



Year 8 2023 Mathematics 2024 Unit 7 Booklet

HGS Maths



Tasks



Dr Frost Course



| Name: | | | | | | |
|-------|--|--|--|------|--|--|
| | | | | | | |

Class: _____

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| 1 Prime Factorisation | | | | | | |
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| 1.1 Prime Factors |
|--|
| 3 is a prime factor of 36 (True / False) |
| 9 is a prime factor of 36 (True / False) |
| 1 is a prime factor of 36 (True / False) |
| 2 is a prime factor of 36 (True / False) |
| 7 is a prime factor of 36 (True / False) |
| |
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| 7 is a prime factor of 12 (True / False) |
|---|
| 6 is a prime factor of 12 (True / False) |
| 5 is a prime factor of 12 (True / False) |
| 4 is a prime factor of 12 (True / False) |
| 3 is a prime factor of 12 (True / False) |
| 2 is a prime factor of 12 (True / False) |
| 1 is a prime factor of 12 (True / False) |
| 1 is a prime factor of 27 (True / False) |
| 2 is a prime factor of 27 (True / False) |
| 3 is a prime factor of 27 (True / False) |
| 7 is a prime factor of 27 (True / False) |
| 9 is a prime factor of 27 (True / False) |
| 13 is a prime factor of 27 (True / False) |
| 13 is a prime factor of 26 (True / False) |
| 3 is a prime factor of 26 (True / False) |
| 2 is a prime factor of 26 (True / False) |
| 2 is a prime factor of 25 (True / False) |
| 5 is a prime factor of 25 (True / False) |
| 12.5 is a prime factor of 25 (True / False) |

1.2 Product of Prime Factors

| Product of Prime Factors | Yes / No ? |
|----------------------------|------------|
| 9 × 11 | |
| 19 × 11 | |
| 19×11^2 | |
| $2 \times 19 \times 11^2$ | |
| $2 \times 19 \times 101^2$ | |

| Product of Prime Factors | Yes / No ? |
|---|------------|
| 5 + 7 | |
| 5 × 7 | |
| 4×7 | |
| 3 × 7 | |
| 2 × 7 | |
| 1 × 7 | |
| $1 \times 7 \times 9$ | |
| $2 \times 7 \times 9$ | |
| $2 \times 7 \times 11$ | |
| $2 \times 7 + 11$ | |
| $2 \times 7 \times 11 \times 21$ | |
| $2 \times 7 \times 11 \times 31$ | |
| $1 \times 2 \times 7 \times 11 \times 31$ | |
| $2 \times 7 \times 7 \times 11 \times 31$ | |
| $2 \times 7^2 \times 11 \times 31$ | |
| $2^2 \times 7^2 \times 11 \times 31$ | |
| $2^3 \times 7^2 \times 11 \times 31$ | |
| $2^3 \times 7^2 \times 11^5 \times 31^4$ | |
| $1^3 \times 7^2 \times 11^5 \times 31^4$ | |
| $2^3 \times 7^2 \times 11^5 \times 41^4$ | |

| Worked Example | | | | | | Your Turn | | | | | | | | | | | | | | |
|-----------------------|--|--|--|------|------|---------------|--|-----------------------|--|--|--|--|--|--|--|--|--------------------------|--|--|--|
| Expr prim | | | | orod | duct | t of | | Express 48 prime fact | | | | | | | | | 48 as a product of ctors | | | |
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| Worked Examp | le | Your Turn | | | | | | | |
|---------------------------|----|-----------|----------|---------------------------|--|--|---|--|--|
| Express 40 as a product o | of | | ss 80 as | 80 as a product of actors | | | | | |
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| Worked Example | | | | | | Your Turn | | | | | | | | | | |
|----------------|---------------------|-------|-------|------|------|-----------|-------------------|--|--|--|------------------------------|--|--|--|--|--|
| Expre numb | ss 2 ³ > | < 3 a | ıs ar | n or | dina | ary | Express 32 number | | | | $^2 \times 5$ as an ordinary | | | | | |
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Fill in the Gaps

| Number | Prime Factor Decomposition | Index Form |
|--------|--|---------------------------|
| 6 | | |
| | $2 \times 2 \times 3$ | |
| 48 | | |
| 240 | | |
| | | $2^4 \times 3^2 \times 5$ |
| | $2 \times 2 \times 2 \times 3 \times 3$ | |
| 216 | | |
| | | $2^2 \times 3^2$ |
| | $2 \times 2 \times 3 \times 3 \times 5 \times 5$ | |
| | | $2 \times 3 \times 5$ |
| 420 | | |
| 12 600 | | |



Fill in the Gaps



| Number | Factor Tree | Product of Prime Factors |
|--------|-------------|--------------------------|
| 18 | 18 9 | 2 × 3 × 3 |
| 10 | 3 3 | 2×3^2 |
| 42 | 42 | |
| 42 | | |
| 12 | 12 | |
| 12 | (2) | |
| 0.5 | 27 | |
| 27 | | |
| | 60 | |
| 60 | | |

| Number | Factor Tree | Product of Prime Factors |
|--------|-------------|--------------------------------|
| 20 | 20 10 5 2 | |
| 55 | 55 | |
| 45 | 45 | |
| 36 | 36 | |
| 126 | 126 | |

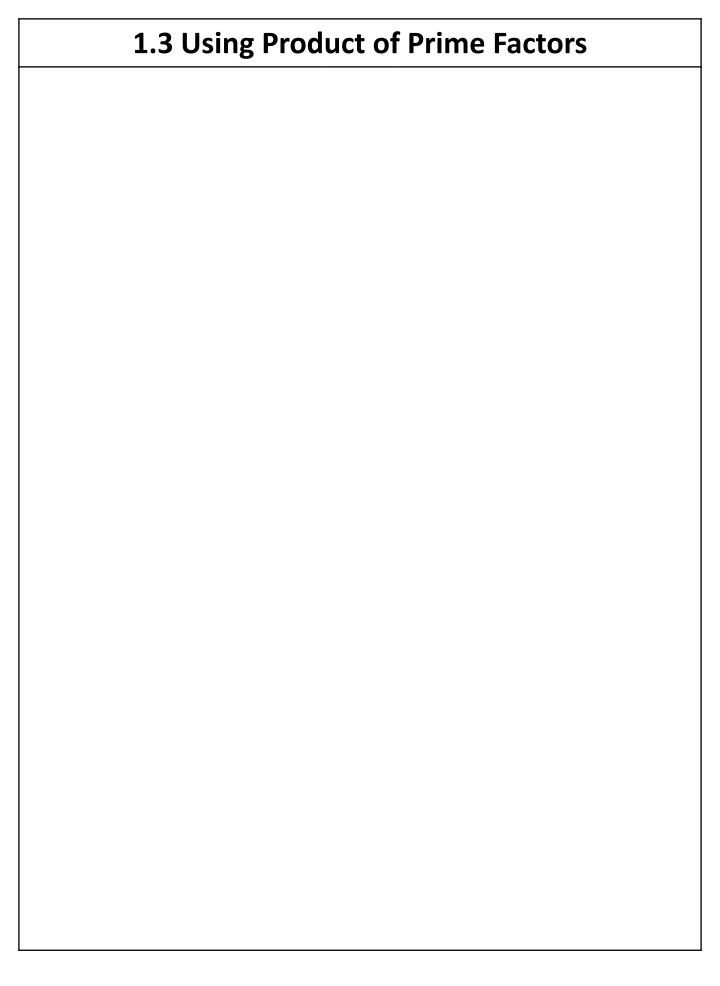


Fill in the Gaps



| Factor Tree | Product of Prime Factors |
|-------------|--------------------------------|
| 135 | 135 |
| | 3 × 3 × 3 × 5 |
| | $3^3 \times 5$ |
| 220 | 220 |
| | |
| | |
| | |
| | $2 \times 2 \times 5 \times 5$ |
| | |
| | |
| 10 | |
| | X3 |

| Factor Tree | Product of Prime Factors |
|-------------|--|
| 330 | 330 |
| | |
| | |
| 525 | 525 |
| | |
| | |
| | |
| 2) 21 | |
| | \times \times \times \times \times \times \times |
| | |
| 9 | |
| | \times \times \times 13 |



| Worked Example | Your Turn | |
|---|---|--|
| $84 = 2^2 \times 3 \times 7$ How is 840 written as its product of prime factors? | $84 = 2^2 \times 3 \times 7$ How is 504 written as its product of prime factors? | |
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| Worked Example | Your Turn | | |
|--|---|--|--|
| $X = 378 \times 12^4$ Write X as a product of its prime factors. | $N = 242 \times 15^2$ Write N as a product of its prime factors. | | |
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| Worked Example | Your Turn |
|--|--|
| $C = 3^a \times 5^b$ | $D = 3^e \times 7^f$ |
| a) 3 <i>C</i> b) 5 <i>C</i> c) 25 <i>C</i> | a) 3 <i>D</i> b) 7 <i>D</i> c) 27 <i>D</i> |
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1.4 Factors from Prime Factors

10 is a factor of
$$2 \times 5 \times 7 \times 11 \times 17$$
 (True / False)

10 is a factor of
$$2 \times 5^3 \times 7 \times 11 \times 17$$
 (True / False)

15 is a factor of
$$2 \times 5^3 \times 7 \times 11 \times 17$$
 (True / False)

25 is a factor of
$$2 \times 5^3 \times 7 \times 11 \times 17$$
 (True / False)

22 is a factor of
$$2 \times 5^3 \times 7 \times 11 \times 17$$
 (True / False)

| Intelligent Prac | ctice |
|--|----------------|
| 2 is a factor of $2 \times 3 \times 7 \times 13$ | (True / False) |
| 3 is a factor of $2 \times 3 \times 7 \times 13$ | (True / False) |
| 5 is a factor of $2 \times 3 \times 7 \times 13$ | (True / False) |
| 7 is a factor of $2 \times 3 \times 7 \times 13$ | (True / False) |
| 4 is a factor of $2 \times 3 \times 7 \times 13$ | (True / False) |
| 6 is a factor of $2 \times 3 \times 7 \times 13$ | (True / False) |
| 14 is a factor of $2 \times 3 \times 7 \times 13$ | (True / False) |
| 21 is a factor of $2 \times 3 \times 7 \times 13$ | (True / False) |
| 15 is a factor of $2 \times 3 \times 7 \times 13$ | (True / False) |
| 15 is a factor of $2 \times 3 \times 5 \times 7 \times 13$ | (True / False) |
| 30 is a factor of $2 \times 3 \times 5 \times 7 \times 13$ | (True / False) |
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Intelligent Practice 9 is a factor of $2 \times 3 \times 5 \times 7 \times 13$ (True / False) 9 is a factor of $2 \times 3^2 \times 5 \times 7 \times 13$ (True / False) 9 is a factor of $2 \times 3^2 \times 5 \times 7 \times 23$ (True / False) 4 is a factor of $2 \times 3^2 \times 5 \times 7 \times 23$ (True / False) 4 is a factor of $2^3 \times 3^2 \times 5 \times 7 \times 23$ (True / False) 8 is a factor of $2^3 \times 3^2 \times 5 \times 7 \times 23$ (True / False) 16 is a factor of $2^3 \times 3^2 \times 5 \times 7 \times 23$ (True / False) 2 is a factor of $2^3 \times 3^2 \times 5 \times 7 \times 23$ (True / False) 28 is a factor of $2^3 \times 3^2 \times 5 \times 7 \times 23$ (True / False) 28 is a factor of $2^2 \times 3^2 \times 5 \times 7 \times 23$ (True / False) 28 is a factor of $2 \times 3^2 \times 5 \times 7 \times 23$ (True / False)

Fluency Practice

| Number | Prime Factor Decomposition | Factor | Yes/No |
|--------|------------------------------------|------------|--------|
| 2520 | $2^3 \times 3^2 \times 5 \times 7$ | 15 = 3 × 5 | Yes |
| 2520 | | 8 | |
| 2520 | | 25 | |
| 2520 | | 45 | |
| 1320 | | 22 | |
| 1320 | | 45 | |
| 1320 | | 88 | |
| 20250 | | 12 | |
| 20250 | | 27 | |
| 20250 | | 15 | |
| 20250 | | 75 | |
| 15120 | | 16 | |
| 15120 | | 21 | |
| 15120 | | 70 | |
| 15120 | | 18 | |

1.5 Types of Numbers from Prime Factors

- Square numbers have even powers in their prime factorisation.
- Cube numbers have powers which are multiples of 3.

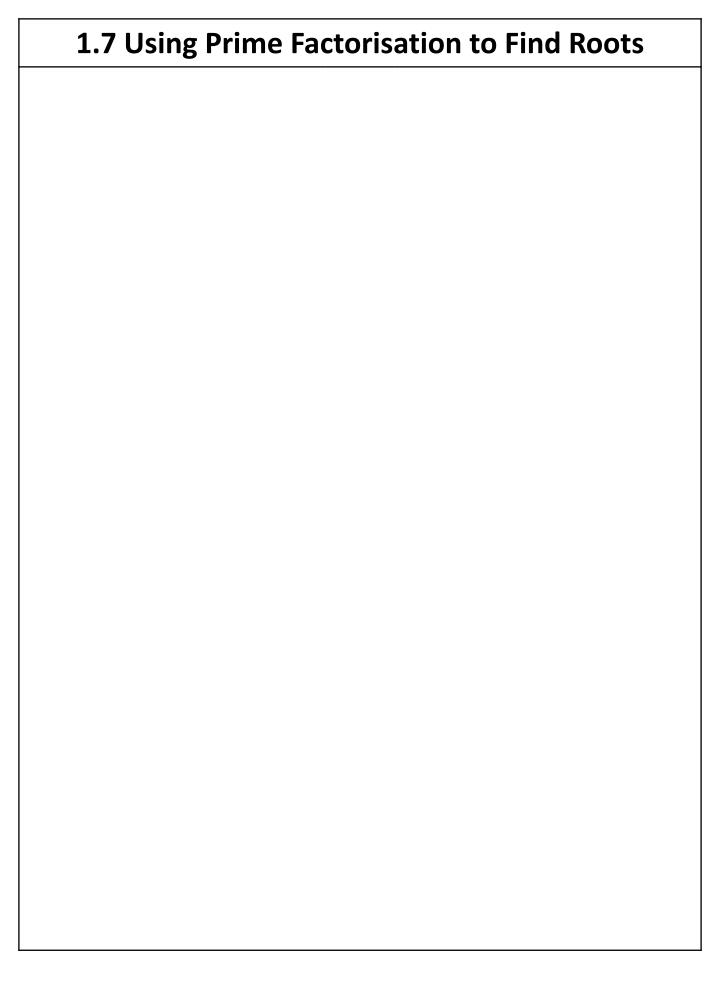
| Product of Prime Factors | Square Number | Cube Number | Neither |
|----------------------------------|---------------|-------------|---------|
| $5^2 \times 11$ | | | |
| $5^2 \times 11^8$ | | | |
| $5^6 \times 11^8$ | | | |
| $5^6 \times 11^9$ | | | |
| $5^6 \times 11^9 \times 17^{13}$ | | | |

| Product of Prime Factors | Square Number | Cube Number | Neither |
|-----------------------------|---------------|-------------|---------|
| 2 × 3 | | | |
| 3 × 3 | | | |
| 3 ² | | | |
| 3^3 | | | |
| $3^3 \times 7$ | | | |
| $3^3 \times 7^2$ | | | |
| $3^3 \times 7^3$ | | | |
| $3^2 \times 7^2$ | | | |
| $5^2 \times 7^2$ | | | |
| $2 \times 5^2 \times 7^2$ | | | |
| $2^2 \times 5^2 \times 7^2$ | | | |
| $2^3 \times 5^2 \times 7^2$ | | | |
| $2^3 \times 5^3 \times 7^3$ | | | |

| Product of Prime Factors | Square Number | Cube Number | Neither |
|---|---------------|-------------|---------|
| $2^4 \times 5^4 \times 7^4$ | | | |
| $2^5 \times 5^5 \times 7^5$ | | | |
| $2^6 \times 5^6 \times 7^6$ | | | |
| $2^7 \times 5^7 \times 7^7$ | | | |
| $2^8 \times 5^8 \times 7^8$ | | | |
| $2^9 \times 5^9 \times 7^9$ | | | |
| $2^9 \times 5^9 \times 7^6$ | | | |
| $2^2 \times 5^9 \times 7^6$ | | | |
| $2^3 \times 5^9 \times 7^6$ | | | |
| $2^6 \times 5^{18} \times 7^{12}$ | | | |
| $2^6 \times 5^{18} \times 7^{12} \times 11$ | | | |
| $2^6 \times 5^{18} \times 7^{12} \times 11^2$ | | | |
| $2^6 \times 5^{18} \times 7^{12} \times 11^3$ | | | |

| 1.6 Using Prime Factorisation to Simplify Fractions | |
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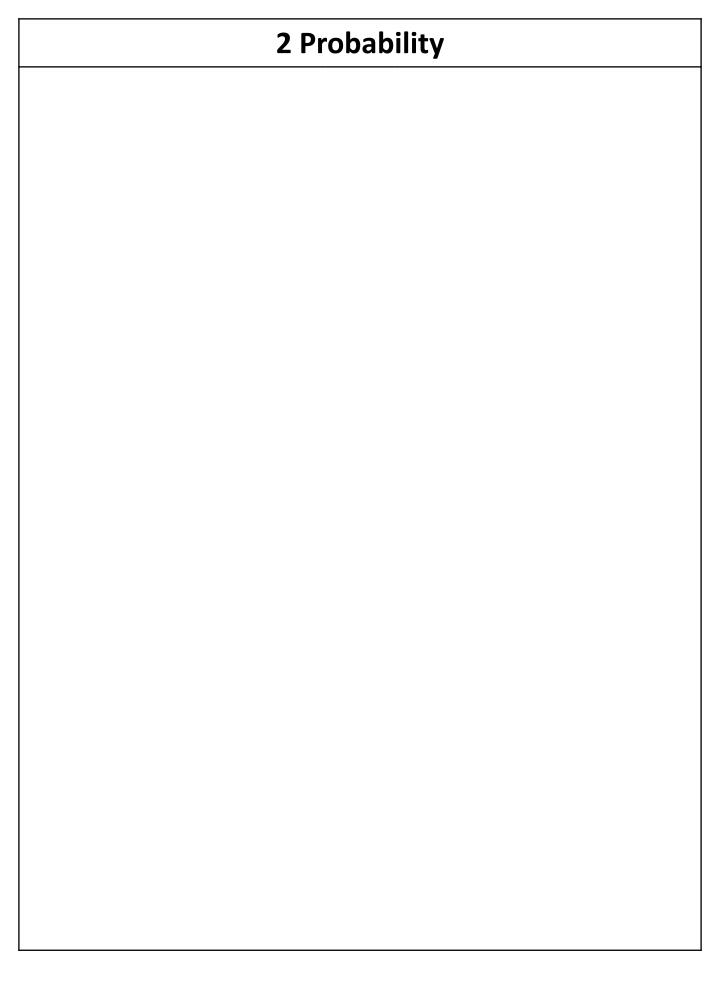
| Worked Example | Your Turn |
|-----------------------------|-----------------------------|
| Simplify $\frac{693}{1925}$ | Simplify $\frac{693}{1155}$ |
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| Worked Exampl | e Your Turn |
|---|--|
| a) Find $\sqrt{784}$ b) Find $\sqrt[3]{216}$ | a) Find $\sqrt{324}$ b) Find $\sqrt[3]{512}$ |
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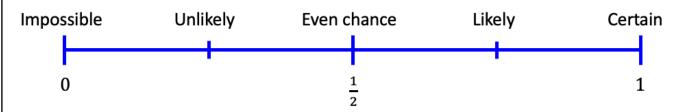
| 1.8 Number of Factors To get the number of factors of a number in prime factorised form, add one to each power and times the powers together. | | | | | | | |
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| Worked Example | | | | | | Your Turn | | | | | | | | | | | |
|---|--|--|--|--|-----------------------------------|---|--|--|--|--|--|--|------|--|--|--|--|
| a) How many factors does 36 have?b) How many factors does 37 have? | | | | | b) | a) How many factors does 72 have?b) How many factors does 73 have? | | | | | | | 3 73 | | | | |
| c) How many factors does 38 have? | | | | | c) How many factors does 74 have? | | | | | | | | | | | | |
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2.1 Probability Scale

- Probability is a numerical measure of how likely or unlikely an event is to occur.
- Probabilities are usually written as fractions, but can be written in any form equivalent to that fraction, e.g., $\frac{3}{4} = 0.75 = 75\%$
- Probabilities can be anywhere between 0 (impossible) and 1 (certain):



Could it be a Probability?

0.35674

Yes / No

1.35674

Yes / No

1

Yes / No

 $\frac{1}{3}$

Yes / No

 $-\frac{1}{3}$

Yes / No

| Intelligent Practice |
|-----------------------------|
|-----------------------------|

0.3

Yes / No

-0.3

Yes / No

1.3

Yes / No

0.000003

Yes / No

0.43045783

Yes / No

1.43045783

Yes / No

-0.43045783

Yes / No

 $0.\dot{4}$

Yes / No

0

Yes / No

1

Yes / No

2

Yes / No

-1

Yes / No

 $\frac{2}{3}$

Yes / No

 $1\frac{2}{3}$

Yes / No

 $-\frac{2}{3}$

Yes / No

 $\frac{3}{2}$

Yes / No

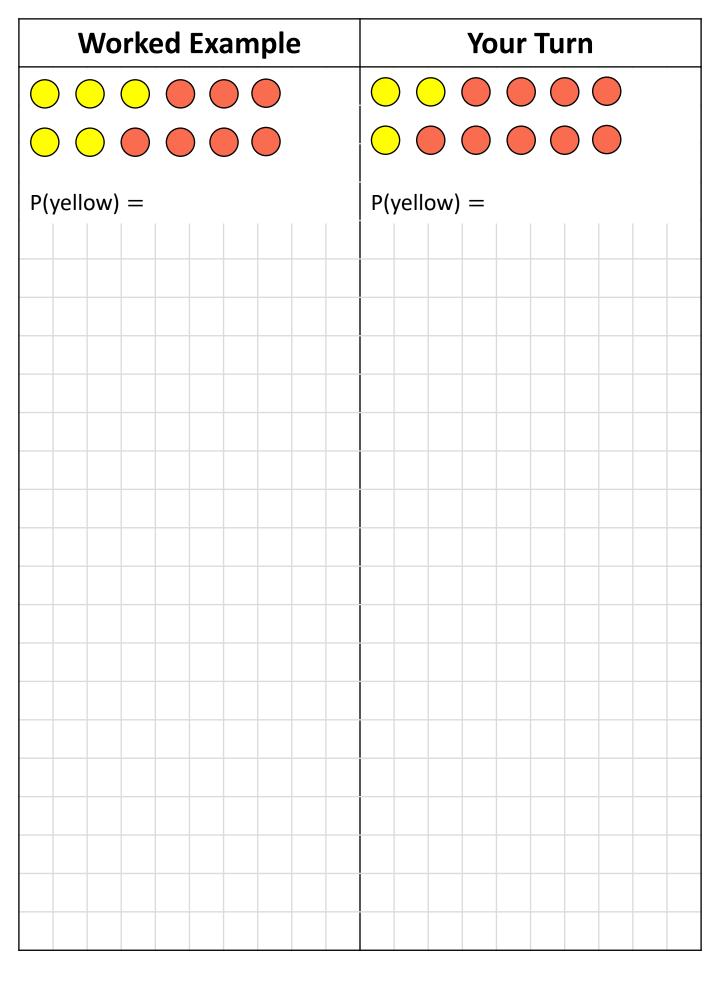
 $\frac{43}{51}$

Yes / No

| Place a probability of $\frac{6}{8}$ on a line, and state how likely it is. | | | | | | | |
|---|--|--|--|--|--|--|--|
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| Worked Example | Your Turn | | | | | | |
|---|---|--|--|--|--|--|--|
| Describe using impossible, unlikely, even chance, likely or certain the probability that: a) You will walk to Mars. b) The day after Monday is Tuesday. c) You roll a three on a fair die. d) You flip a tails on a fair coin. | Describe using impossible, unlikely, even chance, likely or certain the probability that: a) You roll an even number on a fair die. b) The day after Monday is Wednesday. c) You roll a number between 1 and 6 on a fair die. | | | | | | |
| | d) You will go to space in your life. | | | | | | |
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| 2.2 Probability of Single Events | | | | | | |
|--|--|--|--|--|--|--|
| The probability of an event occurring is defined as: Number of desired outcomes | | | | | | |
| Probability = $\frac{\text{Number of desired outcomes}}{\text{Number of possible outcomes}}$ | | | | | | |
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| Worked Example | | | | | | | | Yo | ur | Tu | rn | | | | | | |
|---|---|--|--|--|--|--|------------------------------|----|--|-----------------------------|--------------------------|-----------------------------|-------------------------------|----|--|--|--|
| A bag of sweets contains only 4 red sweets, 2 yellow sweets and 4 green sweets. a) What is the probability of choosing a red sweet? b) What is the probability of choosing a red or yellow sweet? | | | | | | re | d sv gree W ch W | | ts, 4 wee is t sing is t sing | lye ets. he p a re | llow oroked s orok | v sw pabi wee pabi | veet ility et? ility | of | | | |
| c) | c) What is the probability of choosing a mint? | | | | | c) What is the probability of choosing a mint? | | | | | | | | | | | |
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2.3 Mutually Exclusive Events

Mutually exclusive means "cannot happen at the same time".

Examples

- Turning left or turning right (you cannot turn left and right at the same time).
- Going to Liverpool at 9am tomorrow or going to Manchester at 9am tomorrow (you cannot be in two places at once).

Non-Examples

- Turning left and scratching your head can happen at the same time.
- Kings and hearts, because you can have a king of hearts.

| 2.4 Exhaustive Events |
|---|
| The probabilities of all possible outcomes add up to 1. |
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| Worked Example | Your Turn | | | | |
|--|--|--|--|--|--|
| Castle FC play football matches every Saturday. | Castle FC play football matches every Saturday. | | | | |
| The table shows the probability that Castle FC will win or lose. | The table shows the probability that Castle FC will win or lose. | | | | |
| a) Work out the probability that Castle FC will lose | a) Work out the probability that Castle FC will lose | | | | |
| $\begin{array}{ c c }\hline \textbf{Win} & \textbf{Lose} \\\hline \hline \frac{3}{4} & \\\hline \end{array}$ | Win Lose 6/8 8 | | | | |
| b) Work out the probability that Castle FC will lose | b) Work out the probability that Castle FC will win | | | | |
| Win Lose | Win Lose | | | | |
| 0.75 | 0.75 | | | | |
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| Worked Example | Your Turn | | | |
|--|---|--|--|--|
| There are green, red and blue counters in a bag. | It is either raining or not raining. | | | |
| The chance of picking a green counter is 0.1. The chance of picking a red | The chance that it rains tomorrow is 0.55. What is the chance that it does not rain? | | | |
| what is the chance of picking a blue counter? | | | | |
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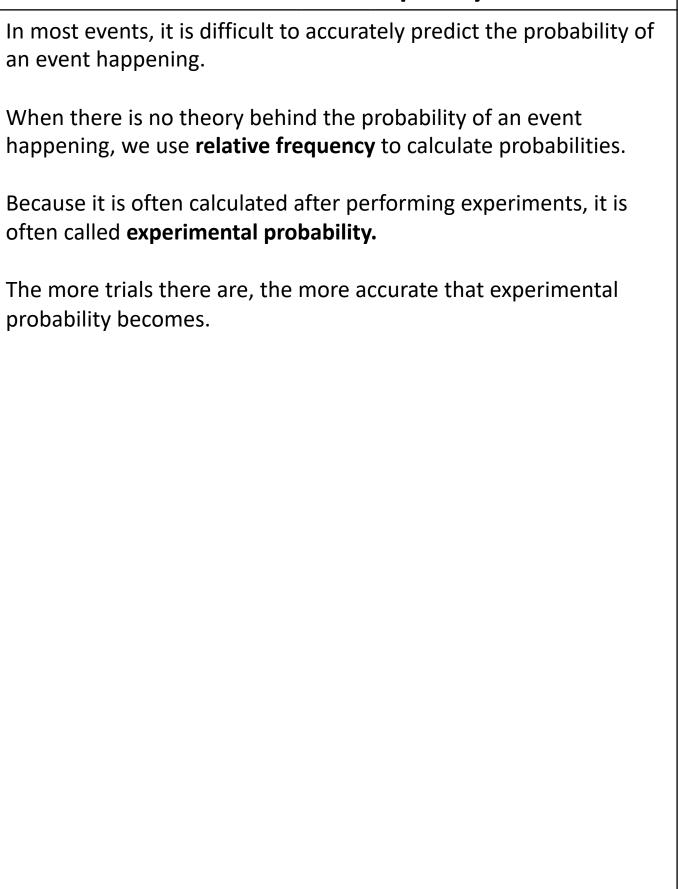
Fluency Practice Green Green Green Green These tables show the probabilities on a spinner. In each case, fill in the blank(s). 0.54 * For this question, blue and orange 0.2 വ വ have **the same** probability. Orange Orange Orange Orange 0.27 One question is impossible to answer. Which one and why? 0.2 Blue Blue 0.15 Blue Blue $\frac{1}{10}$ Red 0.32 Red Red Red 0.3 0.3 7 | 1 (S 4 ဖ ω Green Green Green Green $\frac{3}{10}$ $\frac{3}{10}$ Orange Orange Orange Orange 0.2 0.1 Blue Blue Blue Blue 0.03 0.1 $\frac{1}{10}$ Red Red Red Red 0.3 0.3 $\frac{3}{10}$ 7 | 7 က 2

| Worked | Example | Your Turn | | | | |
|---|---|--|--|--|--|--|
| The relative free teacher throwin bin is 0.5. A teacher 100 times. It throws will be so | g a pen in the ther throws a How many | The relative frequency of a teacher throwing a pen in the bin is 0.5. A teacher throws a pen 1000 times. How many throws will be successful? | | | | |
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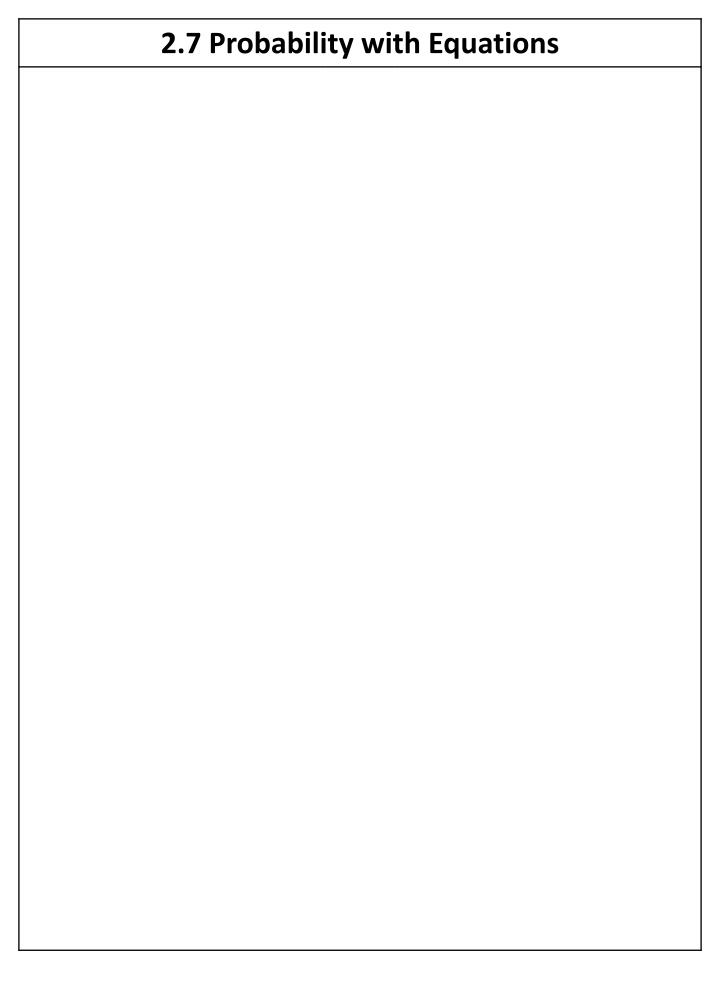
| Worked Example | Your Turn | | | |
|---|---|--|--|--|
| If I roll a fair dice 12 times, how many times would you expect it to land on the number 1? | If I roll a fair dice 60 times, how many times would you expect it to land on the number 1? | | | |
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| Worked Example | Your Turn | | |
|--|--|--|--|
| Keith designs a game. It costs £1.60 to play the game. | Bob designs a game. It costs $50p$ to play the game. | | |
| The probability of winning the game is $\frac{2}{5}$ | The probability of winning the game is $\frac{1}{4}$ | | |
| The prize for each win is £3 | The prize for each win is £1.50 | | |
| 80 people play the game. | 100 people play the game. | | |
| Work out an estimate of the profit that Keith should expect to make. | Work out an estimate of the profit that Bob should expect to make. | | |
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2.6 Relative Frequency



| Worked Example | Your Turn | | | |
|---|---|--|--|--|
| A coin is flipped 30 times. The results are: | A coin is flipped 20 times. The results are: | | | |
| нтнннннтттннтт | тнттттннн | | | |
| тттнннттннтнн | ННТНТНННН | | | |
| a) What are the relative frequencies for heads and tails? | a) What are the relative frequencies for heads and tails? | | | |
| b) The coin is flipped 300 more times. Estimate how many times the coin will land on tails. | b) The coin is flipped 100 more times. Estimate how many times the coin will land on tails. | | | |
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Worked Example

Different coloured counters are placed in a bag. The probabilities of each counter is given.

| Colour | Red | Blue | Green | Purple | |
|-------------|------|------------|----------|--------|--|
| Probability | 0.15 | 6 <i>x</i> | 5x + 0.1 | 0.2 | |

- a) Find the probability of selecting a red counter.
- b) You are told there are 24 red counters in the bag. Find how many blue, green and purple counters there are?

Your Turn

Different coloured counters are placed in a bag. The probabilities of each counter is given.

| Colour | Red | Blue | Green | Purple |
|-------------|----------|------|-----------|-----------|
| Probability | 5x - 0.1 | 0.1 | 2x + 0.04 | 3x + 0.16 |

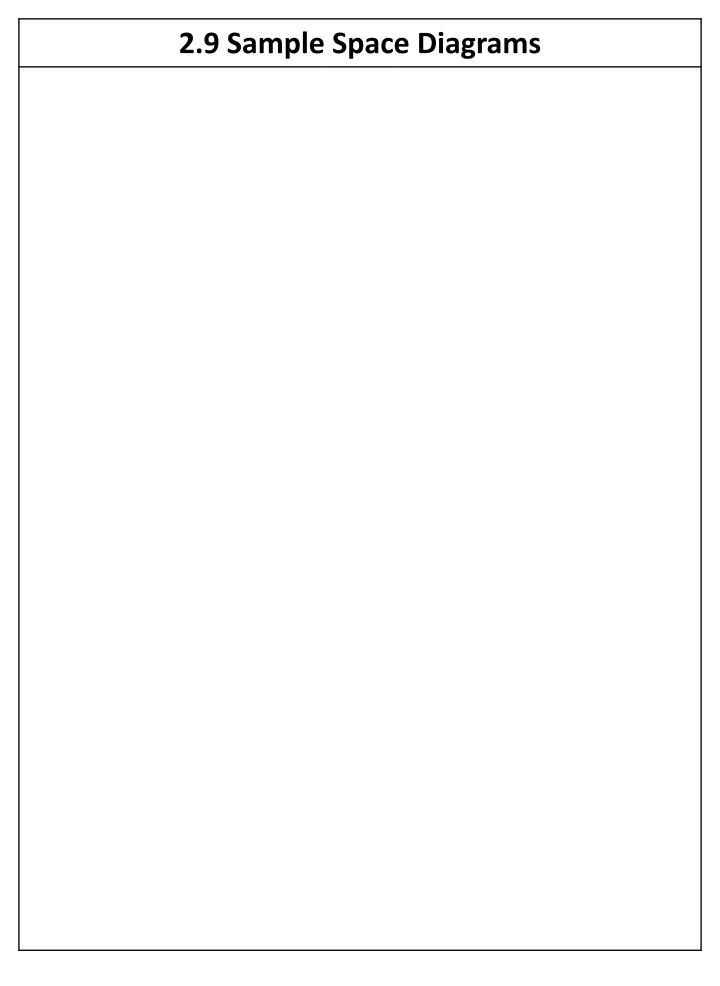
- a) Find the probability of selecting a red counter.
- b) You are told there are 9 blue counters in the bag. Find how many red, green and purple counters there are?

| 2.8 Listing Outcomes |
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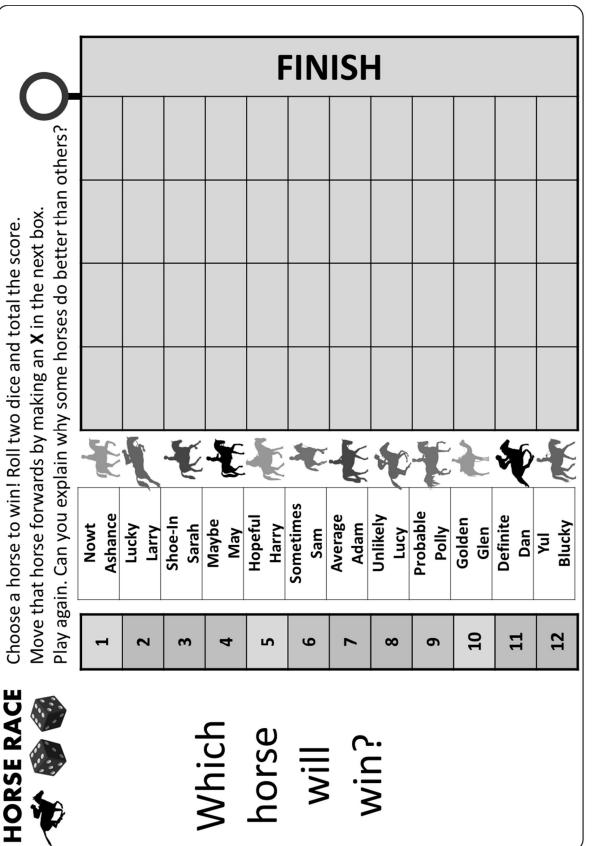
| Worked Example | | | | | | | | | | | | Yo | ur | Tu | rn | | | | |
|----------------|---|--|--|--|--|--|--|--|--|--|--|----|----|----|----|--|--|--|--|
| | ist all the ways of arranging the etters in the word: | | | | | | | | | | List all the ways of arranging the letters in the word: DOG | | | | | | | | |
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| | Work | ced E | | | | Yo | ur | Tu | rn | | | | | | | | | |
|-------|----------------|-------|--|-----|---|----|----|----|----|--|--|--|--|--|--|--|--|--|
| sided | a coin die. Li | | | ix- | I flip a coin and then roll a 4- sided die. List the possible outcomes. | | | | | | | | | | | | | |
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| Worked Example | Your Turn | | | | | | | | |
|--|---|--|--|--|--|--|--|--|--|
| The first five positive integers are 1, 2, 3, 4, 5. I choose two numbers from this list. Write down all possible combinations of two numbers I can choose. | The four square numbers are 1, 4, 9, 16. I choose two numbers from this list. Write down all possible combinations of two numbers I can choose. | | | | | | | | |
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Horse Race





Move that horse forwards by making an X in the next box. Choose a horse to win! Roll two dice and total the score.

Dlay again Can you overlain why come borcer do bottor than others?

∭ ∭

win?

horse

Horse Race

HORSE RACE





- 1) Who won the race(s)?
- 2) Who did you expect to win?
- 3) Do some horses have a higher chance of winning? Why?
- 4) How many ways can you score a 2?
- 5) How many ways can you score a 12?
- 6) How many ways can you score a 4?
- 7) How many ways can you score a **10**?
- 8) How many ways can you score a **7**?

We can make this easier by using a **Sample Space Diagram**.

Score on the 2nd Dice

| | + | 1 | 2 | 3 | 4 | 5 | 6 |
|-----------------------|---|---|---|---|----|---|---|
| ce | 1 | 2 | | | | | |
| Score on the 1st Dice | 2 | | | 5 | | | |
| the 1 | 3 | | | | | | 9 |
| e on | 4 | | | | | | |
| Scol | 5 | | | | | | |
| | 6 | | | | 10 | | |

Fill the table with the totals from 2 dice.

- a) How many ways to score a 6?
- b) How many ways to score a 5?
 - c) How many outcomes are there in total?

Remember, $Probability = \frac{number\ of\ ways\ outcome\ can\ happen}{total\ number\ of\ possible\ outcomes}$

Use this to find:

d) Probability(12) =

e) Probability(8) =

f) P(4) =

g) P(**9**) =

h) P(**7**) =

i) P(**1**) =

If you ran the horse race again, which horse would you pick?

| Worked | Example | Your Turn |
|----------|----------|--|
| <u>-</u> | me time. | Elisa throws a spinner with faces labelled R, G, B and Y and a foursided dice numbered 2, 4, 6 and 8 at the same time. Draw a sample space diagram. |
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| Worked | Example | ` | our Turn | |
|--|---------------------------|--|--|---|
| Noel throws a for and a four-sided same time and a scores. Draw a sample specific sample specific same throws a sample specific sample sample specific sample | dice at the dds up the | dice number a four-side time and a | rows a four-sided ered 2, 4, 6 and 8 and dice at the same dds up the scores. | d |
| | | | The characters of the second | |
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| Worked Exampl | е | Your Turn | | | | | | | |
|--|------------------------|---|--|--|--|--|--|--|--|
| Carolina throws a four-side dice numbered 1, 3, 5 and a four-sided dice numbere 2, -3 and -4 at the same tir and multiplies the scores. Draw a sample space diagr | 7 and d -1, - ne | Carolina throws a six-sided dice and a four-sided dice numbered -1, -2, -3 and -4 at the same time and multiplies the scores. Draw a sample space diagram. | | | | | | | |
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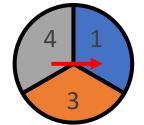
| | Worked Example | | | | | | | | | | | | Yo | ur | Tu | rn | | | |
|----------------------------|--|--|--|--|--|--|--|--|--|---|--|--|----|----|----|----|--|--|---|
| nu fo ar th sc | Paul throws a four-sided dice numbered 2, 4, 6 and 8 and a four-sided dice numbered 1, 3, 5 and 7 at the same time and find the difference between the scores. Draw a sample space diagram. | | | | | | | | | Kayleigh throws a four-sided dice and a six-sided dice at the same time and find the difference between the scores. Draw a sample space diagram. | | | | | | | | | • |
| Di | raw a sample space diagram. | | | | | | | | | | | | | | | | | | |
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Worked Example

I spin these two spinners then add the numbers together to get a score.

Work out the probability that I get a score of 4.





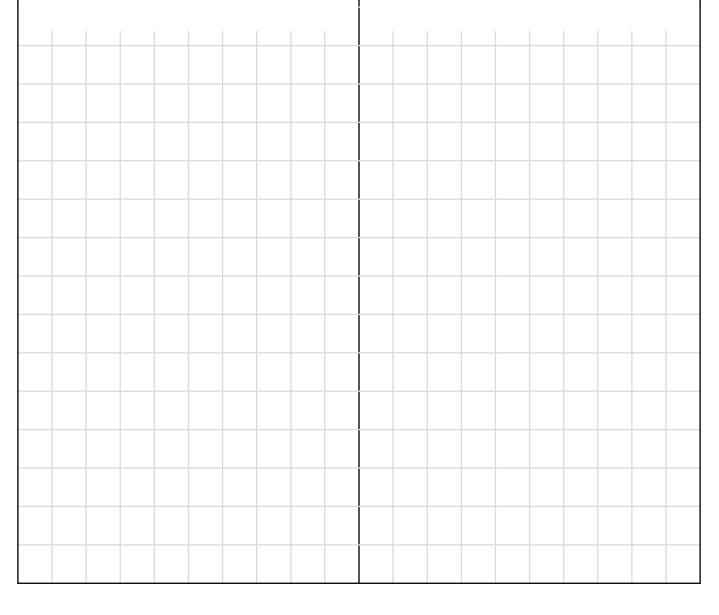
Your Turn

I spin these two spinners then add the numbers together to get a score.

Work out the probability that I get a score of 4.





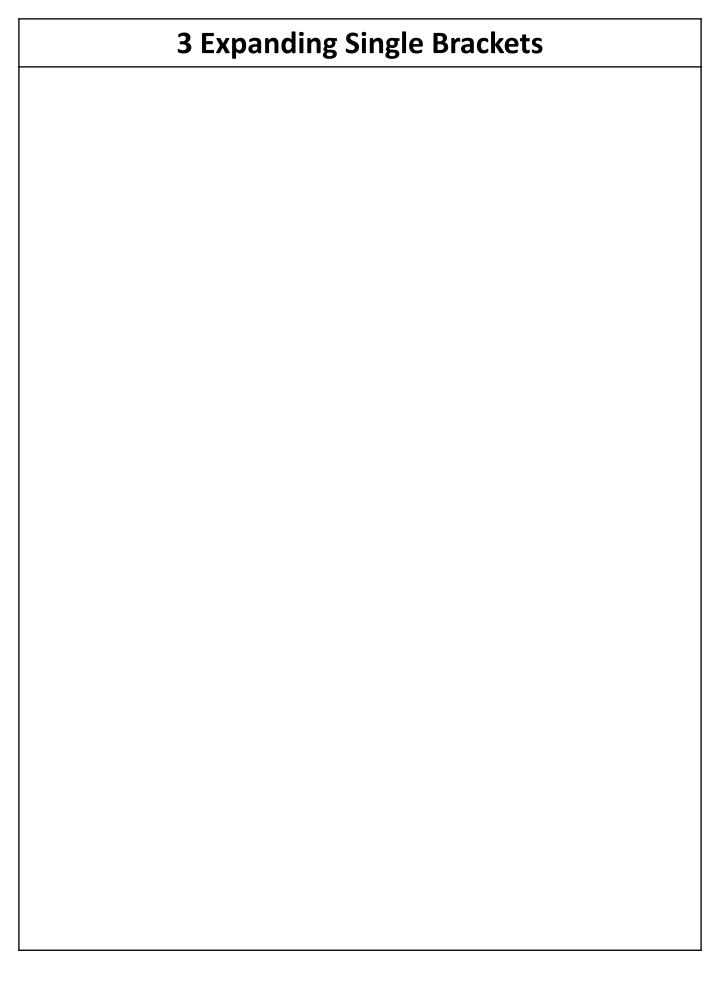




Fill in the Gaps



| Spa | ce | | | | Probability Questions | | | | |
|--------|---------------------|---|---|---|---|--|--|--|--|
| 4 | 1 | 2 | 3 | 4 | Find the probability that the total score is 7. | | | | |
| 2 | 3 | 4 | 5 | 6 | Find the probability that the total score is greater than 4. | | | | |
| 3 | 5 | 5 6 | 6 7 | 8 | Find the probability that the total score is a multiple of 3. | | | | |
| 0 | 2 | 3 | 4 | 5 | Find the probability that the total score is 8. | | | | |
| 3 | 4 | | | | Find the probability that the total score is less than 7. | | | | |
| 5 | | | | | Find the probability that the total score is a multiple of 4. | | | | |
| 4 | 1 | 2 | 3 | 4 | Find the probability that the total score is even. | | | | |
| 2 | 1 | | | 8 | Find the probability that the total score is greater than 6. | | | | |
| 3 | | 6 | | | Find the probability that the total score is prime. | | | | |
| 0 | 2 | 3 | 5 | 7 | Find the probability that the difference is zero. | | | | |
| 3 | U | | 2 | | Find the probability that the difference is odd. | | | | |
| 7 | 5 | | | | Find the probability that the difference is two or more. | | | | |
| | 1 | 2 | 3 | 4 | Find the probability that the total score is 10. | | | | |
| 3 5 | | | | | $\frac{5}{16}$ | | | | |
| 7 | | | | | $\frac{3}{8}$ | | | | |
| | 1 2 3 4 5 7 7 3 5 7 | 1 2 3 3 4 4 5 2 2 4 3 3 4 4 1 1 1 2 2 3 3 4 4 1 1 1 2 1 3 5 5 7 5 1 1 3 5 7 5 | 1 2 1 2 3 2 3 4 3 4 5 4 5 6 2 3 2 4 3 3 4 5 4 5 6 1 2 1 1 2 1 1 1 2 1 3 6 4 1 2 3 2 0 3 6 4 1 1 2 3 7 5 | 1 2 3 1 2 3 4 2 3 4 5 3 4 5 6 4 5 6 7 2 3 4 2 4 3 4 2 4 3 4 5 6 4 5 6 7 1 2 3 1 1 | 1 2 3 4 1 2 3 4 5 2 3 4 5 6 3 4 5 6 7 8 2 3 4 5 2 4 4 4 4 1 2 4 4 1 1 2 8 3 4 1 1 2 8 3 6 4 <td< td=""></td<> | | | | |

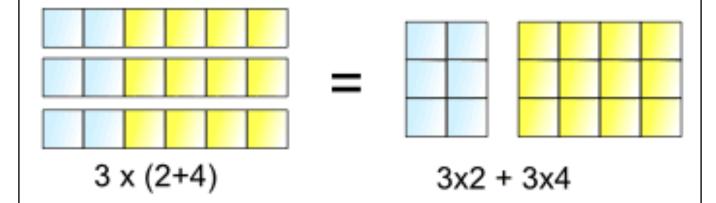


3.1 Distributive Law

The **distributive law** says that multiplying a number by a group of numbers added together is the same as doing each multiplication separately.

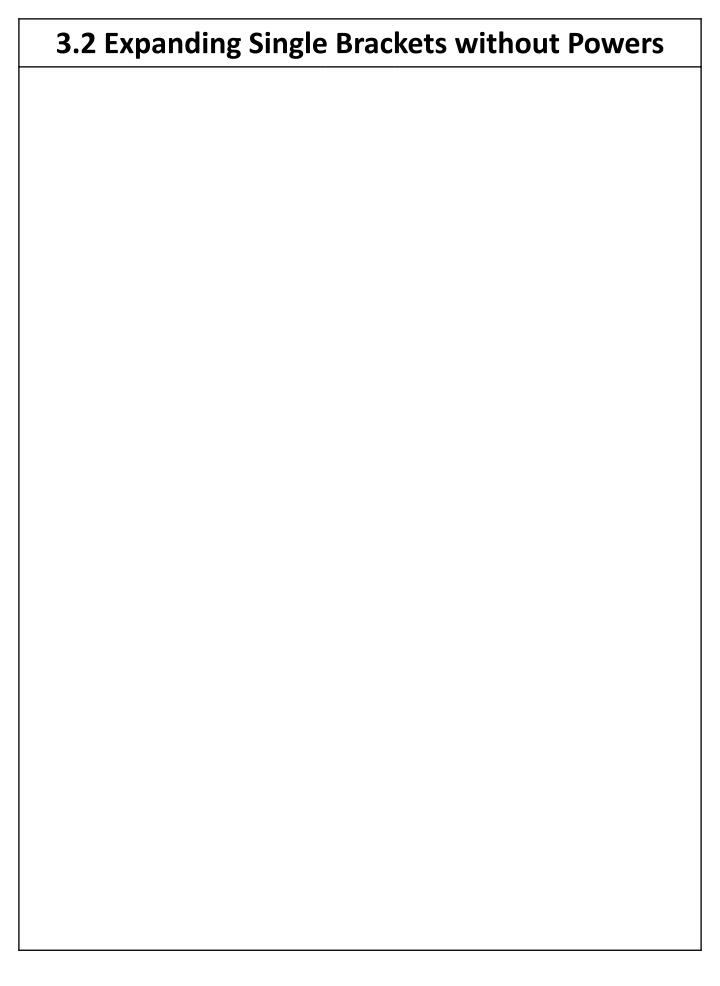
For example: $3 \times (2 + 4) = 3 \times 2 + 3 \times 4$

So the "3" can be "distributed" across the "2+4" into 3 times 2 and 3 times 4.

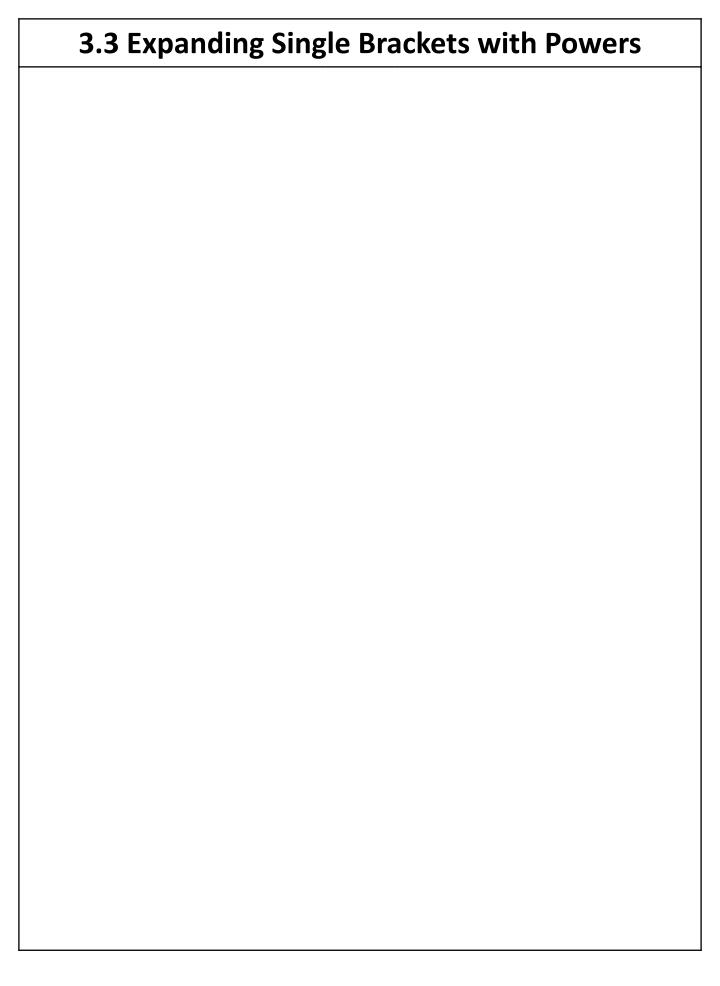


Frayer Model – Distributive Law **Definition Characteristics Examples Non-Examples**

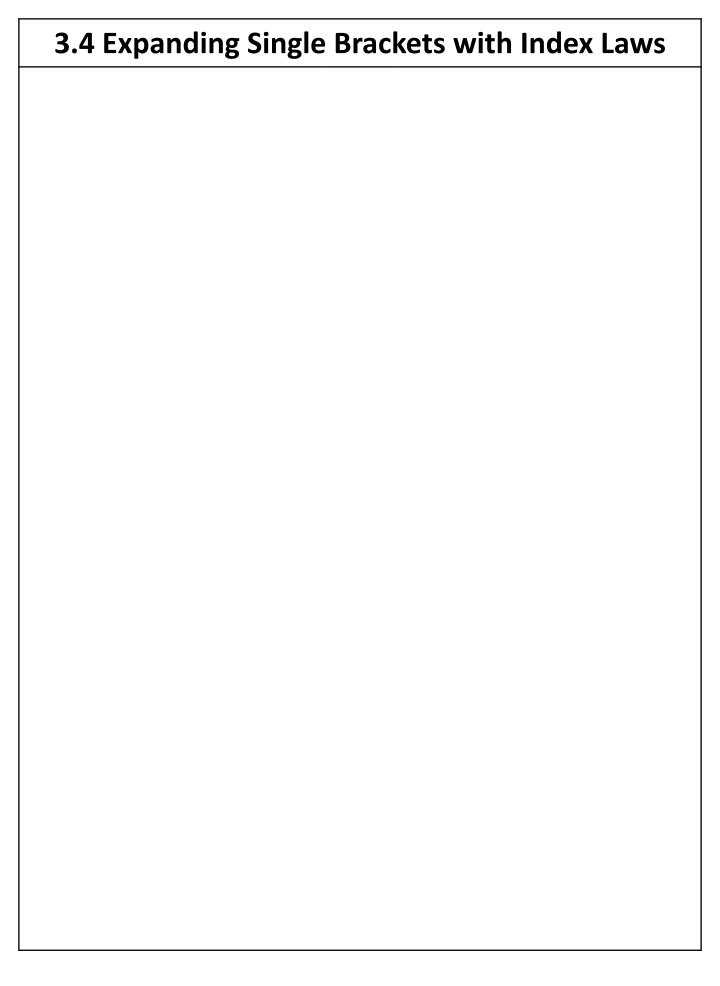
| | Wo | rked | Exam | ple | | Your Turn | | | | | | | | | | |
|------|------------------|------|------|-------|----|---|--|--|--|--|--|--|--|--|--|--|
| cald | culate: 7 × (| | | perty | to | Use the distributive property to calculate: a) $3 \times (80 + 7)$ b) $(30 + 8) \times 7$ | | | | | | | | | | |
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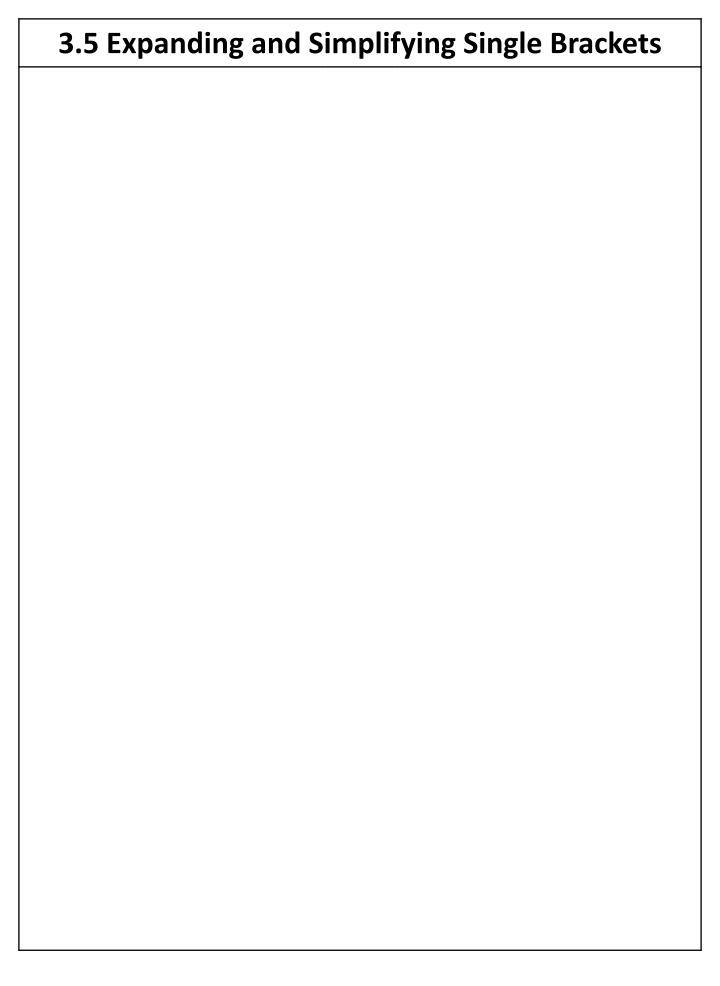
Worked Example Your Turn Expand: Expand: a) 2(x-3)a) 2(3-x)b) -2(x-3)b) -2(3-x)



| Worked Examp | Your Turn | | | | | | | | | | | |
|--|--|--|--|--|--|--|--|--|--|--|--|--|
| Expand: a) $2x(x-3)$ b) $-2x(x-3)$ | Expand: a) $2x(3-x)$ b) $-2x(3-x)$ | | | | | | | | | | | |
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| | Work | ed Ex | ampl | е | Your Turn | | | | | | | | | |
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| a) | and and $a^3bc(4a^5b^2)$ | $10b^2c$ | $^{2} + 9a$ | a^2) b^2) | a) a | band and simplify: $a^3b^5(3a^3b + 7ab^4c)$ $7x^5y^4(6x^2y + 5x^4y)$ | | | | | | | | |
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| | Wo | Your Turn | | | | | | | | | | | | |
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| Expa a) b) | Expand and simplify: a) $-5 + 2(4y - 1)$ b) $6z + 3 + 5(7z + 2)$ | | | | | | | | | | | | | |
| | | S) | | | | | | | | | | | | |
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| Worked Example | | | | | | | | | | Your Turn Expand and simplify: a) $2(x-1) + 5(x-4)$ b) $2(x-1) - 5(x-4)$ | | | | | | | | | | | |
|----------------|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|
| a) | Expand and simplify: a) $2(x-1) + 3(x-4)$ b) $2(x-1) - 3(x-4)$ | | | | | | | | | | | | | | | | | | | | |
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| Worked Example | | | | | | | | | | Your Turn | | | | | | | | | | | |
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| a) | Expand and simplify: a) $2x(x-1) - 3x(x-4)$ b) $2x(x-1) - 3(x-4)$ | | | | | | | | | Expand and simplify: a) $2x(x-1) - 5x(x-4)$ b) $2x(x-1) - 5(x-4)$ | | | | | | | | | | | |
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