      (x, -9)



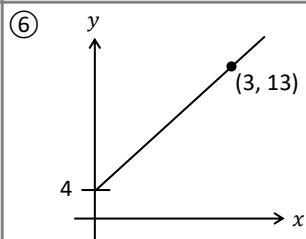
Find the coordinates of point A.

Find the coordinates of the point where the graphs  $y = 3x + 9$  &  $y = \frac{x}{2} + 4$  intersect.

⑤

Line N is parallel to the graph  $y = 5x - 7$  & passes through (4, 22).  
 Find the equation of Line N

Line O is parallel to the graph  $y = 5 - 2x$  & passes through (5, -13).  
 Find the equation of Line O



Find the equation of this line.

Line P passes through (1, 3) & (3, 11).  
 Find the equation of this line.

Line Q passes through (-2, 10) & (5, -4).  
 Find the equation of this line.

⑦

$y = 2x + 5$   
 Find the gradient of a line perpendicular to this graph.

$y = 10 - 4x$   
 Find the gradient of a line perpendicular to this graph.

$3y + 2x = 7$   
 Find the gradient of a line perpendicular to this graph.

⑧

Line R is perpendicular to the graph  $y = 2x + 4$  & passes through (8, 2).  
 Find the equation of Line R

Line S passes through (4, 6) & (8, 8)  
 Line T is perpendicular to this line & passes through its midpoint.  
 Find the equation of Line T.

## Fluency Practice

Harder Coordinate Geometry		
(a)	(b)	(c)
<p>Find an equation of the line that passes through the points <math>(4, 2)</math> and <math>(-8, 11)</math>. Give your answer in the form <math>ax + by = c</math> where <math>a</math>, <math>b</math> and <math>c</math> are integers.</p> <p style="text-align: center; color: red;"><math>3x + 4y = 20</math></p>	<p>The straight line <math>L</math> has equation <math>5x - 3y = 18</math>. Find an equation of the line that is parallel to <math>L</math> and crosses the <math>x</math>-axis at <math>(4, 0)</math>.</p> <p style="text-align: center; color: red;"><math>y = \frac{5}{3}x - \frac{20}{3}</math></p>	<p>The straight line <math>L_1</math> has equation <math>x + 2y - 7 = 0</math>. The straight line <math>L_2</math> passes through the points <math>(-2, -6)</math> and <math>(5, 8)</math>. Show that the lines <math>L_1</math> and <math>L_2</math> are perpendicular to each other.</p> <p style="text-align: center; color: red;"><math>m \text{ for } L_1 = -\frac{1}{2} \quad m \text{ for } L_2 = 2</math></p> <p style="text-align: center; color: red;"><math>-\frac{1}{2} \times 2 = -1, \text{ therefore perpendicular}</math></p>
(d)	(e)	(f)
<p>The straight line <math>L</math> passes through the points <math>(1, -1)</math> and <math>(5, 9)</math>. Find an equation of the line that is parallel to <math>L</math> and passes through the point <math>(2, 4)</math>. Give your answer in the form <math>ax + by + c = 0</math> where <math>a</math>, <math>b</math> and <math>c</math> are integers.</p> <p style="text-align: center; color: red;"><math>5x - 2y - 2 = 0</math></p>	<p>The straight line <math>L_1</math> has equation <math>2x - 3y = 4</math>. The straight line <math>L_2</math> is perpendicular to <math>L_1</math> and passes through the point <math>(1, 2)</math>. Find the equation of the line <math>L_2</math> and the coordinates of the point where it crosses the <math>x</math>-axis.</p> <p style="text-align: center; color: red;"><math>y = -\frac{3}{2}x + \frac{7}{2}</math></p> <p style="text-align: center; color: red;"><math>(\frac{7}{3}, 0)</math></p>	<p><math>ABC</math> is a triangle, where <math>\widehat{BAC} = 90^\circ</math>. The point <math>C</math> has coordinates <math>(9, 5)</math> and points <math>A</math> and <math>B</math> lie on the line with equation <math>2x + 3y = 7</math>. Find the equation of the line that passes through <math>A</math> and <math>C</math>, giving your answer in the form <math>ax + by = c</math> where <math>a</math>, <math>b</math> and <math>c</math> are integers.</p> <p style="text-align: center; color: red;"><math>3x - 2y = 17</math></p>

# Exam Questions

**Q1.**  $y = 5x - 4$  is the equation of a straight line.

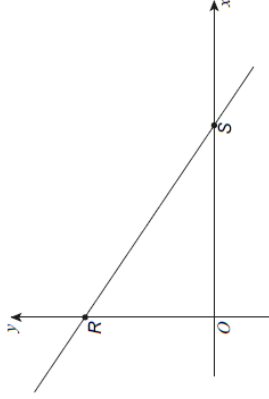
(a) Write down the gradient of the line  $y = 5x - 4$

Answer ..... (1)

(b) Write down the coordinates of the  $y$ -intercept of the line  $y = 5x - 4$

Answer (....., .....), ..... (1)  
 (Total 2 marks)

**Q2.** A sketch of  $2x + 3y = 12$  is shown.



(a) Work out the coordinates of  $R$ .

Answer (....., .....), ..... (1)

(b) Work out the coordinates of  $S$ .

Answer (....., .....), ..... (2)  
 (Total 3 marks)

**Q3.**

(a) Write down the equation of a straight line that is parallel to  $y = 5x + 6$

..... (1)

(b) Find an equation of the line that is perpendicular to the line  $y = 5x + 6$  and passes through the point  $(-2, 5)$ .

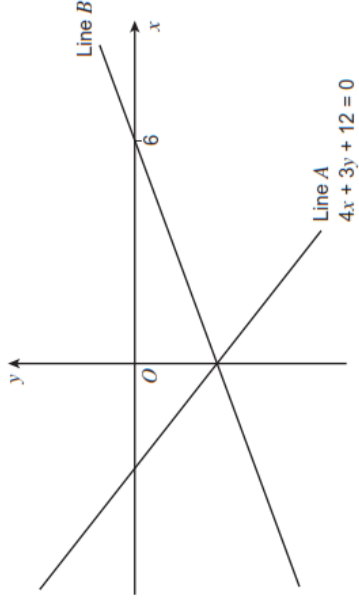
..... (3)  
 (Total 4 marks)

# Exam Questions

**Q4.** Lines,  $A$  and  $B$ , intersect on the  $y$ -axis.

Line  $B$  intersects the  $x$ -axis at the point  $(6, 0)$ .

The equation of line  $A$  is  $4x + 3y + 12 = 0$



Work out the equation of line  $B$ .

Answer .....

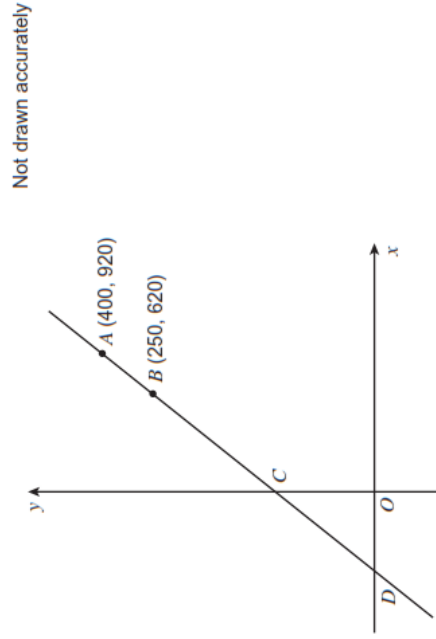
(Total 4 marks)

**Q5.** The diagram shows a line  $ABCD$ .

$A$  is the point  $(400, 920)$ .

$B$  is the point  $(250, 620)$ .

The line cuts the  $y$ -axis at  $C$  and the  $x$ -axis at  $D$ .



Work out the coordinates of  $C$  and  $D$ .

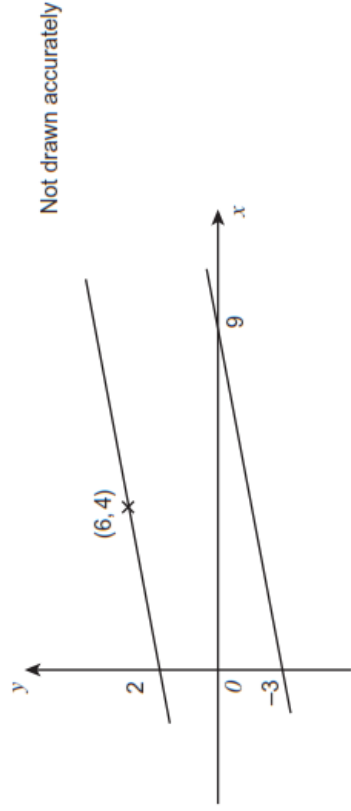
$C$  ( ..... , ..... )

$D$  ( ..... , ..... )

# Exam Questions

(Total 4 marks)

**Q6.** Two straight lines are shown.

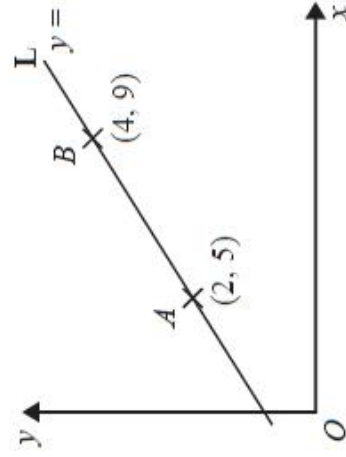


Prove that the lines never meet.

Page 69

(Total 3 marks)

**Q7.**



The point  $A$  has coordinates  $(2, 5)$ .

The point  $B$  has coordinates  $(4, 9)$ .

The line  $L$  passes through the points  $A$  and  $B$ .

The equation of line  $L$  is  $y = 2x + 1$

$M$  is the midpoint of the line segment  $AB$ .

Find an equation of the line that is perpendicular to line  $L$  and passes through  $M$ .



# Exam Questions

(Total 4 marks)

**\*Q8.**  $A$  is the point with coordinates  $(1, 3)$   
 $B$  is the point with coordinates  $(4, -1)$   
The straight line  $L$  goes through both  $A$  and  $B$ .  
Is the line with equation  $2y = 3x - 4$  perpendicular to line  $L$ ?  
You must show how you got your answer.

Page 70

(Total 4 marks)

**Q9.**

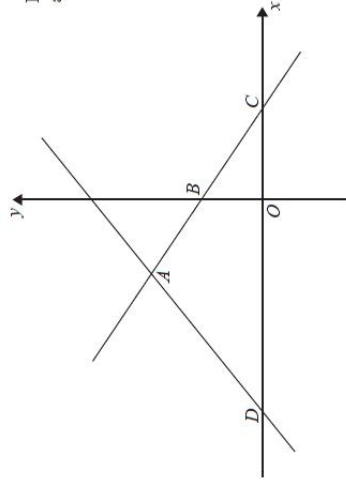


Diagram NOT  
accurately drawn

In the diagram,  $ABC$  is the line with equation  $y = -\frac{1}{2}x + 5$

$AB = BC$

$D$  is the point with coordinates  $(-13, 0)$

Find an equation of the line through  $A$  and  $D$ .

### 3 Graphical Inequalities

## Extension

linear inequalities: regions

(1)  $y \leq 2x + 3$

$$x \leq 3$$

$$y \geq 5$$

(2)  $x + 2y \geq 8$

$$x \leq 6$$

$$y \leq 3$$

(3)  $x + y \geq 9$

$$x \leq 4$$

$$y \leq x + 5$$

(4)  $y \geq 2x - 3$

$$y \geq 3$$

$$y \leq x + 2$$

(5)  $y \leq \frac{1}{3}x + 6$

$$y \geq x$$

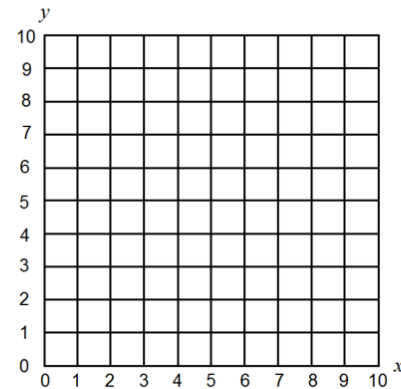
$$y \geq 7$$

(6)  $x + 2y \geq 8$

$$x \leq 6$$

$$2y \leq 3x - 8$$

find each of these regions  
on a 10 by 10 grid:



the region for all questions should  
be a triangle with an area of  
4 squares

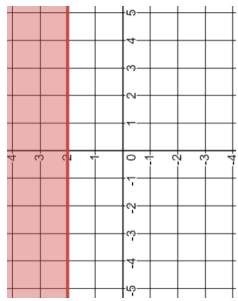
establish that this is the case

# Fluency Practice

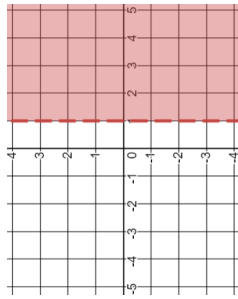
## Describing Graphical Inequalities

Write down the inequality or inequalities that define the shaded region.

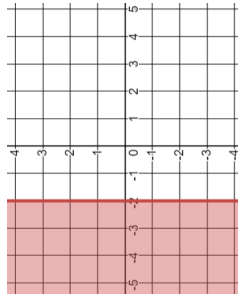
**(a)**



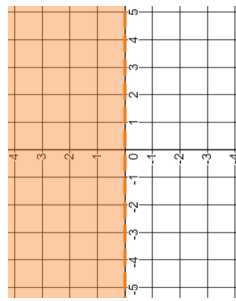
**(b)**



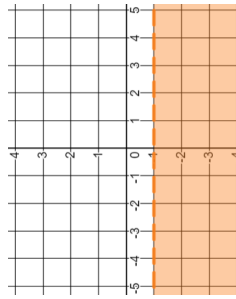
**(c)**



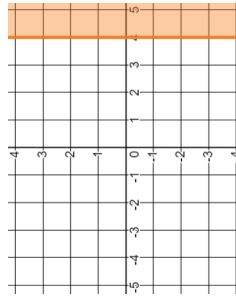
**(d)**



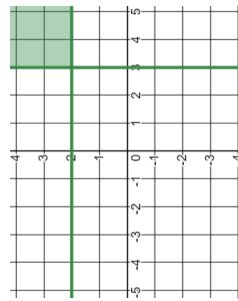
**(e)**



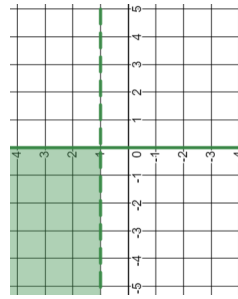
**(f)**



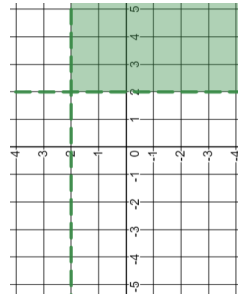
**(g)**



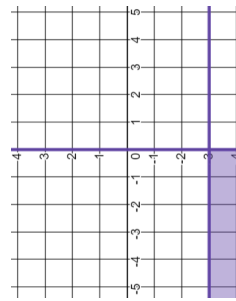
**(h)**



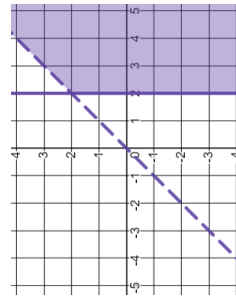
**(i)**



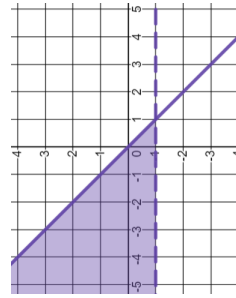
**(j)**



**(k)**



**(l)**

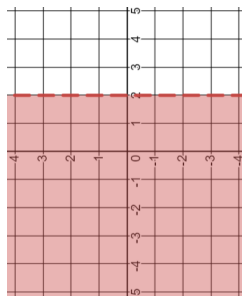


# Fluency Practice

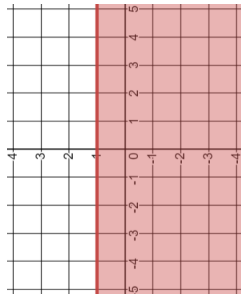
## Describing Harder Graphical Inequalities

Write down the inequality or inequalities that define the shaded region.

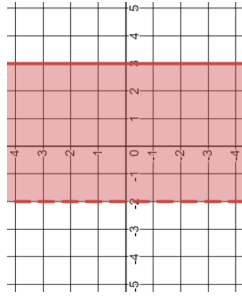
**(a)**



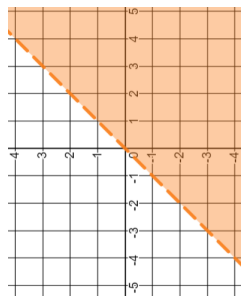
**(b)**



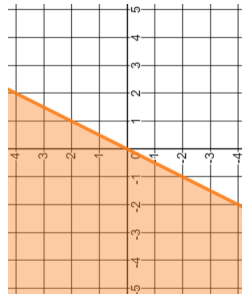
**(c)**



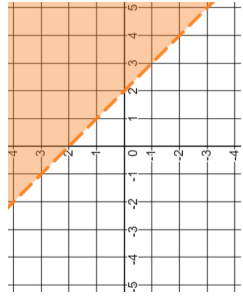
**(d)**



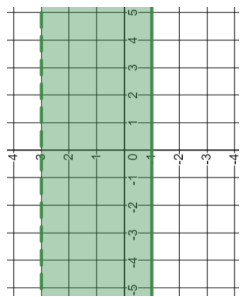
**(e)**



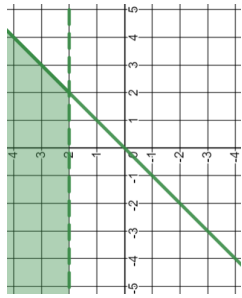
**(f)**



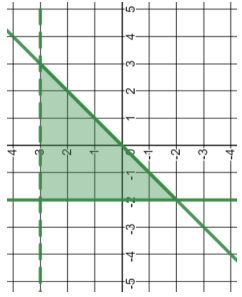
**(g)**



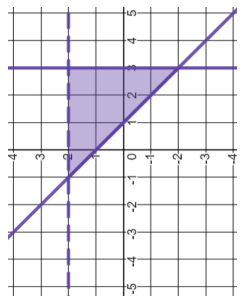
**(h)**



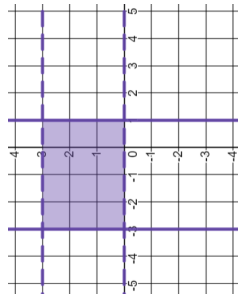
**(i)**



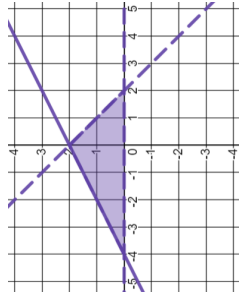
**(j)**



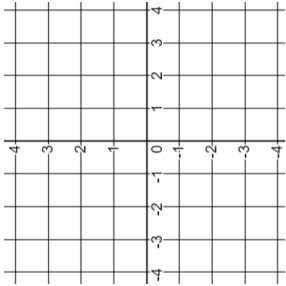
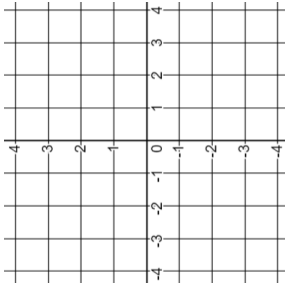
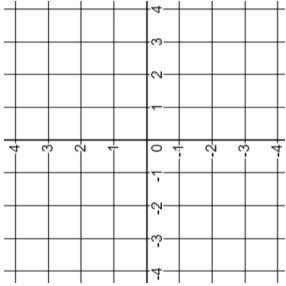
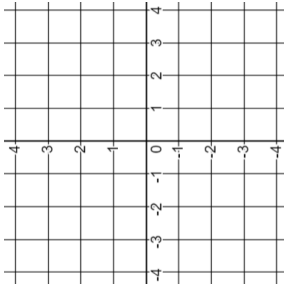
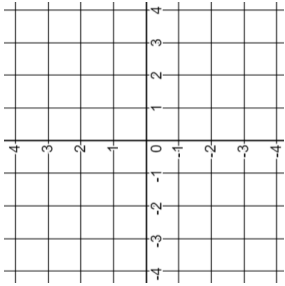
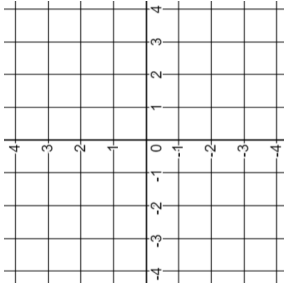
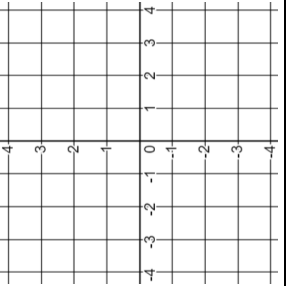
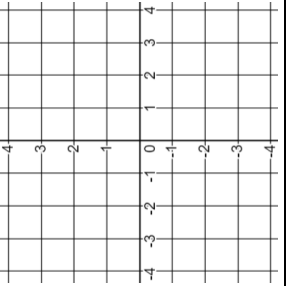
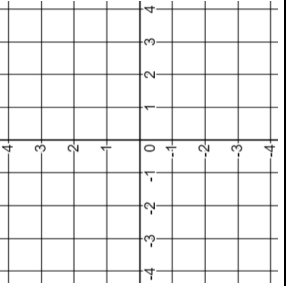
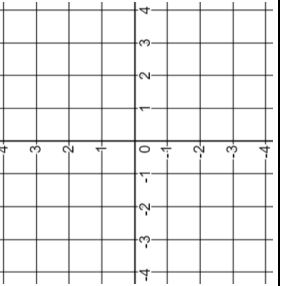
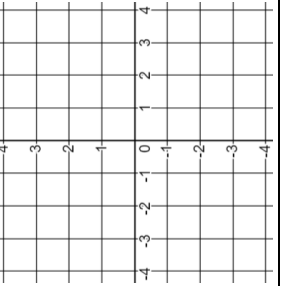
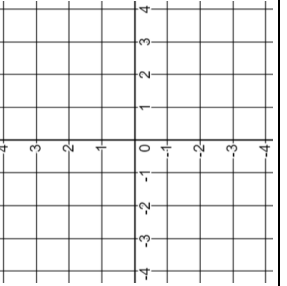
**(k)**



**(l)**

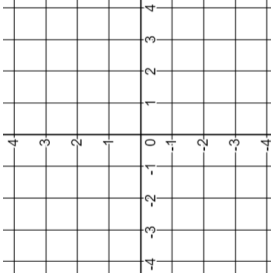
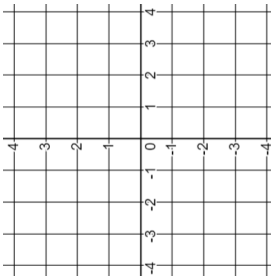
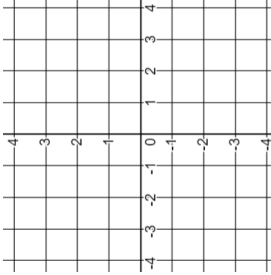
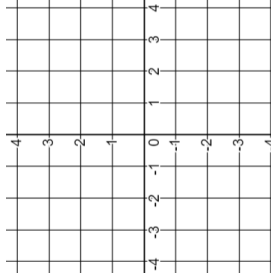
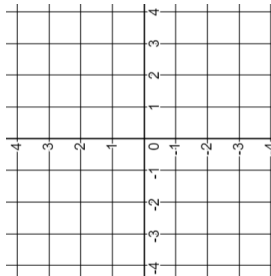
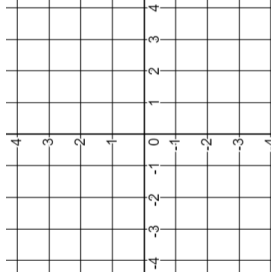
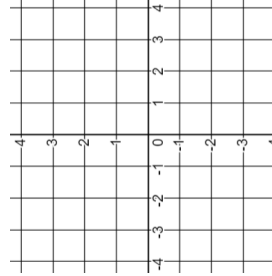
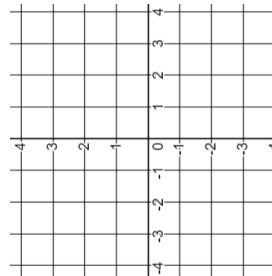
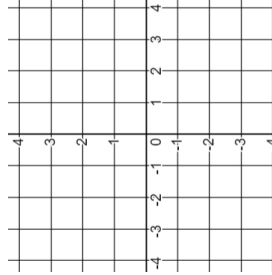
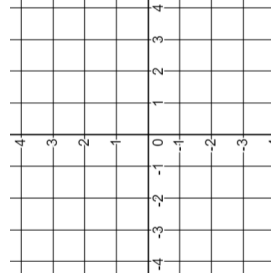
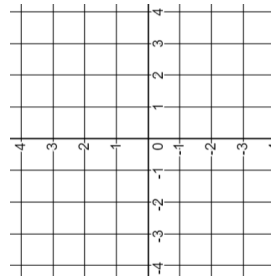
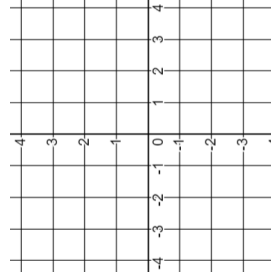


# Fluency Practice

Shading Graphical Inequalities		
<b>(a)</b>	<b>(b)</b>	<b>(c)</b>
$y > 1$	$y \leq -2$	$x < 0$
		
<b>(d)</b>	<b>(e)</b>	<b>(f)</b>
$x \geq 3$	$y \geq 0$	$x \leq -3$
		
<b>(g)</b>	<b>(h)</b>	<b>(i)</b>
$x \geq 2 \text{ and } y < 1$	$x < -1 \text{ and } y > 3$	$x \leq 0 \text{ and } y < 0$
		
<b>(j)</b>	<b>(k)</b>	<b>(l)</b>
$x \geq -1 \text{ and } y \geq 3$	$y \geq x \text{ and } x < 2$	$y < -x \text{ and } y \leq -1$
		

# Fluency Practice

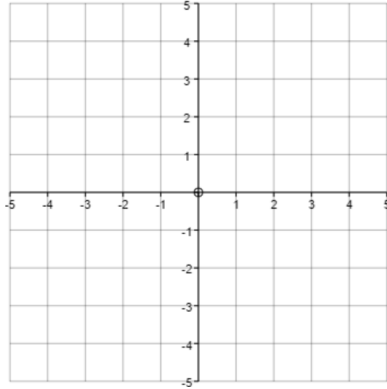
## Shading Harder Graphical Inequalities

Shading Harder Graphical Inequalities		
<b>(a)</b>	<b>(b)</b>	<b>(c)</b>
$y \geq -1$	$x < 2$	$y > x$
		
<b>(d)</b>	<b>(e)</b>	<b>(f)</b>
$y \geq 0.5x - 1$	$x + y \leq 3$	$-3 \leq y < 2$
		
<b>(g)</b>	<b>(h)</b>	<b>(i)</b>
$-2 \leq x < 3$	$x \geq 0$ and $y < x$	$x \geq -1, y > 0$ and $x + y < 2$
		
<b>(j)</b>	<b>(k)</b>	<b>(l)</b>
$2 < x < 4$ and $-1 \leq y \leq 1$	$y < 2x, x + y \leq 4$ and $y > 0$	$y < x, y \geq -2$ and $2x + y < 4$
		

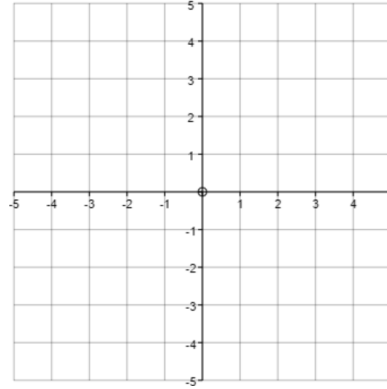
# Fluency Practice

## Shading and Describing Harder Graphical Inequalities

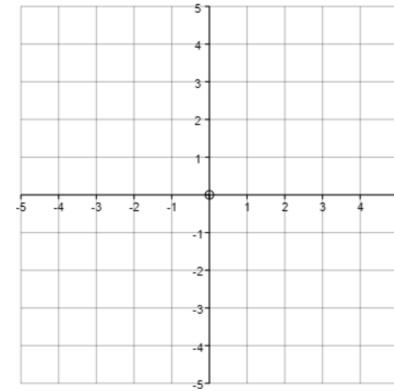
Shade the region that satisfies the inequalities  $x \leq 4$   $y \geq -1$   $y \leq x$



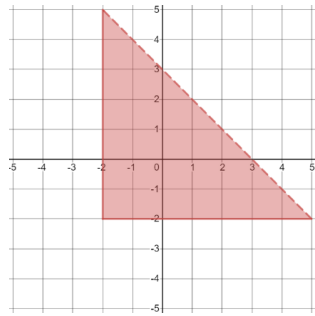
Shade the region that satisfies the inequalities  $x > -1$   $y \geq 0$   $x + y \leq 3$



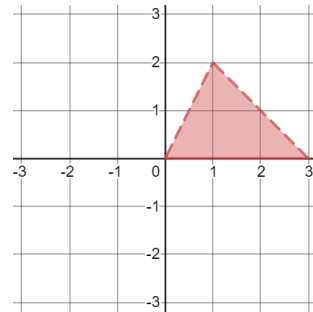
Shade the region that satisfies the inequalities  $2x + 3y < 6$   $y \leq x + 2$   $y > -1$



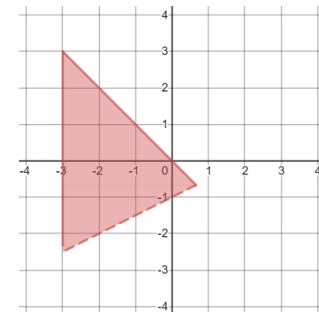
Write down the inequalities which fully describe the shaded region.



Write down the inequalities which fully describe the shaded region.



Write down the inequalities which fully describe the shaded region.

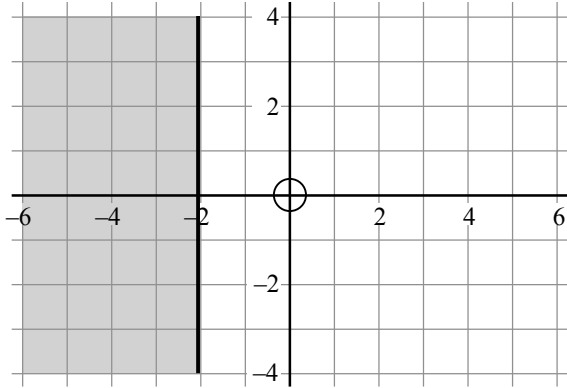




# Fluency Practice

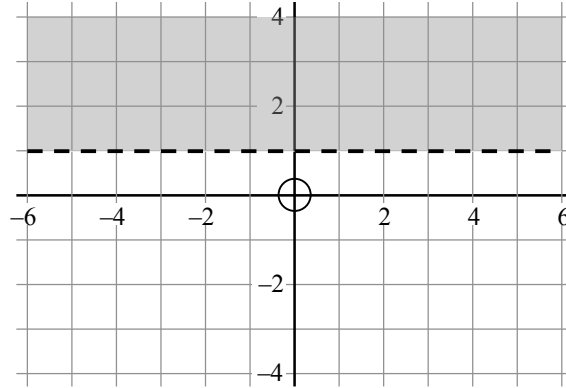
**A1**

Write down the inequality which defines the unshaded region.



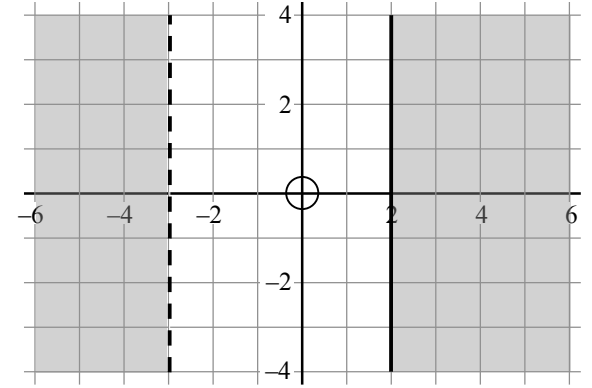
**A2**

Write down the inequality which defines the unshaded region.



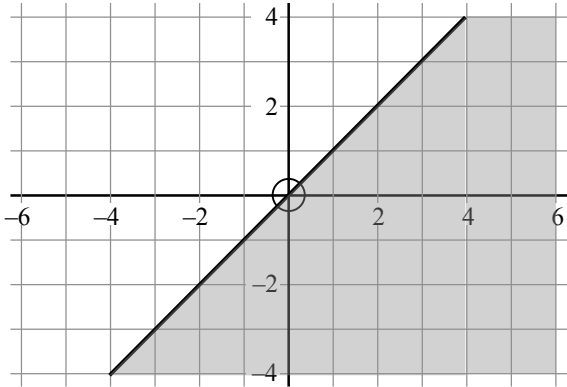
**A3**

Write down the inequalities which define the unshaded region.



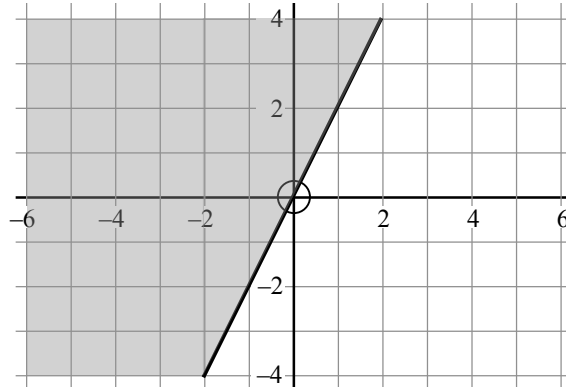
**B1**

Write down the inequality which defines the unshaded region.



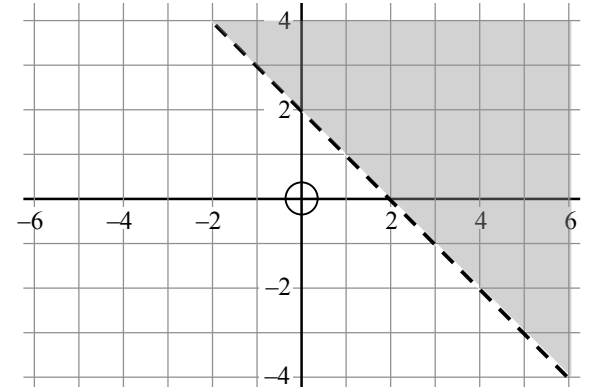
**B2**

Write down the inequality which defines the unshaded region.



**B3**

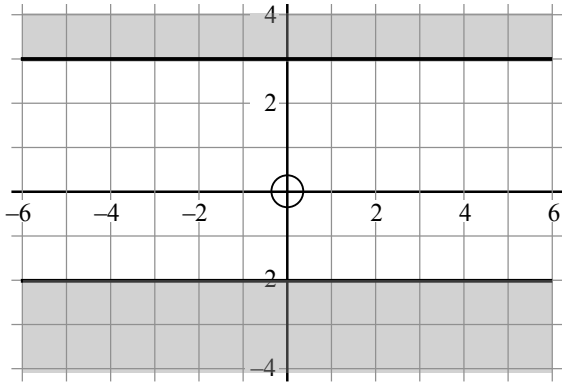
Write down the inequality which defines the unshaded region.



# Fluency Practice

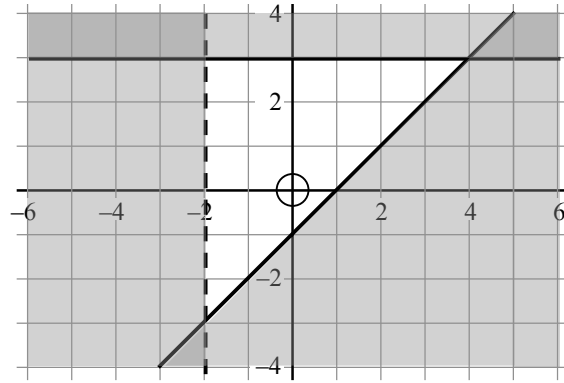
**A1**

Write down the inequalities which fully define the unshaded region.



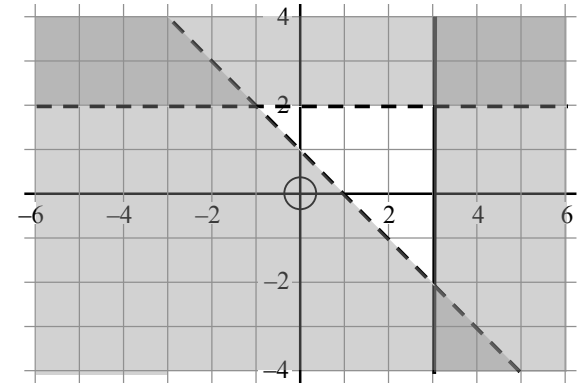
**A2**

Write down the inequalities which fully define the unshaded region.



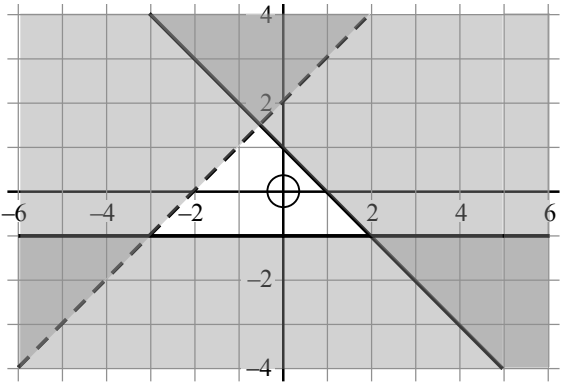
**A3**

Write down the inequalities which fully define the unshaded region.



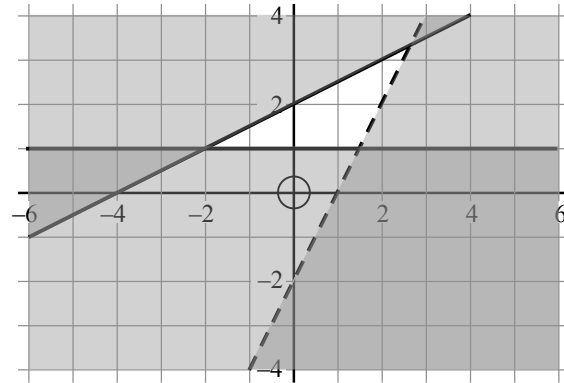
**B1**

Write down the inequalities which fully define the unshaded region.



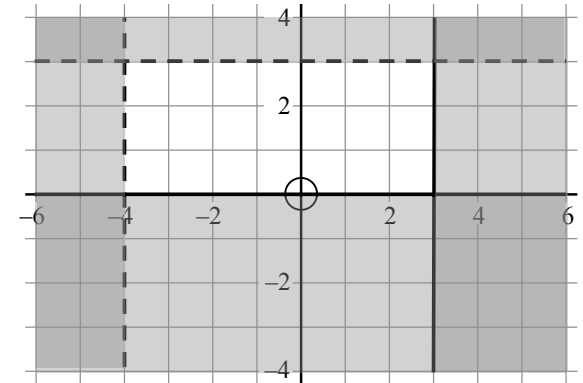
**B2**

Write down the inequalities which fully define the unshaded region.



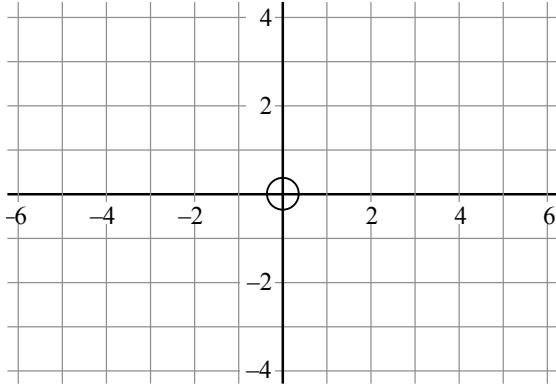
**B3**

Write down the inequalities which fully define the unshaded region.

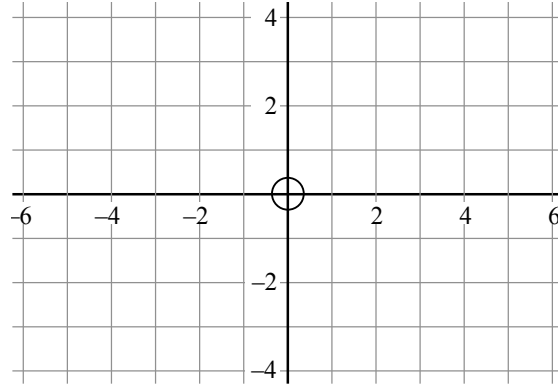


# Fluency Practice

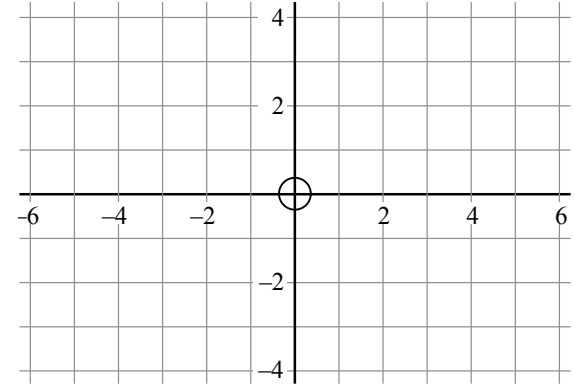
**A1** Show, by shading on the grid, the region defined by  $y \geq -1$   
Label your region **R**.



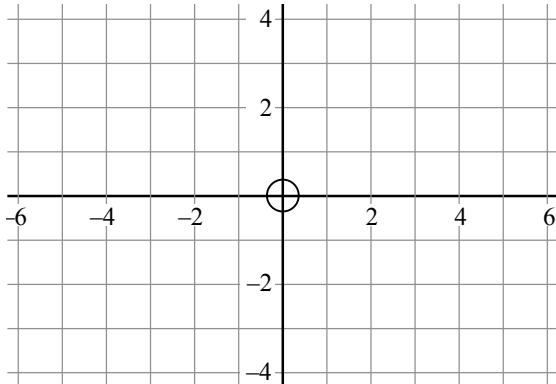
**A2** Show, by shading on the grid, the region defined by  $x < 3$   
Label your region **R**.



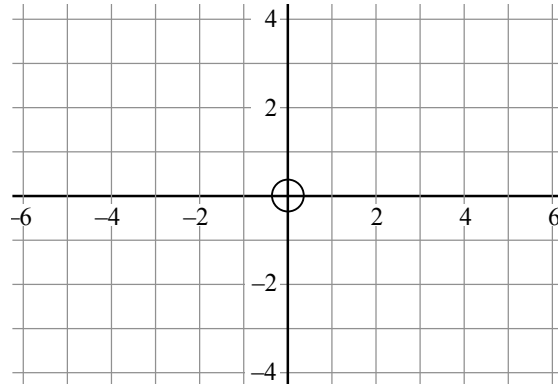
**A3** Show, by shading on the grid, the region defined by  $y < x$   
Label your region **R**.



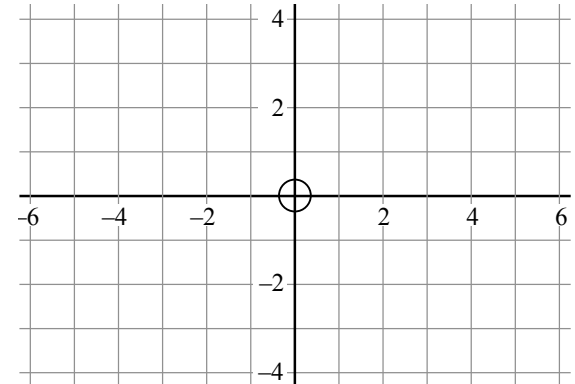
**B1** Show, by shading on the grid, the region defined by  $y \geq 0.5x - 1$   
Label your region **R**.



**B2** Show, by shading on the grid, the region defined by  $x + y \leq 3$   
Label your region **R**.

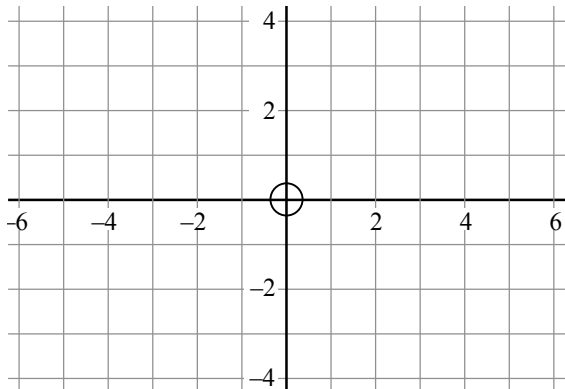


**B3** Show, by shading on the grid, the region defined by  $-3 \leq y < 2$   
Label your region **R**.

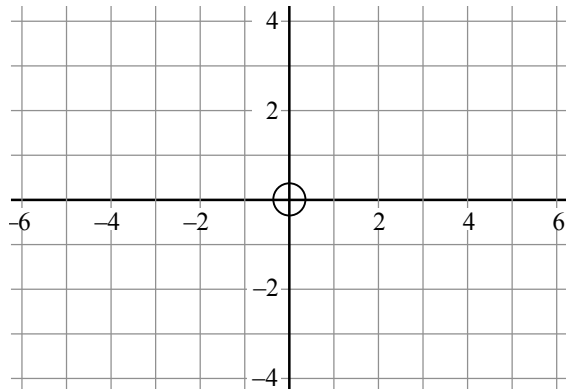


# Fluency Practice

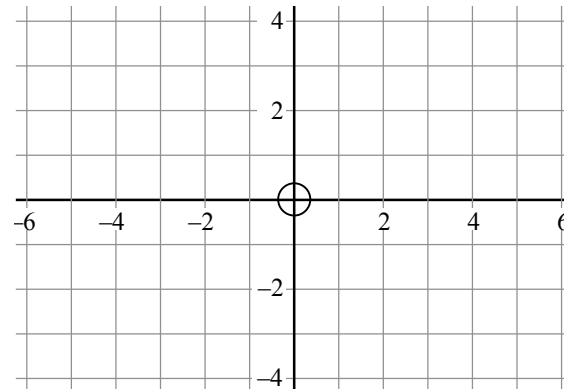
**A1** Show, by shading on the grid, the region defined by  $-4 \leq x \leq 3$   
Label your region **R**.



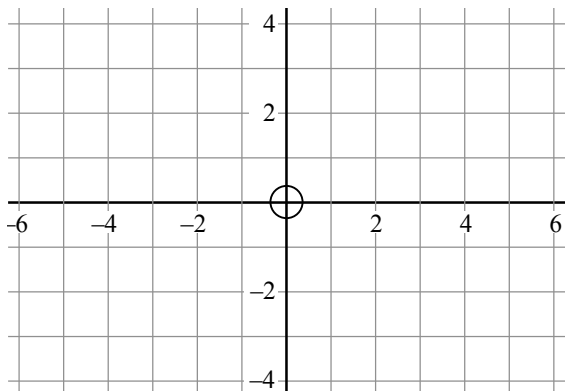
**A2** Show by shading on the grid the region defined by  $x \geq -3$ ,  $y < 2$  and  $y > x$   
Label your region **R**.



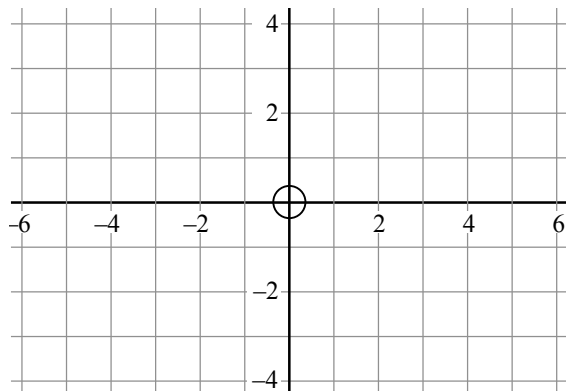
**A3** Show by shading on the grid the region defined by  $x + y \leq -1$ ,  $x \geq -4$  and  $y \geq -3$   
Label your region **R**.



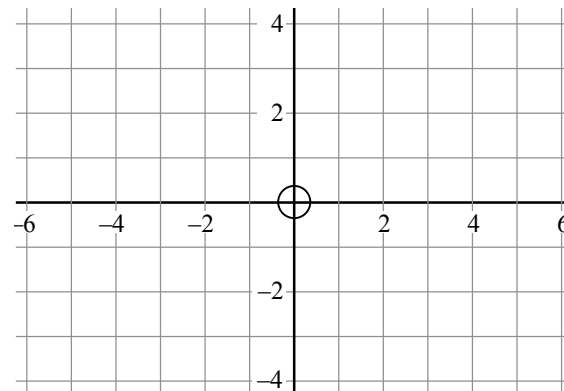
**B1** Show by shading on the grid the region defined by  $-2 < y \leq 3$  and  $-3 \leq x < 5$   
Label your region **R**.



**B2** Mark with a cross (x) a point on the grid which satisfies both the inequalities  $x > 1$  and  $x - 3y > 3$



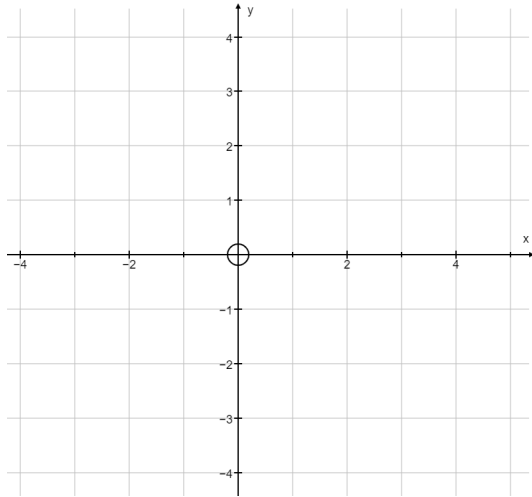
**B3** Show by shading on the grid the region defined by  $y > x + 3$ ,  $x \geq -3$  and  $2y - x \leq 4$   
Label your region **R**.



# Interwoven Maths – Pythagoras' Theorem with Inequalities

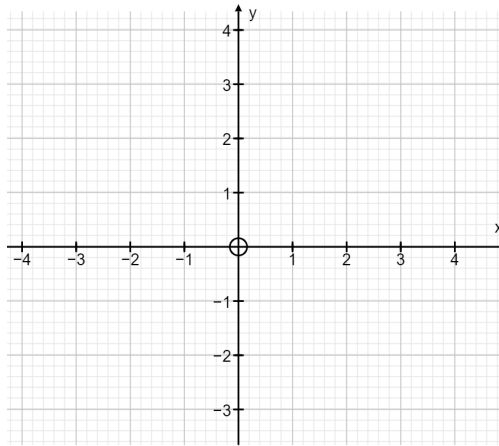
Identify the region described by the inequalities and calculate the perimeter of the region.

$$\begin{aligned} y &\geq 1 \\ x &\geq 2 \\ 2y + x &\leq 6 \end{aligned}$$



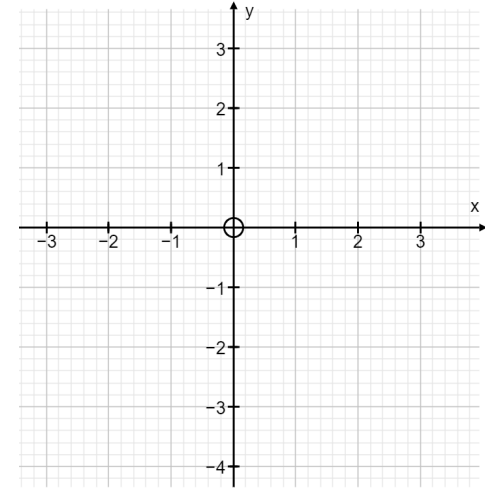
Perimeter:

$$\begin{aligned} y &\geq 0 \\ y &\leq 1.5x \\ y &\geq 3x - 9 \\ y &\leq 3 \end{aligned}$$



Perimeter:

$$\begin{aligned} y &\leq 4x + 11 \\ 5y + 4x &\leq 7 \\ y &\geq -1 \end{aligned}$$

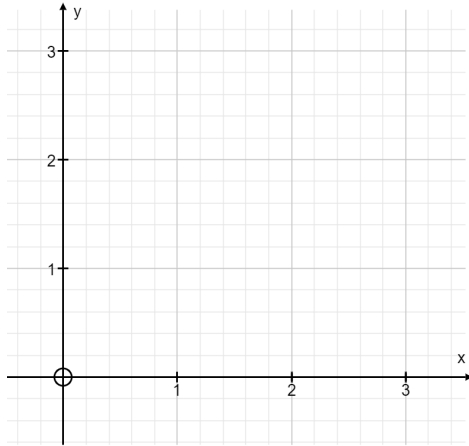


Perimeter:

## Interwoven Maths – Pythagoras' Theorem with Inequalities

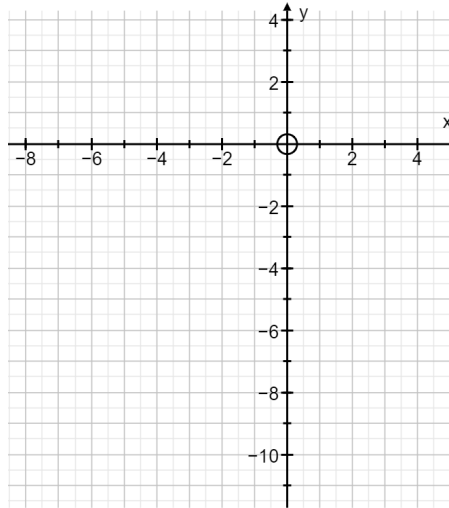
Identify the region described by the inequalities and calculate the perimeter of the region.

$$\begin{aligned} y &\geq \frac{2}{3}x \\ y &\leq 1.5x \\ x &\leq 3 \\ y &\leq 3 \end{aligned}$$



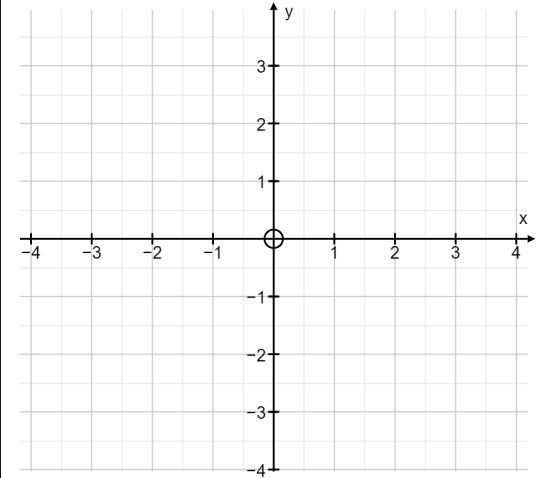
Perimeter:

$$\begin{aligned} 2y + 2x &\leq 7 \\ 2x - 2y &\leq 7 \\ 2y - 4x &\geq 7 \end{aligned}$$



Perimeter:

$$\begin{aligned} 3y + x &\leq 6 \\ 4x - 3y &\leq 9 \\ 3y - x &\leq 6 \\ 4x + 3y &\geq -9 \end{aligned}$$

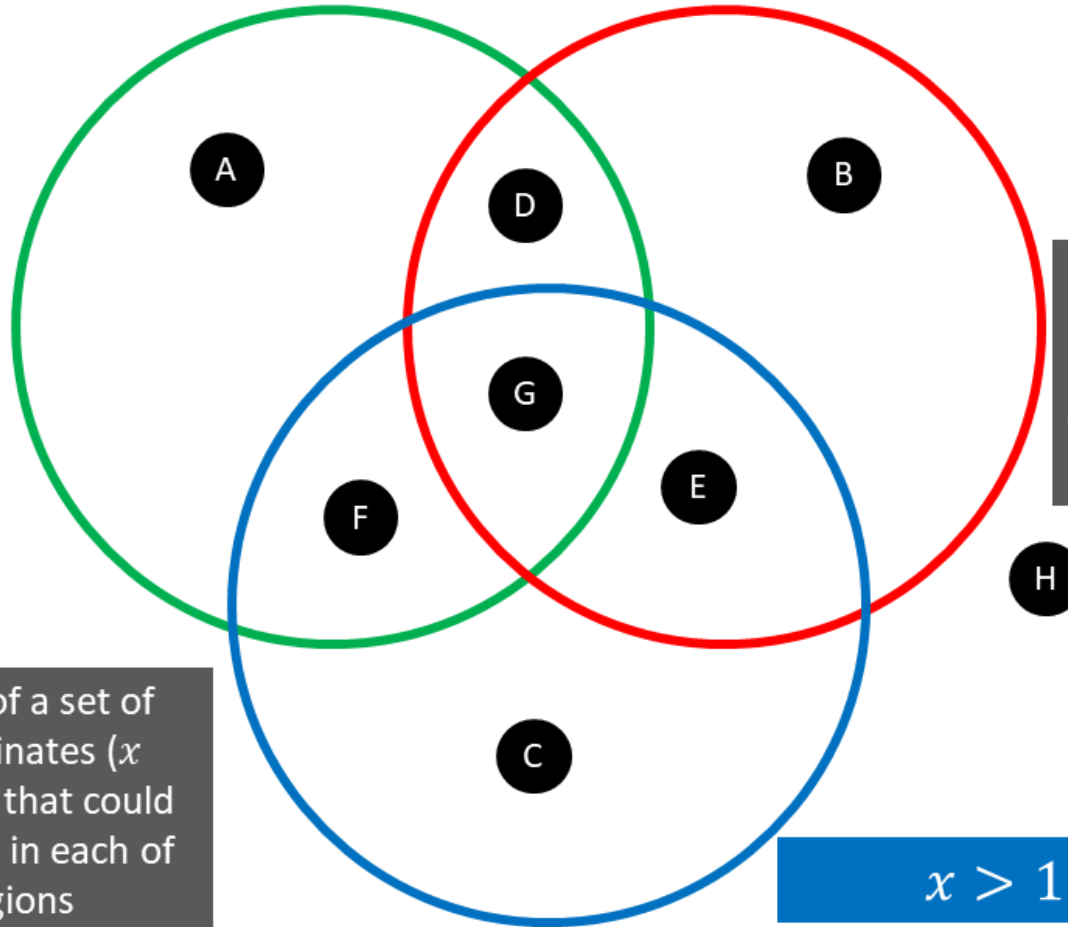


Perimeter:

# Maths Venns

$$y < 2x$$

$$y < 6$$



If you think a region is impossible to fill, convince me why!

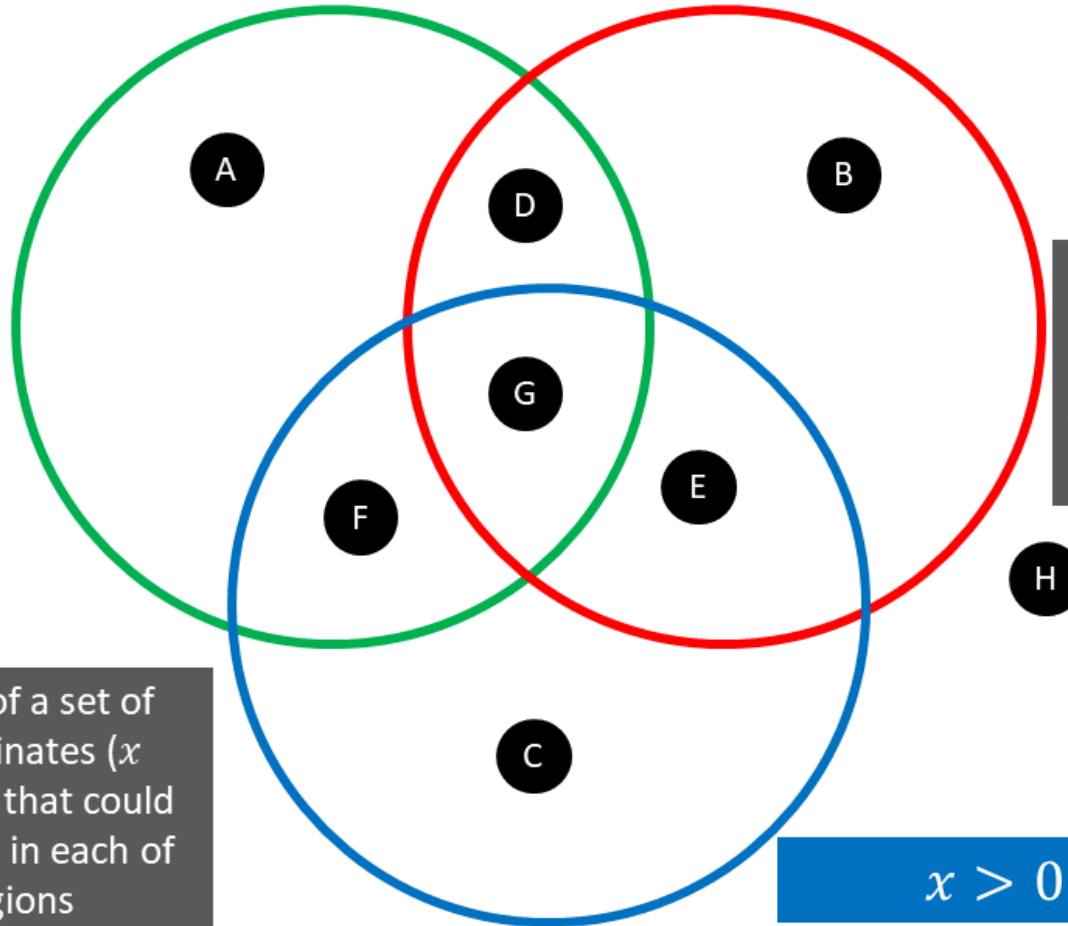
Think of a set of co-ordinates ( $x$  and  $y$ ) that could belong in each of the regions

$$x > 1$$

# Maths Venns

$$y < x$$

$$x + y < 8$$



If you think a region is impossible to fill, convince me why!

Think of a set of co-ordinates ( $x$  and  $y$ ) that could belong in each of the regions

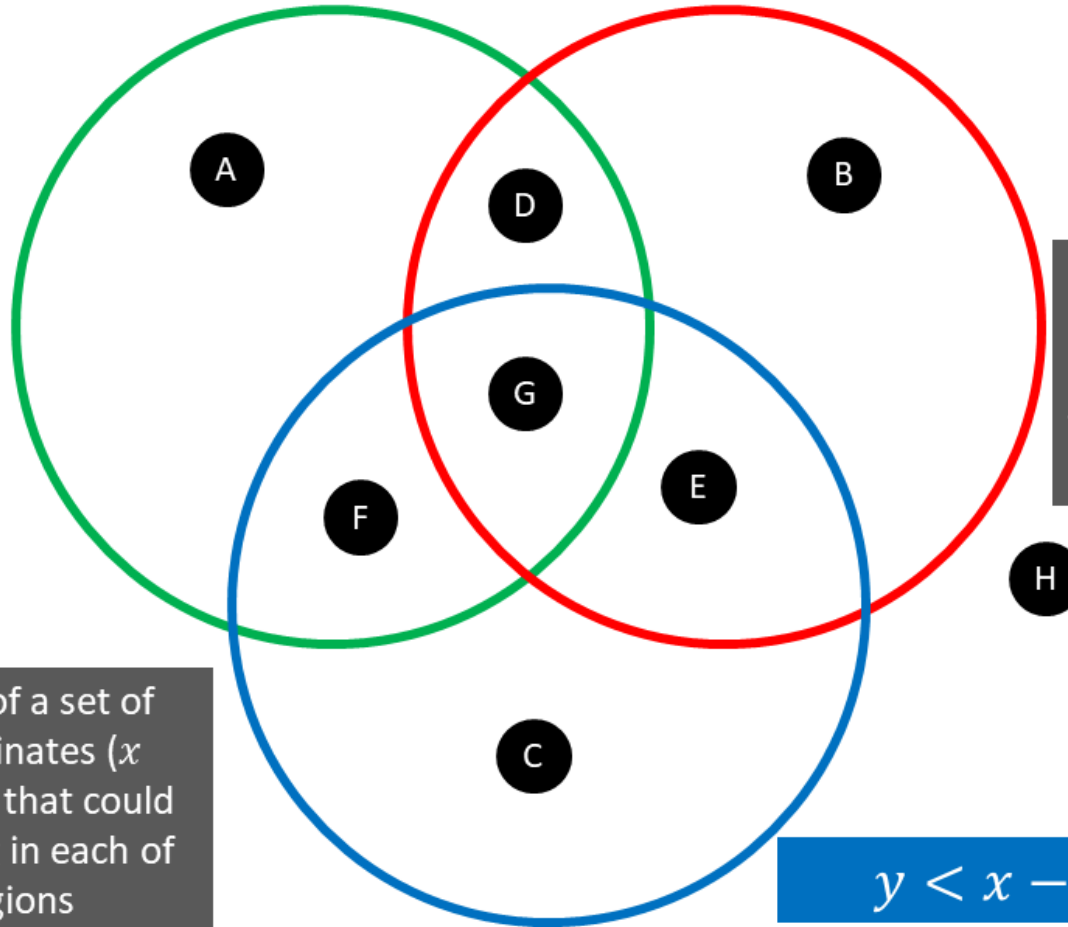
$$x > 0$$



# Maths Venns

$$y > 2x + 1$$

$$x + y < 1$$



If you think a region is impossible to fill, convince me why!

Think of a set of co-ordinates ( $x$  and  $y$ ) that could belong in each of the regions

$$y < x - 1$$

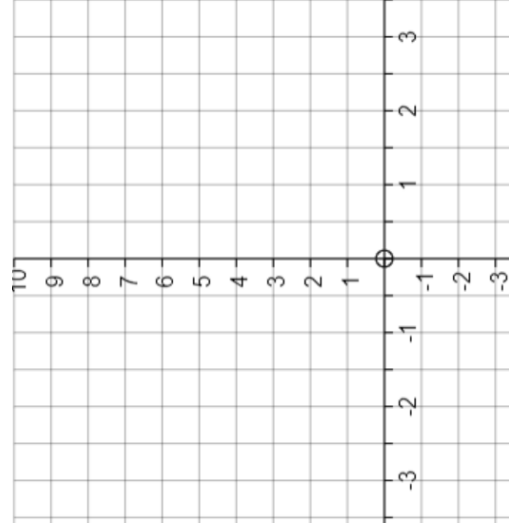
## 4 Non-Linear Graphs

# Fluency Practice

## Plotting Quadratic Graphs

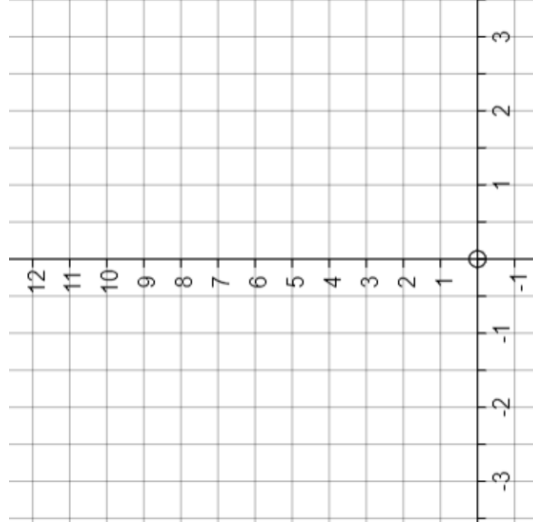
**(a)  $y = x^2$**

$x$	-3	-2	-1	0	1	2	3
$y$							



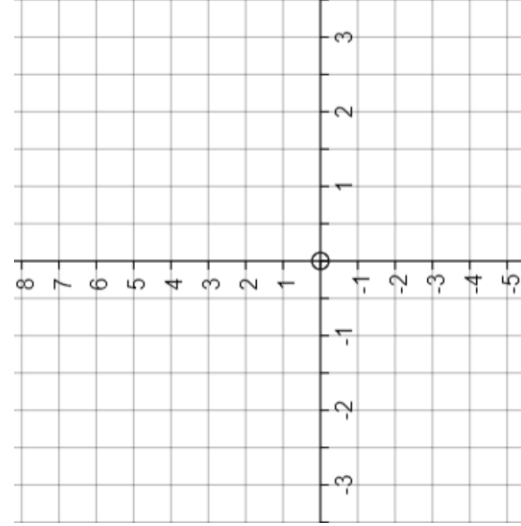
**(b)  $y = x^2 + 3$**

$x$	-3	-2	-1	0	1	2	3
$y$							



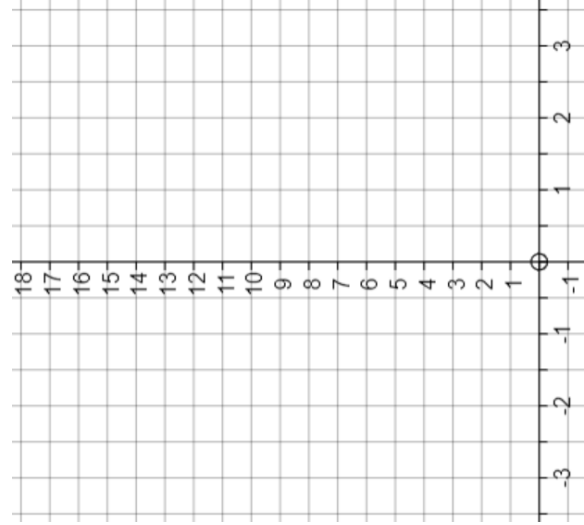
**(c)  $y = x^2 - 2$**

$x$	-3	-2	-1	0	1	2	3
$y$							



**(d)  $y = 2x^2$**

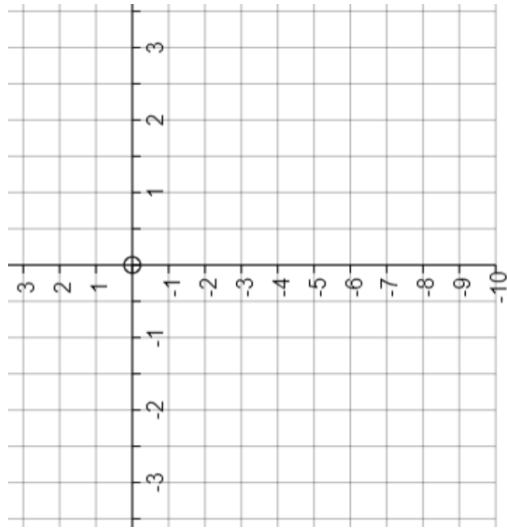
$x$	-3	-2	-1	0	1	2	3
$y$							



# Fluency Practice

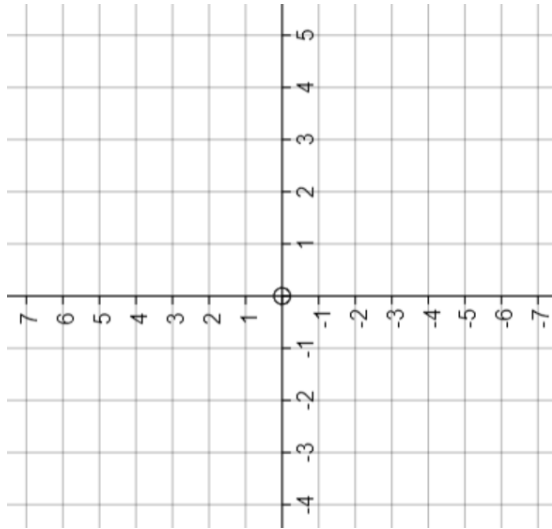
**(e)**  $y = -x^2$

$x$	-3	-2	-1	0	1	2	3
$y$							



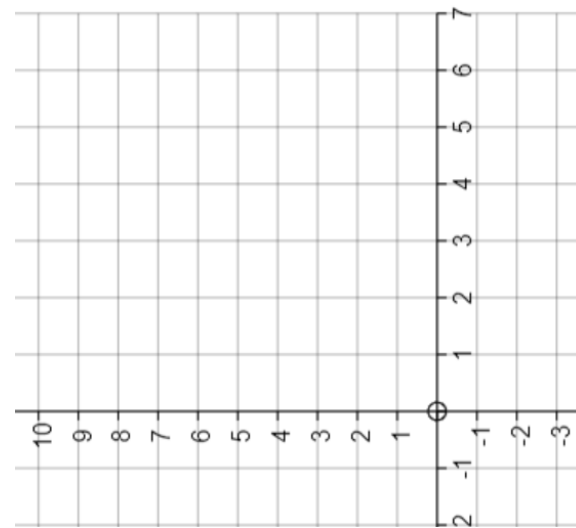
**(f)**  $y = x^2 - x - 6$

$x$	-3	-2	-1	0	1	2	3	4
$y$								



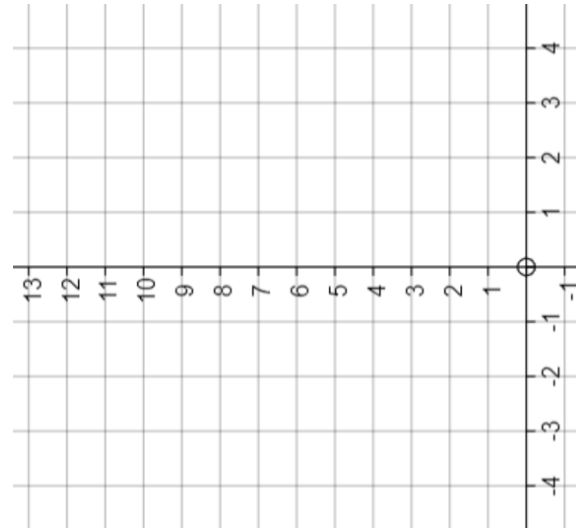
**(g)**

Plot the graph of  $y = x^2 - 5x + 4$  for  $-1 \leq x \leq 6$



**(h)**

Plot the graph of  $y = 12 + x - x^2$  for  $-3 \leq x \leq 4$



# Fluency Practice

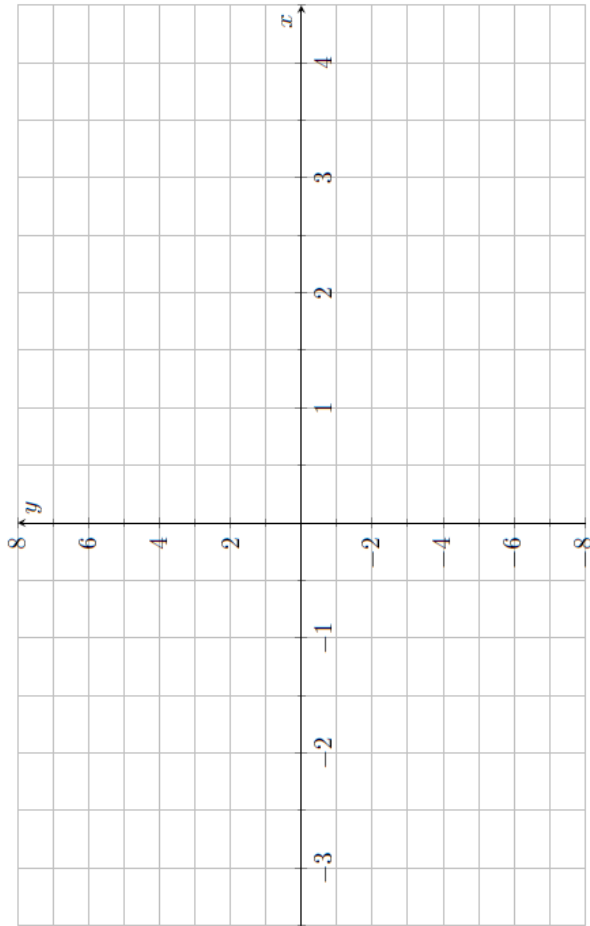
## Solving Equations Graphically

**(a)**

Plot the graph of  $y = 6 + x - x^2$ . Use the graph to find the solutions to equation

(a)  $6 + x - x^2 = 0$

(b)  $6 + x - x^2 = -6$

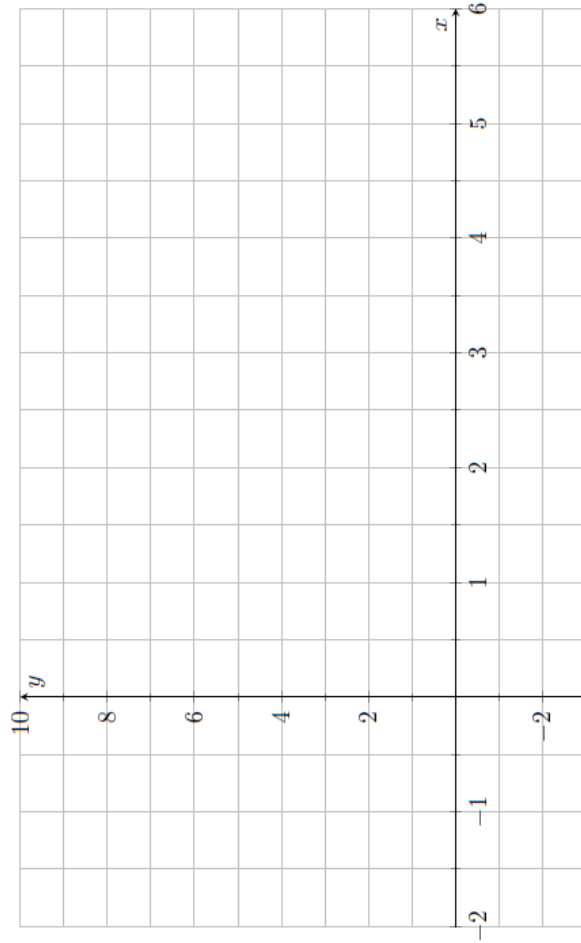


**(b)**

Plot the graph of  $y = x^2 - 4x + 3$ . Use the graph to find the solutions to equation

(a)  $x^2 - 4x + 3 = 0$

(b)  $x^2 - 4x + 3 = 8$



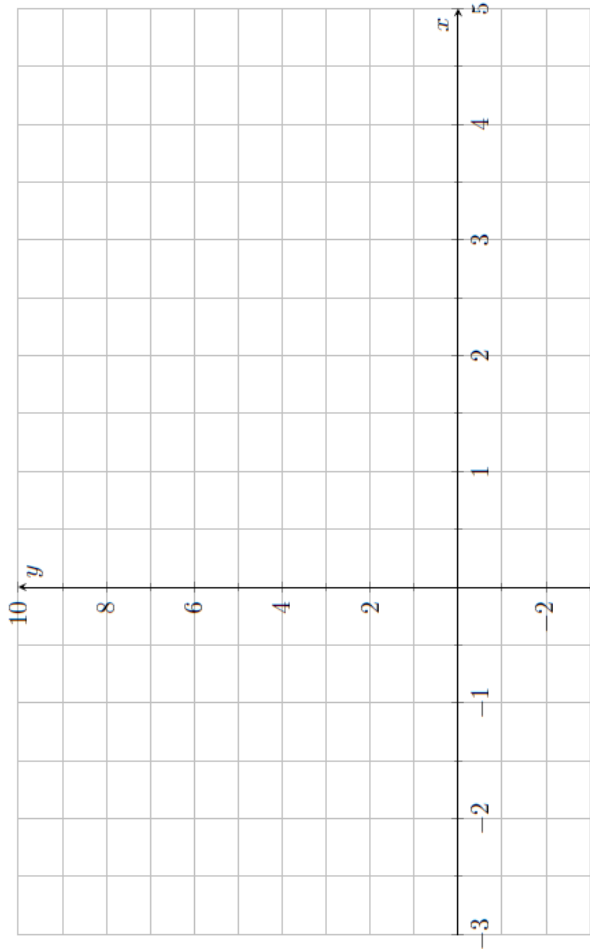
# Fluency Practice

**(c)**

Plot the graph of  $y = 8 + 2x - x^2$ . Use the graph to find the solutions to the equation

(a)  $8 + 2x - x^2 = 5$

(b)  $8 + 2x - x^2 = 8 - x$

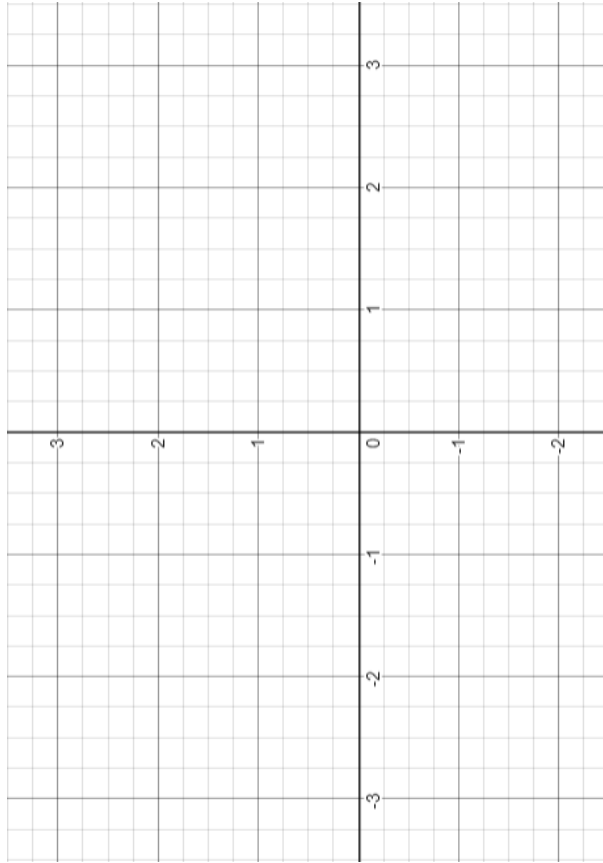


**(d)**

Plot the graph of  $y = x^3 - 3x$ . Use the graph to estimate the solutions to the equation

(a)  $x^3 - 3x = 1$

(b)  $x^3 - 3x = x + 1$



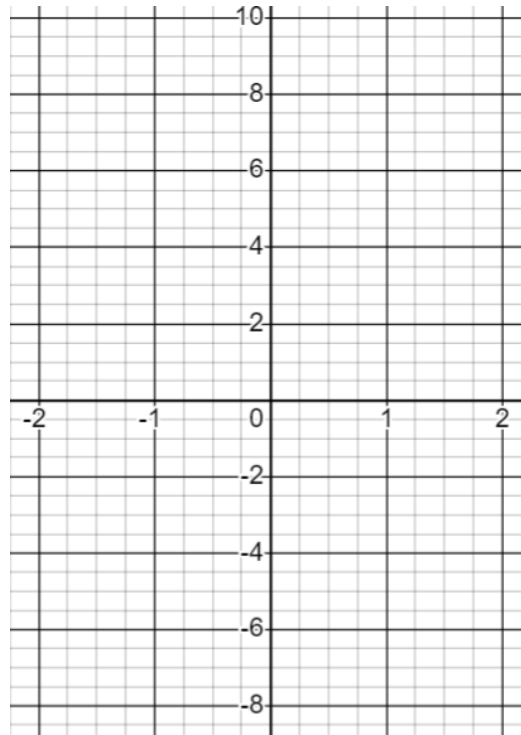
# Fluency Practice

## Plotting Cubic Graphs

**(a)**

Plot the graph of  $y = x^3 + 1$   
from  $x = -2$  to  $x = 2$

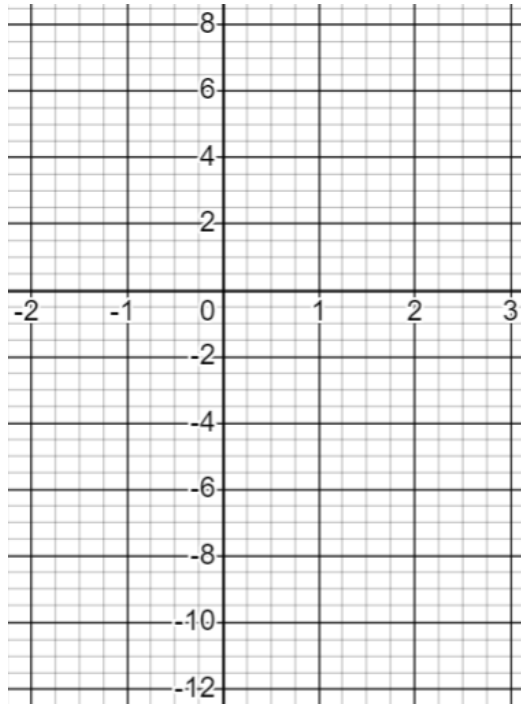
$x$	-2	-1	0	1	2
$y$					



**(b)**

Plot the graph of  $y = x^3 - 2x^2 - x + 2$   
from  $x = -2$  to  $x = 3$

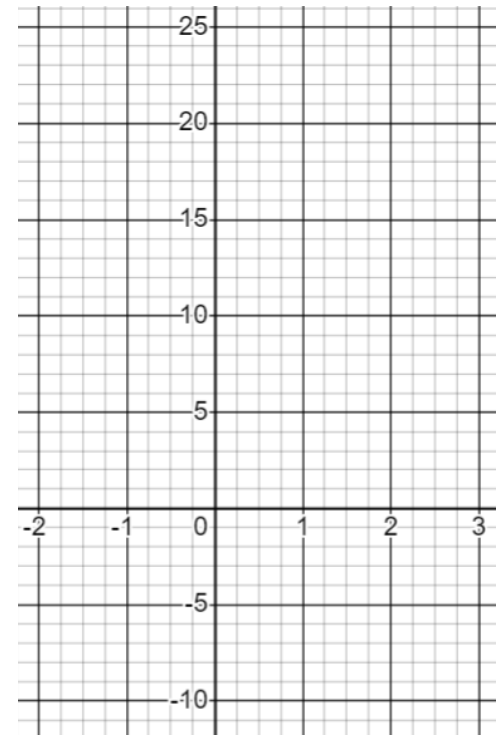
$x$	-2	-1	0	1	2	3
$y$						



**(c)**

Plot the graph of  $y = 3 - x + 2x^2 - x^3$   
from  $x = -2$  to  $x = 3$

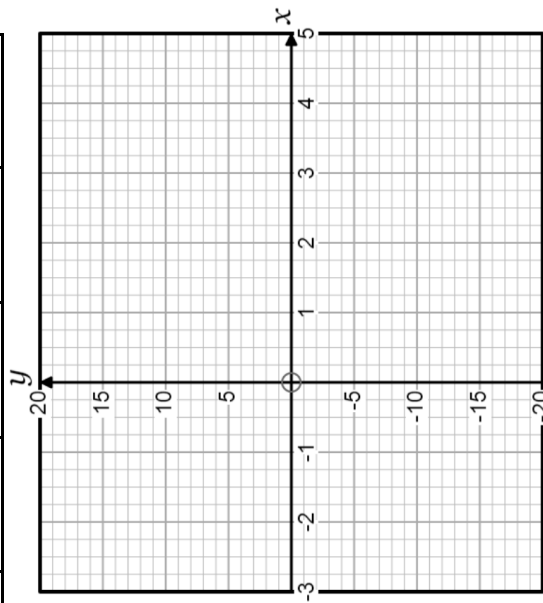
$x$	-2	-1	0	1	2	3
$y$						



# Fluency Practice

1. Draw the graph of  $y = x^3 - 4x^2 + 3$

x	-2	-1	0	1	2	3	4
y							



2. Estimate the roots of

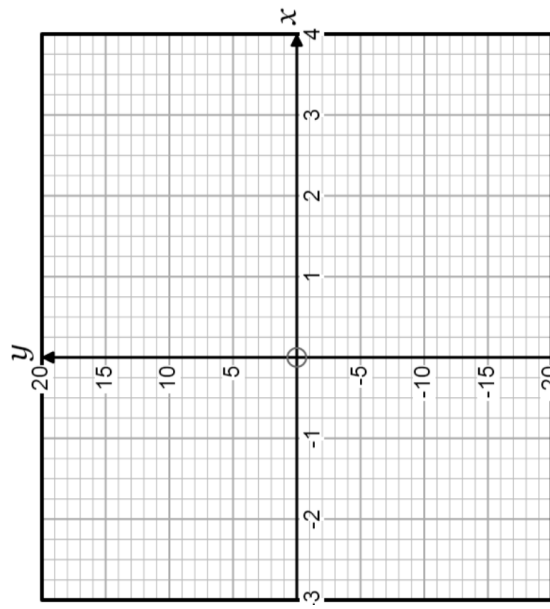
$$y = x^3 - 4x^2 + 3$$

3. Estimate the co-ordinates of the turning points of

$$y = x^3 - 4x^2 + 3$$

4. Draw the graph of  $y = 2x(x-2)(x+2)$

x	-2.5	-2	-1	0	1	2	2.5
y							



5. What are the roots of  $y = 2x(x-2)(x+2)$ ?

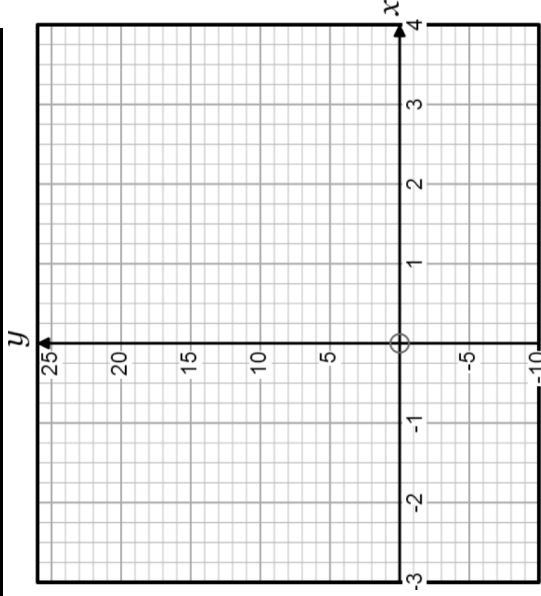
6. Estimate the co-ordinates of the turning points of  $y = 2x(x-2)(x+2)$



# Fluency Practice

7. Draw the graph of  $y = 5 - x^3 + 3x^2$

x	-2	-1	0	1	2	3	4
y							



8. Estimate the roots of  $y = 5 - x^3 + 2x^2$

9. Estimate the co-ordinates of the turning points of  $y = 5 - x^3 + 2x^2$

10. Why is this cubic graph 'upside down'?

11. Match the graphs to their functions:


$y = -x^2$

$y = 2x$

$y = (x-3)(x+1)$

$y = x^2 - 10$

$y = -x^3$

$y = 4 - x$

$y = 0.5x^2$

$y = x^3$

$y = x^3 - 3$

$y = (x-5)(x-3)(x+1)$

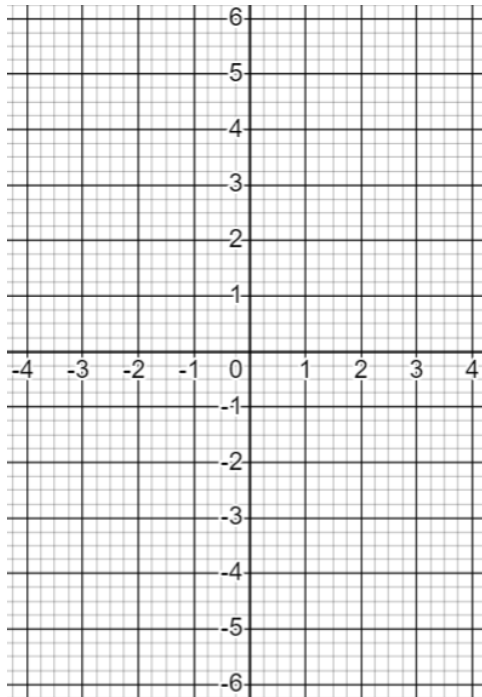
# Fluency Practice

## Plotting Reciprocal Graphs

**(a)**

Plot the graph of  $y = \frac{2}{x}$   
from  $x = -4$  to  $x = 4$

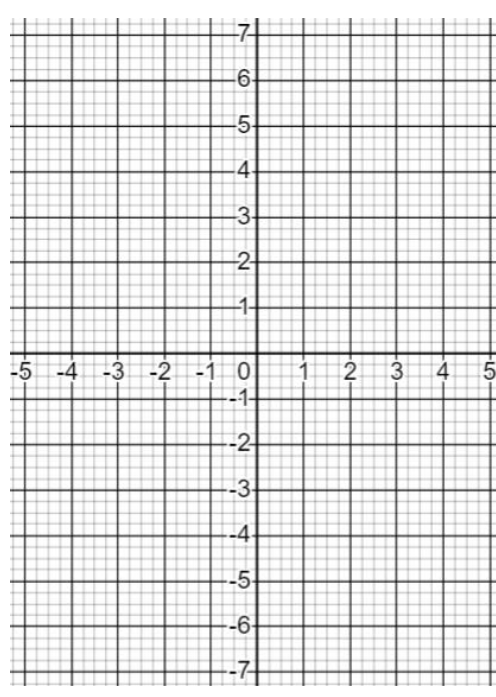
$x$	-4	-2	-1	0	1	2	4
$y$							



**(b)**

Plot the graph of  $y = -\frac{5}{x}$   
from  $x = -5$  to  $x = 5$

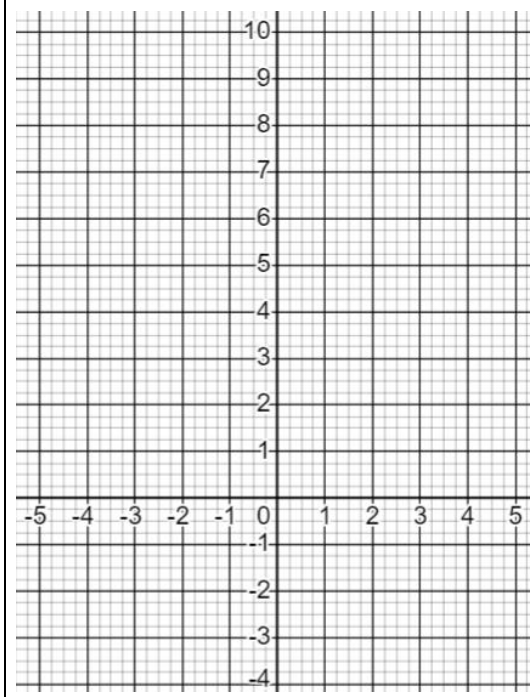
$x$	-5	-2	-1	0	1	2	5
$y$							



**(c)**

Plot the graph of  $y = \frac{10}{x^2}$   
from  $x = -2$  to  $x = 3$

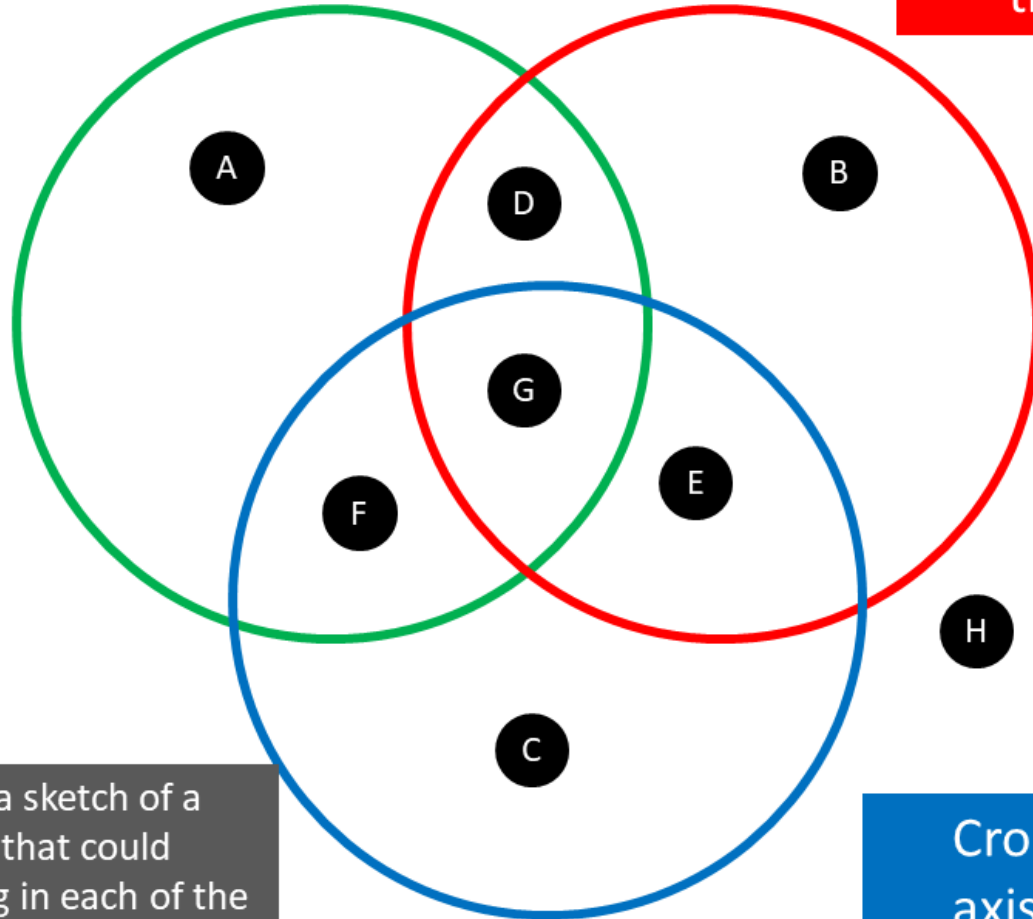
$x$	-5	-2	-1	0	1	2	5
$y$							



# Maths Venns

Is symmetrical about the y-axis

Passes through the origin



If you think a region is impossible to fill, convince me why!

BONUS:  
Can you give the equations?

Draw a sketch of a graph that could belong in each of the regions.

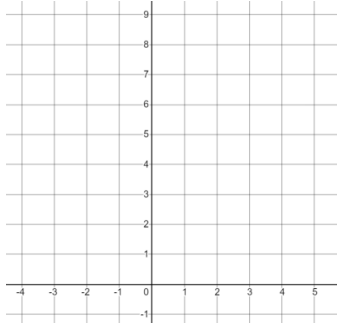
Crosses the x-axis twice

# Fluency Practice

**(a)**

Plot the graph of the equation  $y = 2x + 3$

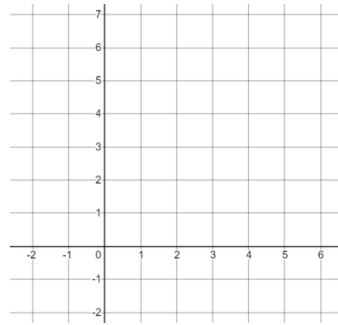
$x$	-2	-1	0	1	2	3
$y$						



**(c)**

Plot the graph of  $y = x^2 - 4x + 2$

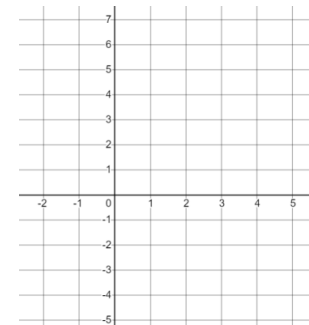
$x$	-1	0	1	2	3	4	5
$y$							



**(e)**

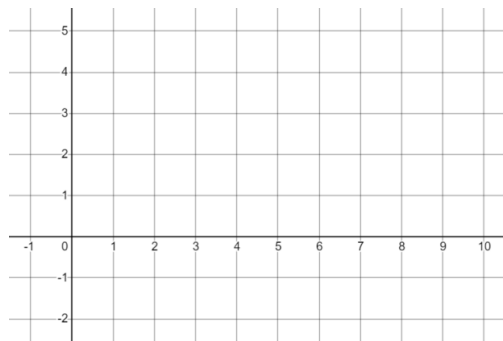
Plot the graph of  $y = x^3 - 4x^2 + 5$

$x$	-1	0	1	2	3	4
$y$						



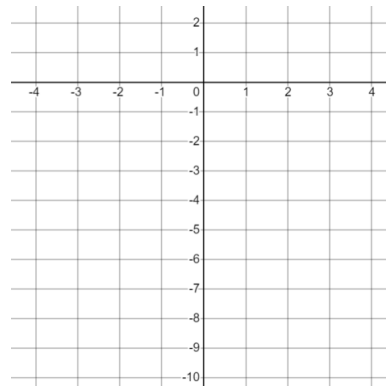
**(b)**

On the grid, plot the graph of  $2x - 3y = 6$  from  $x = 0$  to  $x = 9$



**(d)**

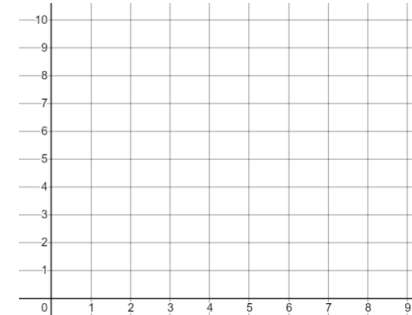
Plot the graph of  $y = 2 + x - x^2$  for  $x = -3$  to  $x = 3$



**(f)**

Plot the graph of  $y = x + \frac{8}{x}$

$x$	1	2	3	4	6	8
$y$						



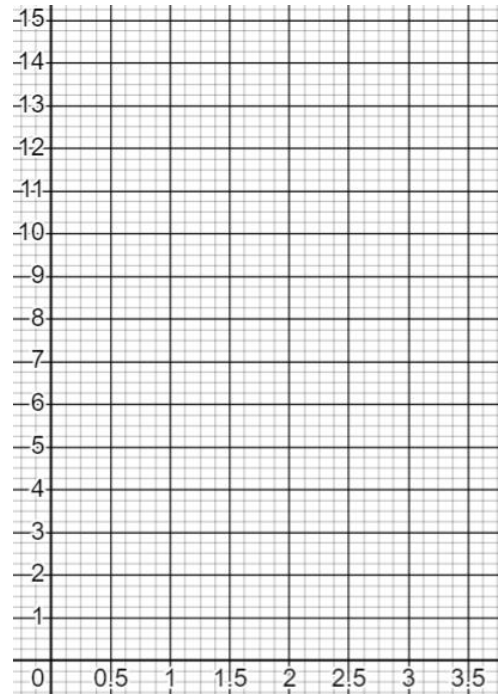
# Fluency Practice

## Plotting Harder Non-Linear Graphs

**(a)**

Plot the graph of  $y = x^2 + \frac{2}{x^2}$   
between  $x = 0.5$  and  $x = 3.5$

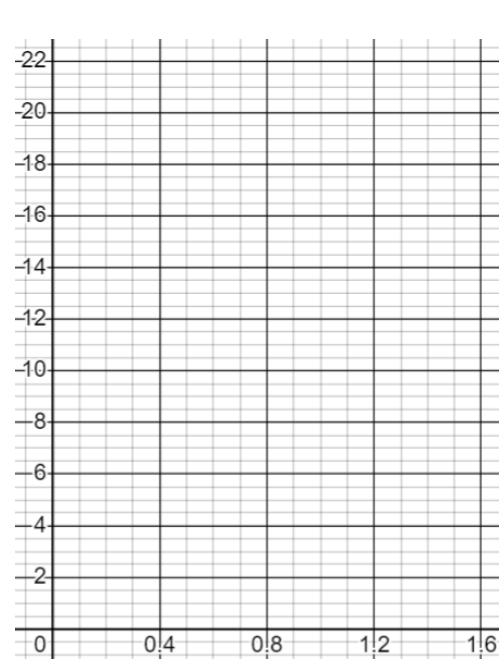
$x$	0.5	1	1.5	2	2.5	3	3.5
$y$							



**(b)**

Plot the graph of  $y = x^3 + 3x + \frac{2}{x}$   
from  $x = 0.1$  to  $x = 1.5$

$x$	0.1	0.2	0.4	0.7	1	1.2	1.5
$y$							



**(c)**

Plot the graph of  $y = x \left( \frac{x}{2} - \frac{1}{x^2} \right)$   
from  $x = -4$  to  $x = -0.5$

$x$	-4	-3	-2	-1	-0.5	-0.25
$y$						

