



**Year 9
Mathematics
CATCH UP**



Name: _____

Class: _____

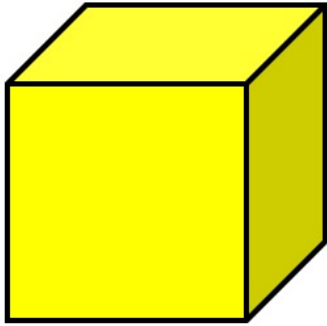
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Please see catch up course on drfrostmaths.com

1 Properties of 3D Shapes

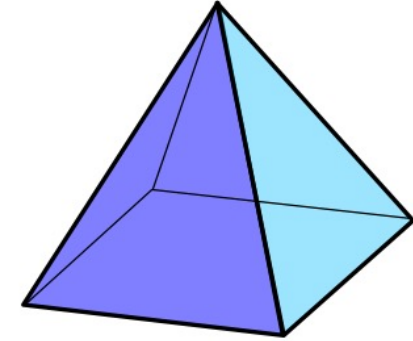
Cube



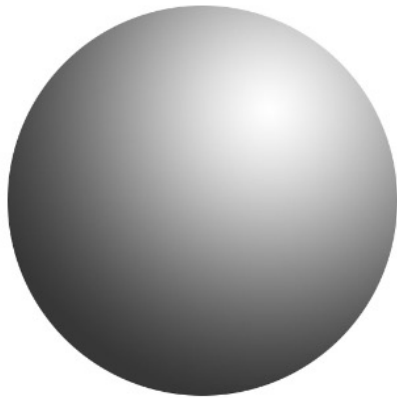
Cuboid



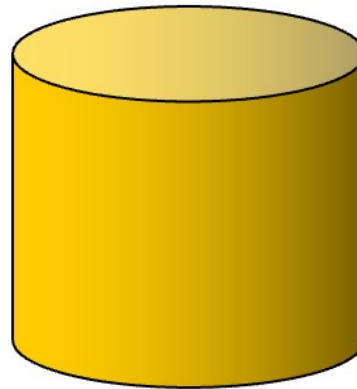
Square-based pyramid



Sphere



Cylinder



Cone



Edges, Faces and Vertices

Faces

A face is a flat or curved surface on a 3D shape.

Edges

An edge is where two faces meet.

Vertices

A vertex is a corner where edges meet. The plural is vertices.

Worked Example

For the cuboid, write down the:



Number of faces (F)

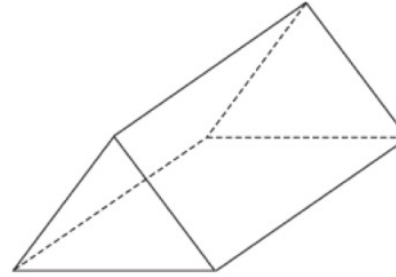
The number of edges (E)

The number of vertices (V)

Calculate $V - E + F$

Your Turn

For the triangular prism, write down the:



Number of faces (F)

The number of edges (E)

The number of vertices (V)

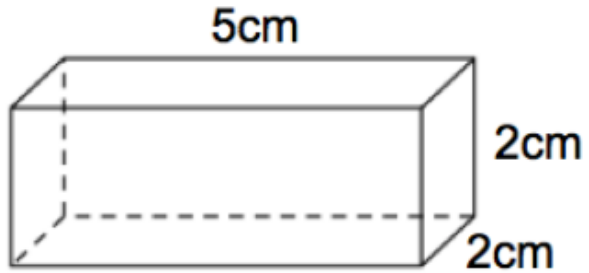
Calculate $V - E + F$

Nets

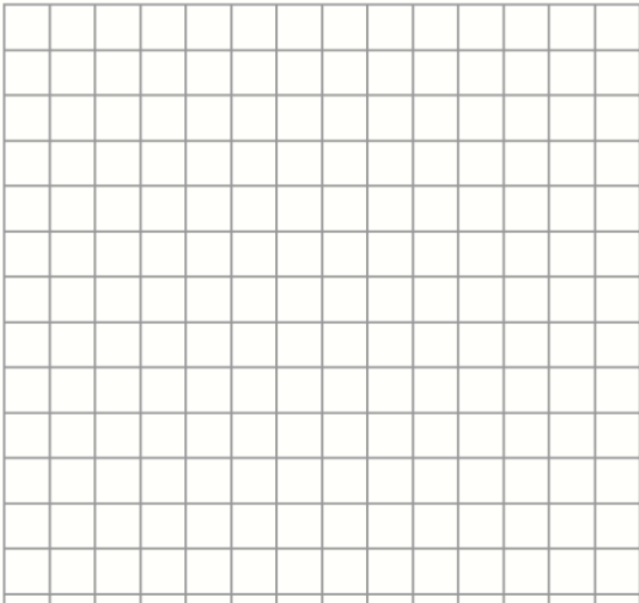
A net shows what a 3D solid could look like if 'unfolded' and laid out flat

Worked Example

Draw a net for the cuboid.

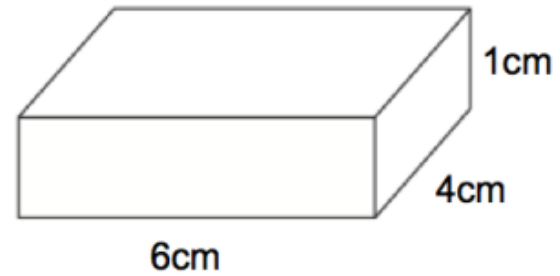


Each square represents 1 cm^2

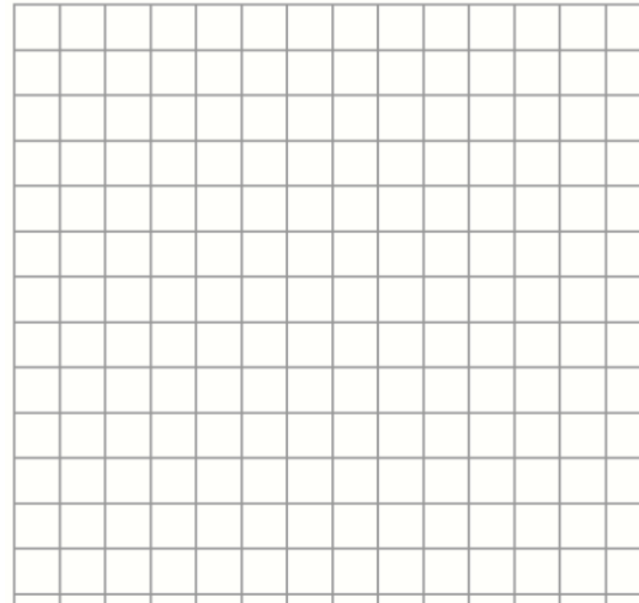


Your Turn

Draw a net for the cuboid.

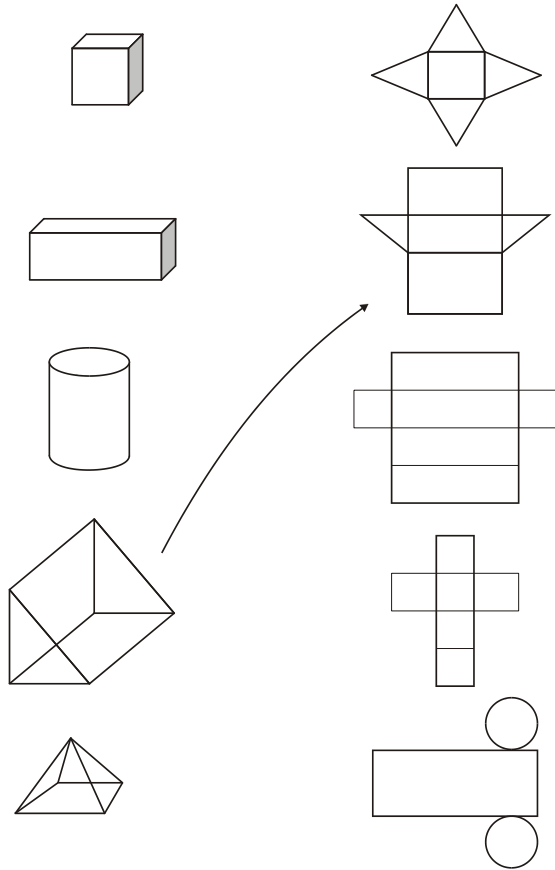


Each square represents 1 cm^2

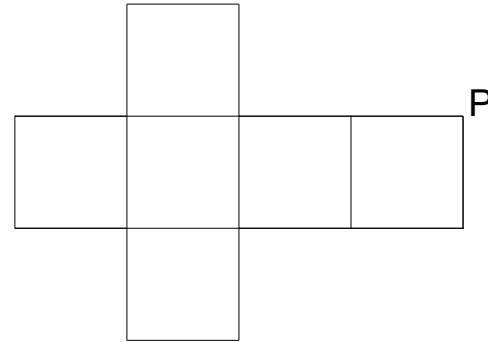


Fluency Practice

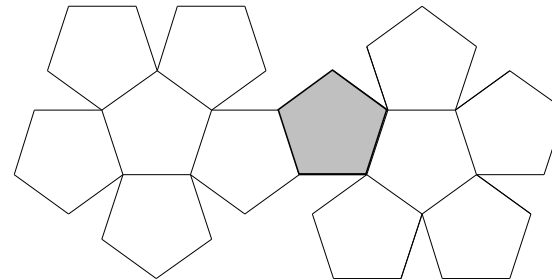
1. Match the 3D solids with their net



2. The net is folded to make a cube.
Two other vertices meet at *P*.
Mark each of these vertices with the letter *P*.

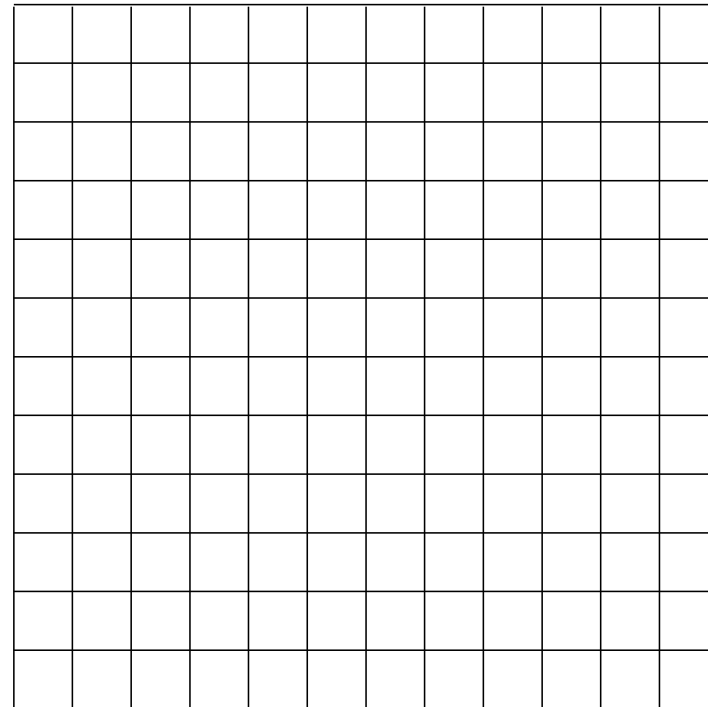
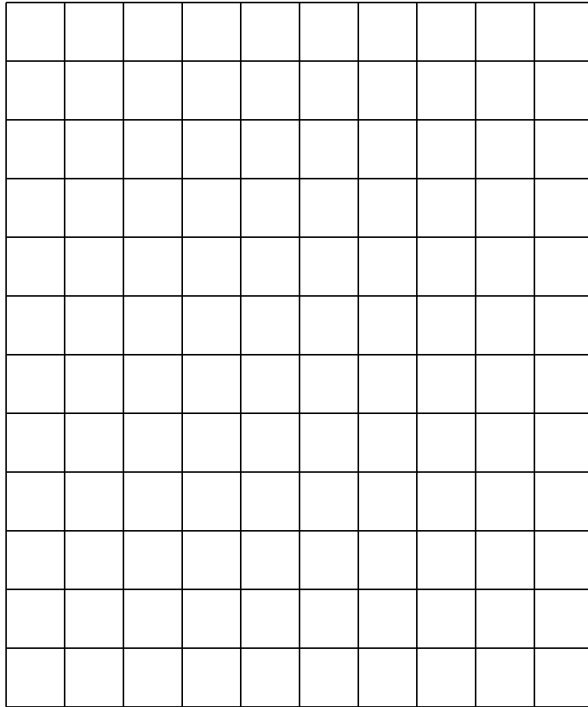
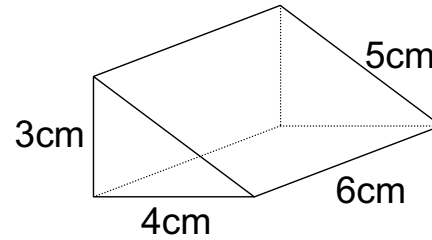
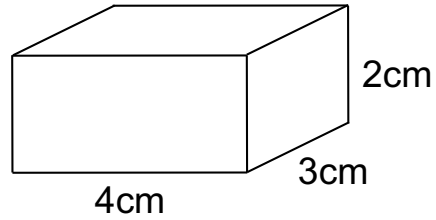


3. The net shown is folded to make a dodecahedron. Label the face which is opposite the shaded one



Fluency Practice

4. Using the grid provided with 1 square = 1 cm, draw an accurate net of these solids

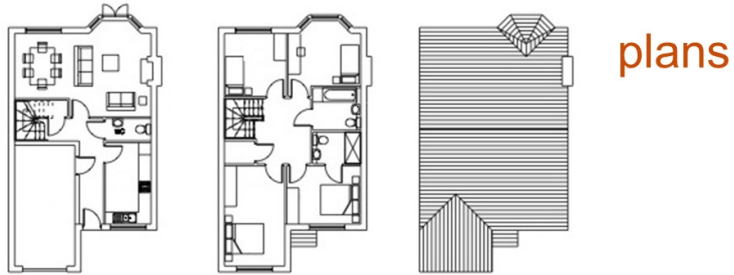


2 Plans and Elevations

The **plan** is the view from the top of a 3D solid.

Elevations are horizontal views of a 3D object:

- **Front elevation:** The view from the front of an object.
- **Back elevation:** The view from behind the object.
- **Side elevation:** The view from the side of an object.



front
elevation

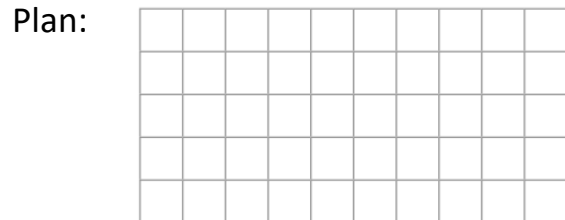
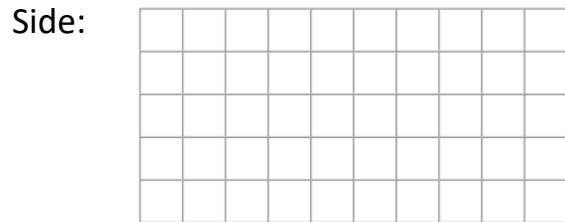
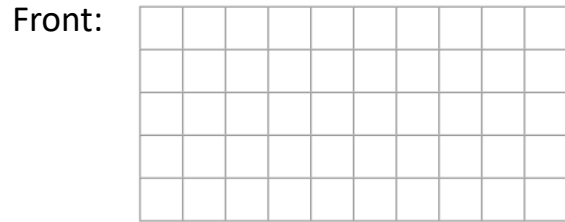
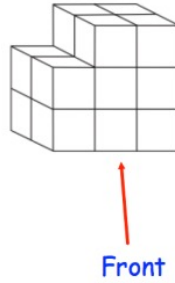
side
elevation

back
elevation

side
elevation

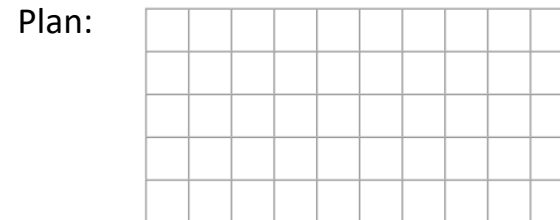
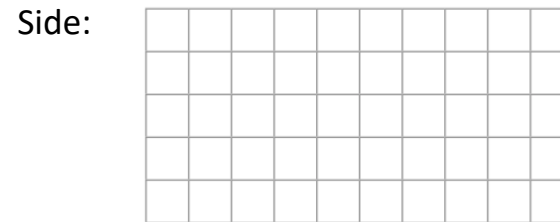
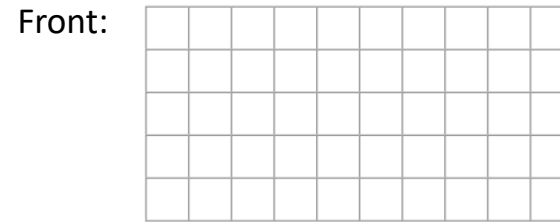
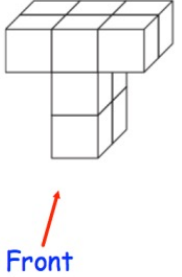
Worked Example

A shape is made of centimetre cubes. On the centimetre square grid, draw the elevations:



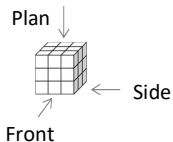
Your Turn

A shape is made of centimetre cubes. On the centimetre square grid, draw the elevations:



Fluency Practice

Cutting Cubes 3 × 3 × 3



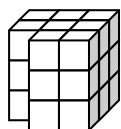
Draw the plan and elevations for each cube.

Solid line = a visible edge
Dashed line = a hidden edge

If we can see where all the missing cubes have been removed, we assume...?

1

Ex.)



Plan



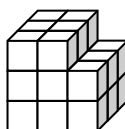
Side Elevation



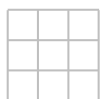
Front Elevation



a)



Plan



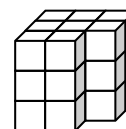
Side Elevation



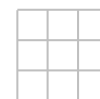
Front Elevation



b)



Plan



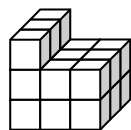
Side Elevation



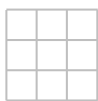
Front Elevation



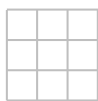
c)



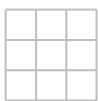
Plan



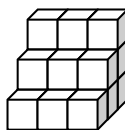
Side Elevation



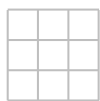
Front Elevation



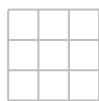
d)



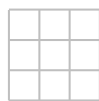
Plan



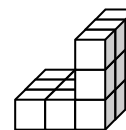
Side Elevation



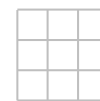
Front Elevation



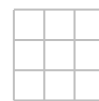
e)



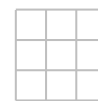
Plan



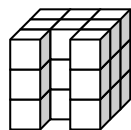
Side Elevation



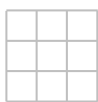
Front Elevation



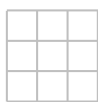
f)



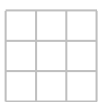
Plan



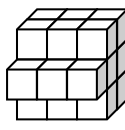
Side Elevation



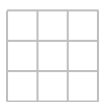
Front Elevation



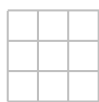
g)



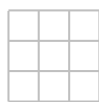
Plan



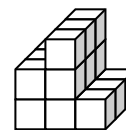
Side Elevation



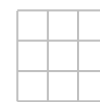
Front Elevation



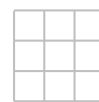
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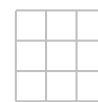
Plan



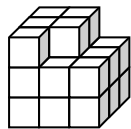
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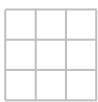
Front Elevation



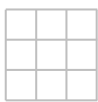
i)



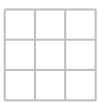
Plan



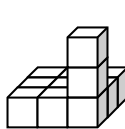
Side Elevation



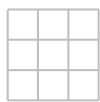
Front Elevation



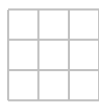
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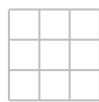
Plan



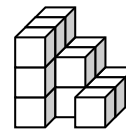
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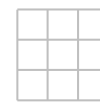
Front Elevation



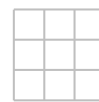
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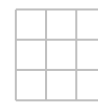
Plan



Side Elevation

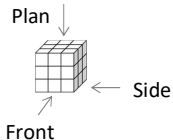


Front Elevation



Fluency Practice

Cutting Cubes 3 × 3 × 3



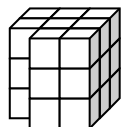
Draw the plan and elevations for each cube.

Solid line = a visible edge
Dashed line = a hidden edge

If we can see where all the missing cubes have been removed, we assume...?

2

Ex.)



Plan



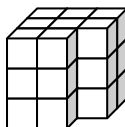
Side Elevation



Front Elevation



a)



Plan



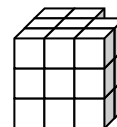
Side Elevation



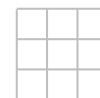
Front Elevation



b)



Plan



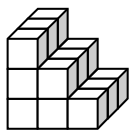
Side Elevation



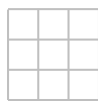
Front Elevation



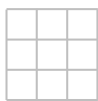
c)



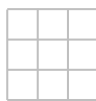
Plan



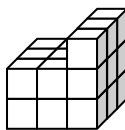
Side Elevation



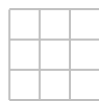
Front Elevation



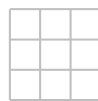
d)



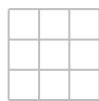
Plan



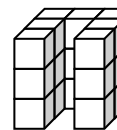
Side Elevation



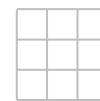
Front Elevation



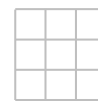
e)



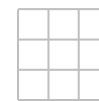
Plan



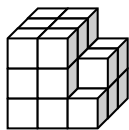
Side Elevation



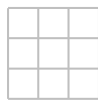
Front Elevation



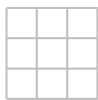
f)



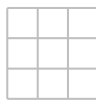
Plan



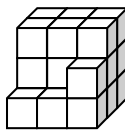
Side Elevation



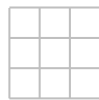
Front Elevation



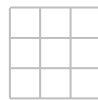
g)



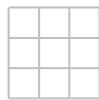
Plan



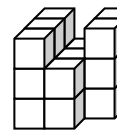
Side Elevation



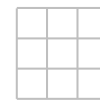
Front Elevation



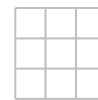
h)



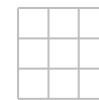
Plan



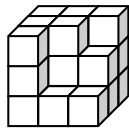
Side Elevation



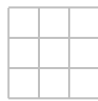
Front Elevation



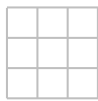
i)



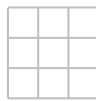
Plan



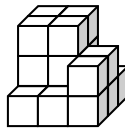
Side Elevation



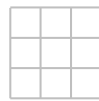
Front Elevation



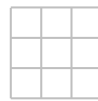
j)



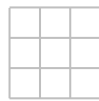
Plan



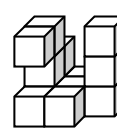
Side Elevation



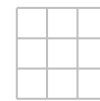
Front Elevation



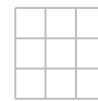
k)



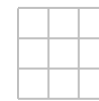
Plan



Side Elevation

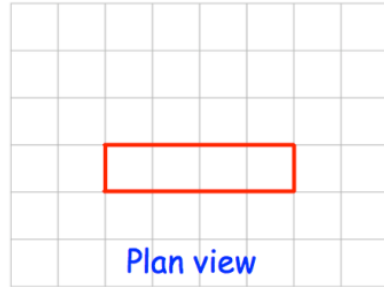
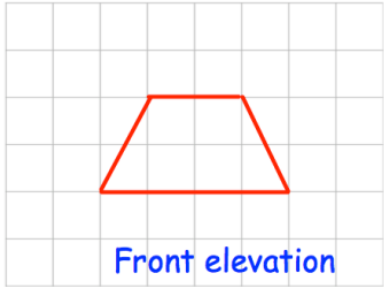


Front Elevation

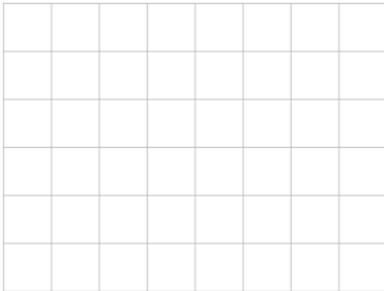


Worked Example

Given the elevations



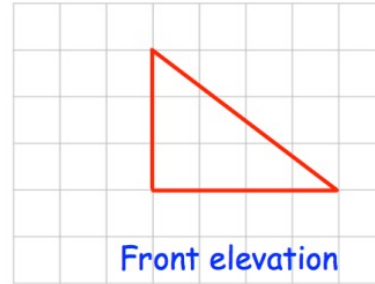
Draw the plan view



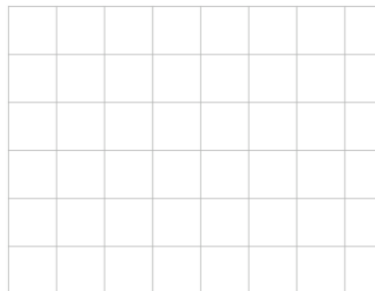
Sketch the solid shape

Your Turn

Given the elevations



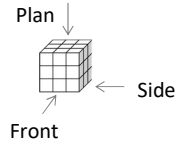
Draw the plan view



Sketch the solid shape

Fluency Practice

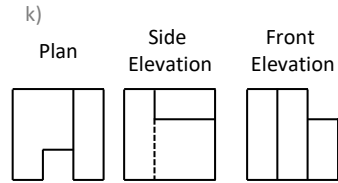
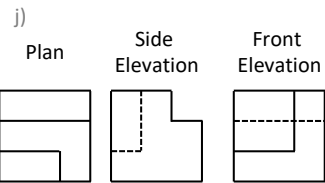
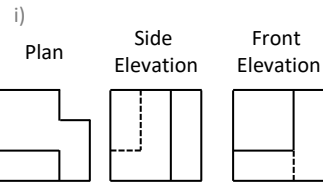
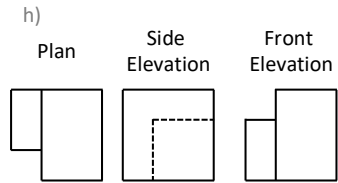
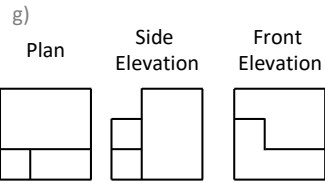
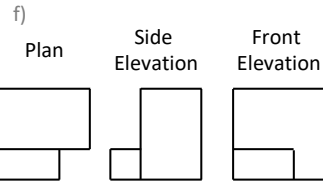
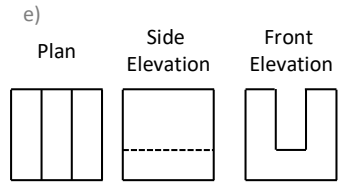
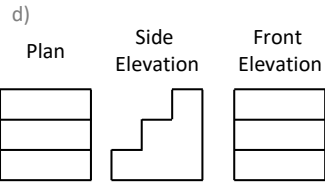
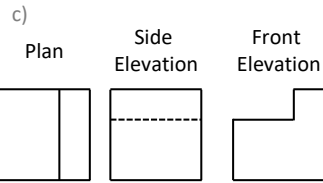
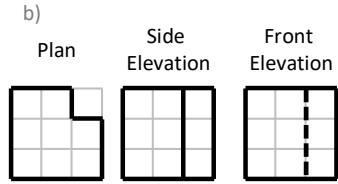
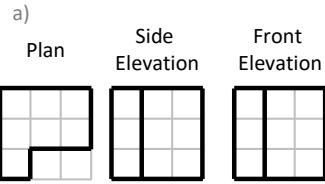
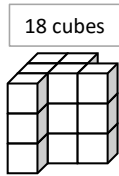
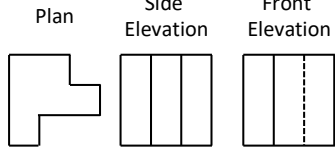
Counting Cubes $3 \times 3 \times 3$



The plans & elevations for different shapes are shown.

How many cubes are in each shape?

EX.)



3 Volume and Surface Area of Prisms

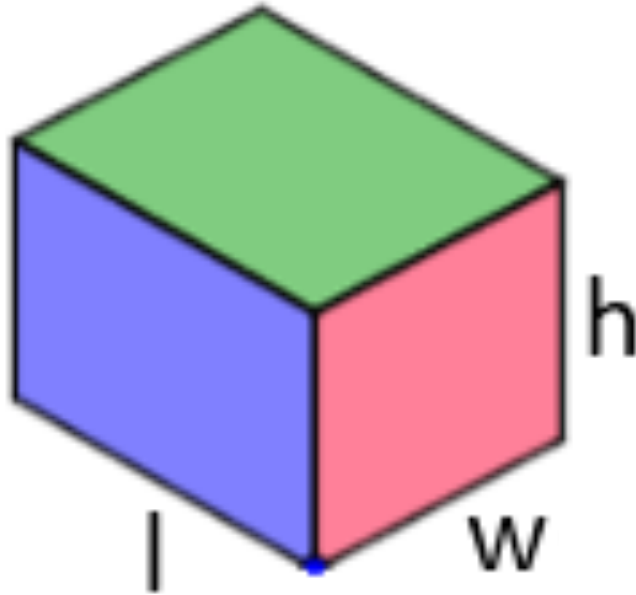
Volume is the amount of space an object takes up.

Surface Area is the total area across the surface.

Volume of Cuboids

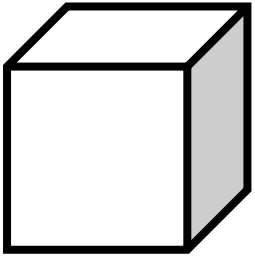
Volume of Cuboid = Length \times Width \times Height

Volume of Cuboid = $l \times w \times h$



Worked Example

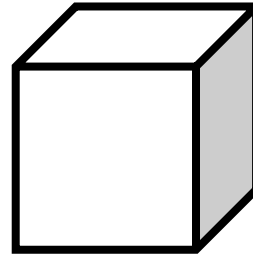
Calculate the volume of the cube:



3 cm

Your Turn

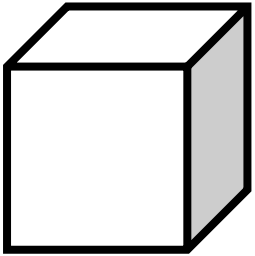
Calculate the volume of the cube:



5 cm

Worked Example

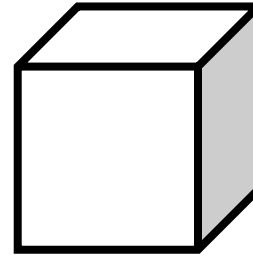
Find x , given that the volume of the cube is 27 cm^3



$x \text{ cm}$

Your Turn

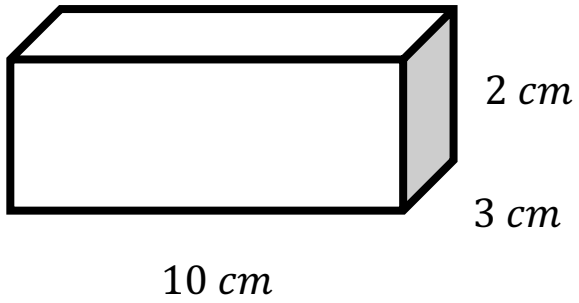
Find x , given that the volume of the cube is 125 cm^3



$x \text{ cm}$

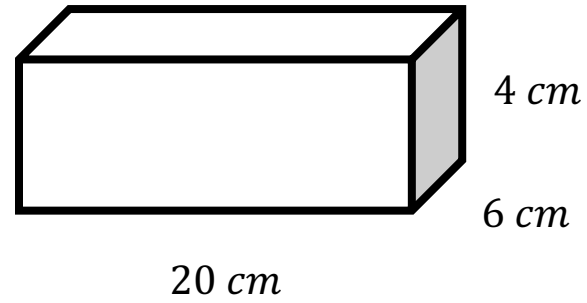
Worked Example

Calculate the volume of the cuboid:



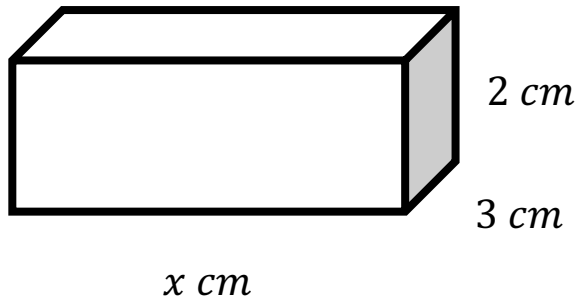
Your Turn

Calculate the volume of the cuboid:



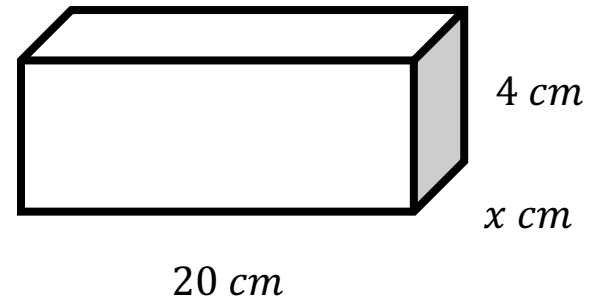
Worked Example

Find x , given that the volume of the cuboid is 60 cm^3



Your Turn

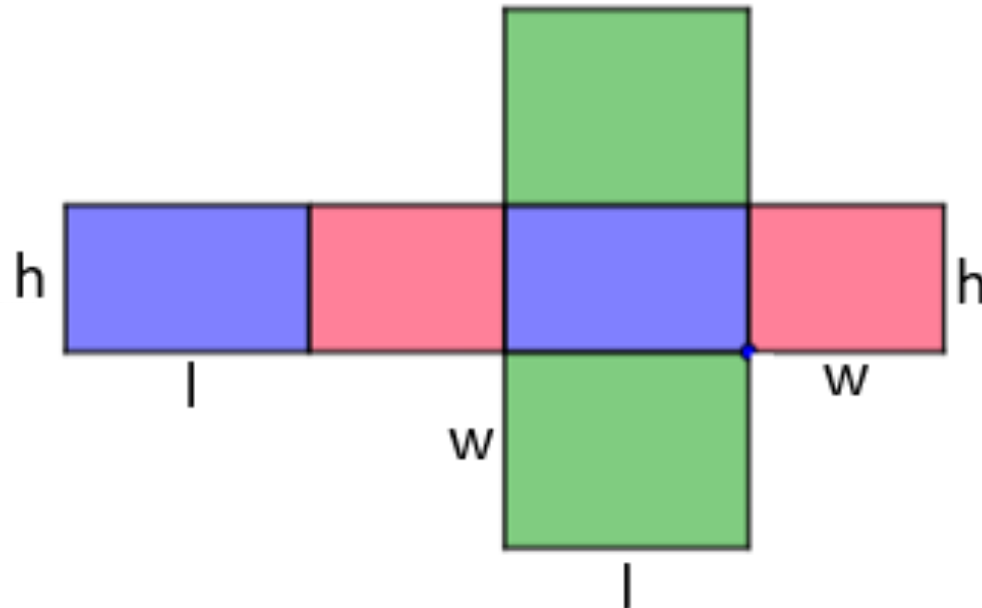
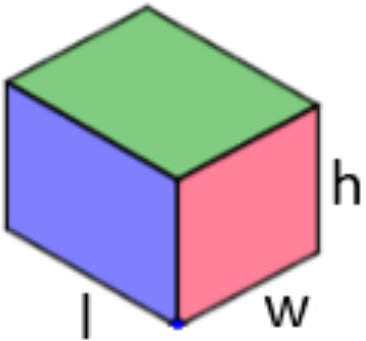
Find x , given that the volume of the cuboid is 480 cm^3



Surface Area of Cuboids

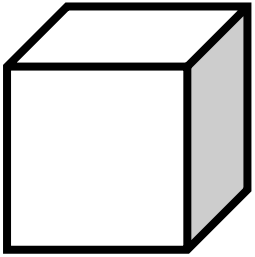
Surface Area of Cuboid = $2 \times \text{Length} \times \text{Width} + 2 \times \text{Length} \times \text{Height} + 2 \times \text{Width} \times \text{Height}$

Surface Area of Cuboid = $2lw + 2lh + 2wh$



Worked Example

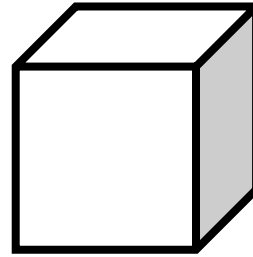
Calculate the surface area of the cube:



3 cm

Your Turn

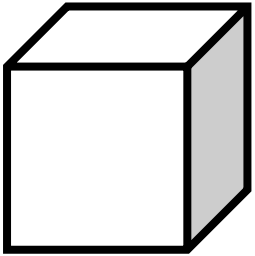
Calculate the surface area of the cube:



5 cm

Worked Example

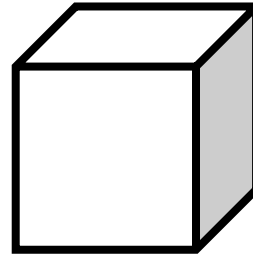
Find x , given that the total surface area of the cube is 54 cm^2 :



$x \text{ cm}$

Your Turn

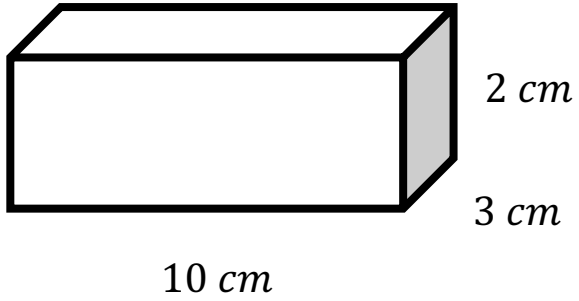
Find x , given that the total surface area of the cube is 150 cm^2 :



$x \text{ cm}$

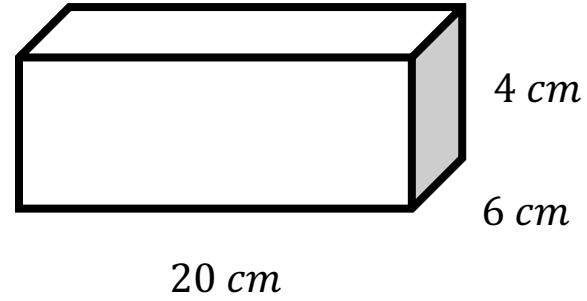
Worked Example

Calculate the total surface area of the cuboid:



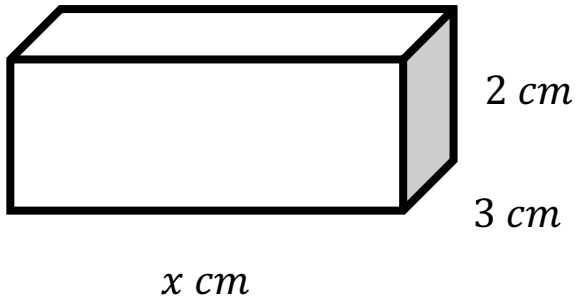
Your Turn

Calculate the total surface area of the cuboid:



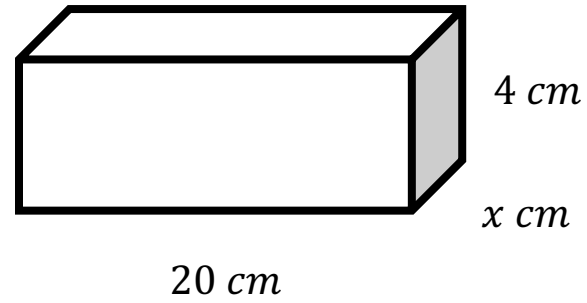
Worked Example

Find x , given that the total surface area is 448 cm^2



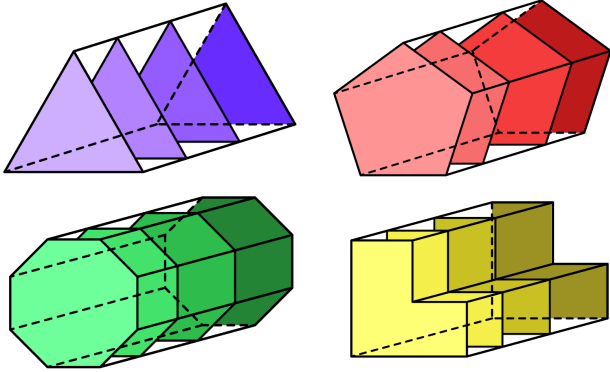
Your Turn

Find x , given that the total surface area is 112 cm^2



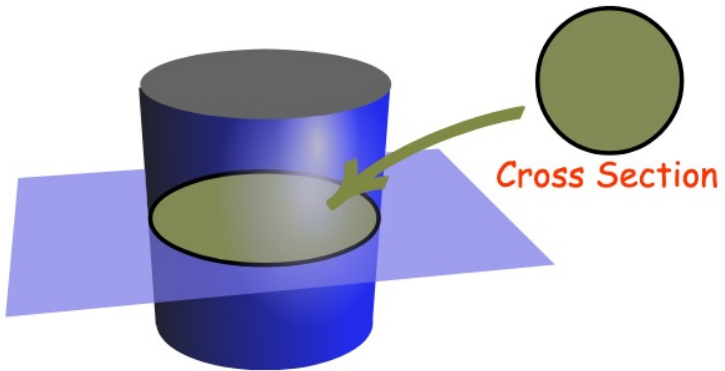
Prisms

A **prism** is a 3D shape which has the same *cross-section* along its length.

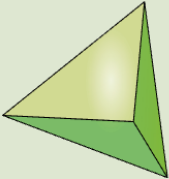
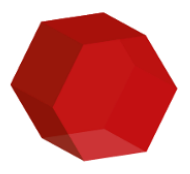
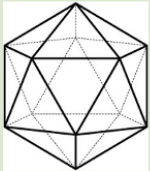
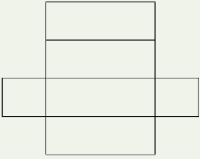
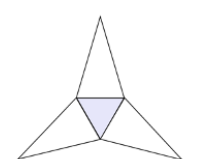


Cross-Section


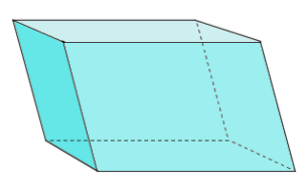

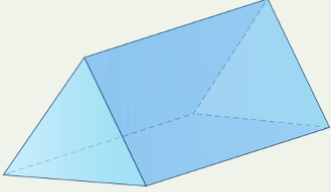

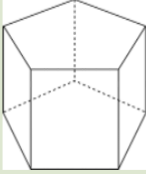
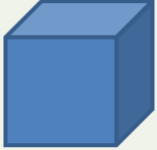
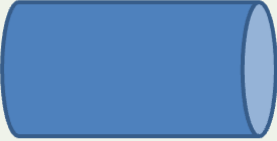
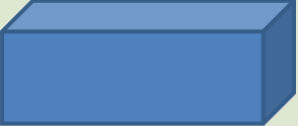
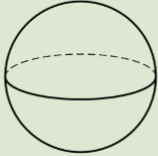
It is the shape made when a solid is cut through parallel to the base.



What is a Prism?

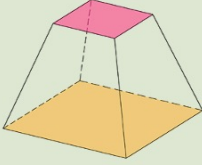
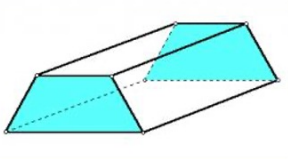
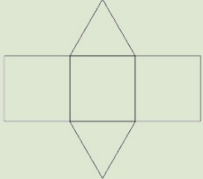

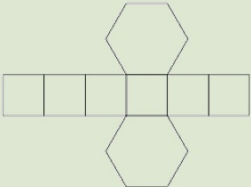
Shape	Prism?
	
	
	
<p data-bbox="126 853 188 889">Net</p> 	
<p data-bbox="126 1079 188 1115">Net</p> 	

Fluency Practice

Shape	Prism?	Shape	Prism?
			
			
			
			
			

Fluency Practice

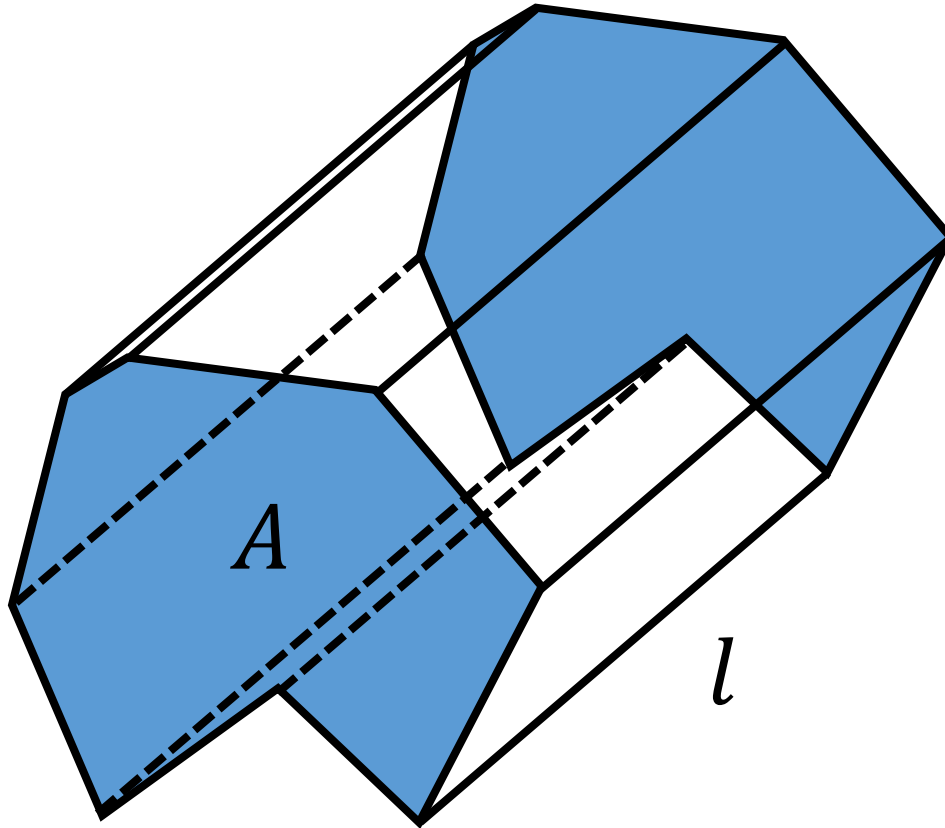
Shape	Prism?
	
	
	
	
	

Shape	Prism?
	
	
Net 	
Net 	
Net 	

Volume of Prisms

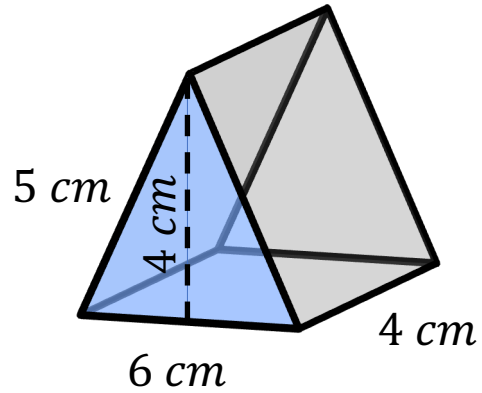
Volume of Prism = Area of Cross Section \times Length

Volume of Prism = $A \times l$



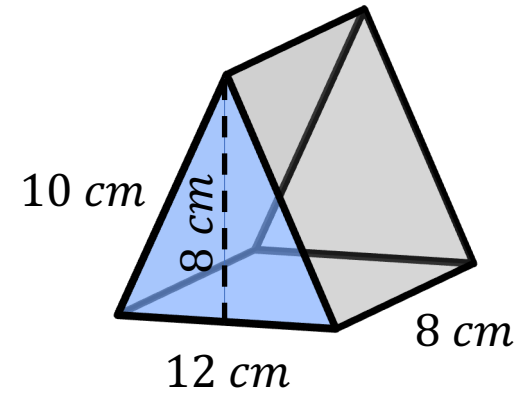
Worked Example

Calculate the volume of the triangular prism:



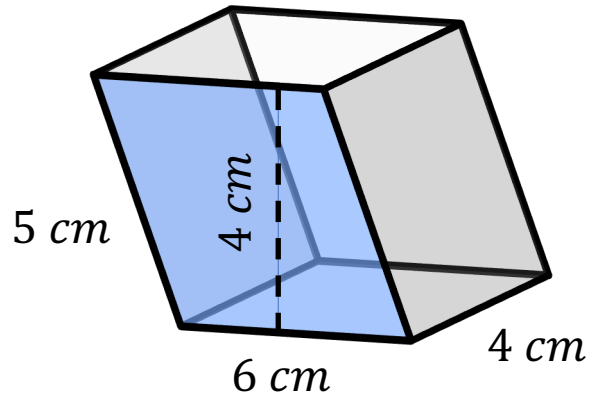
Your Turn

Calculate the volume of the triangular prism:



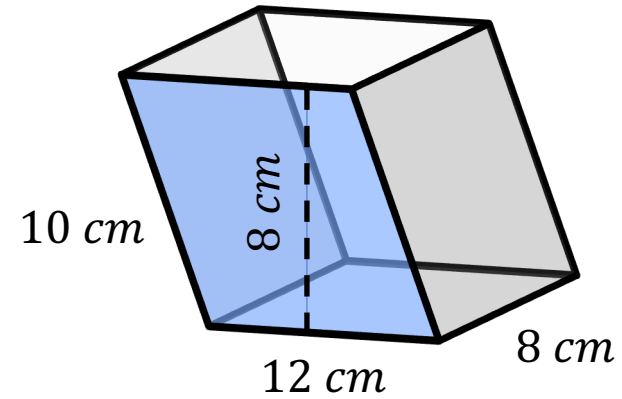
Worked Example

Calculate the volume of the parallelepiped:



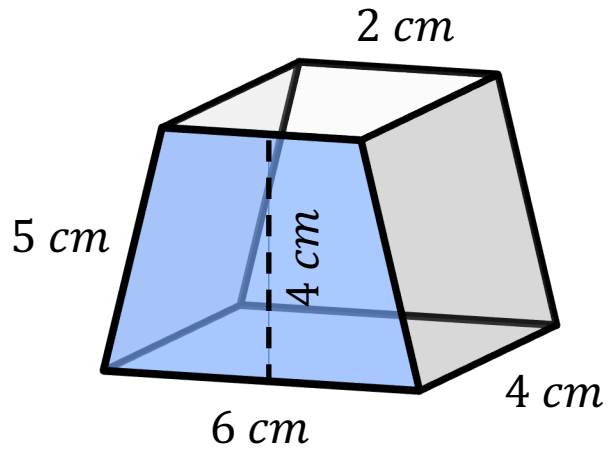
Your Turn

Calculate the volume of the parallelepiped:



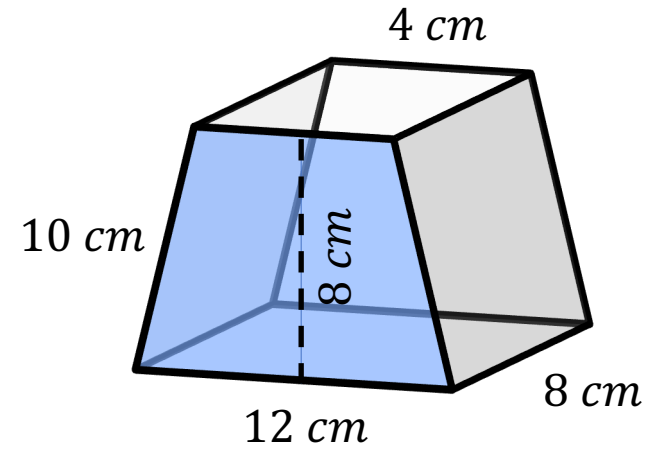
Worked Example

Calculate the volume of the trapezium prism:



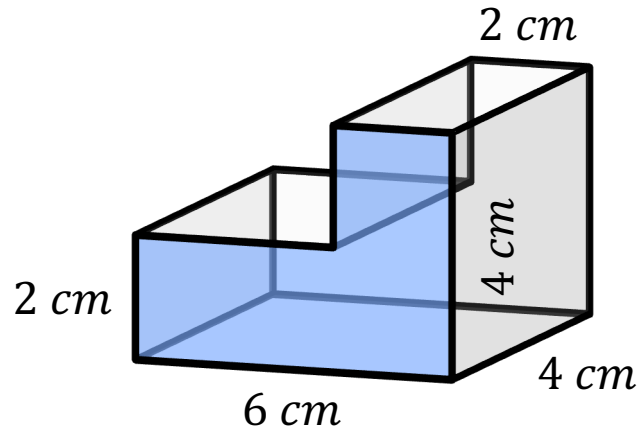
Your Turn

Calculate the volume of the trapezium prism:



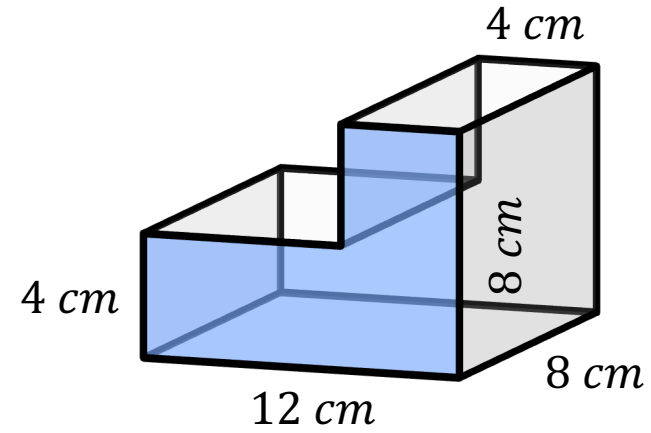
Worked Example

Calculate the volume of the trapezium prism:



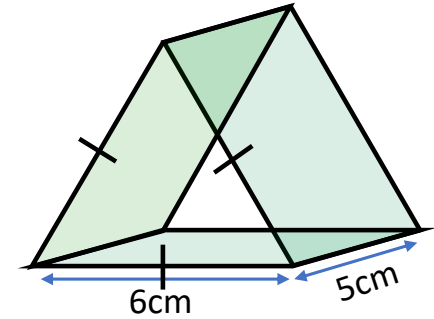
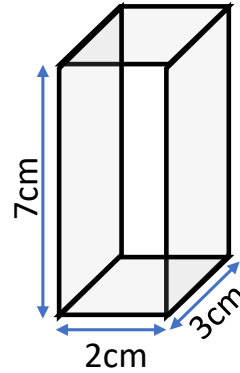
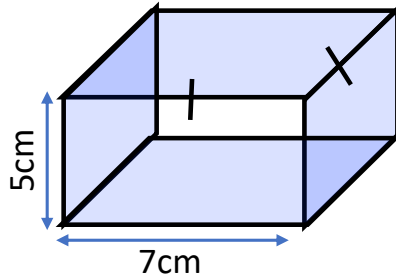
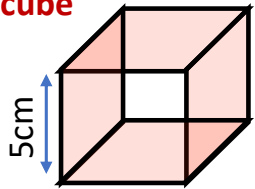
Your Turn

Calculate the volume of the trapezium prism:



Tubes

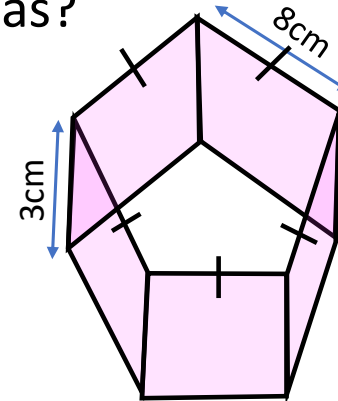
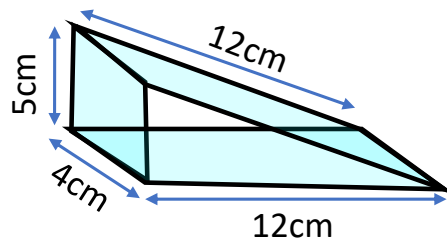
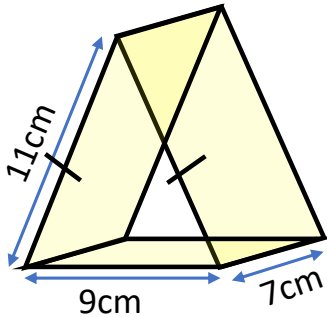
cube



Here are 7 prism "tubes"

Calculate the area of the net that makes each of the 7 tubes

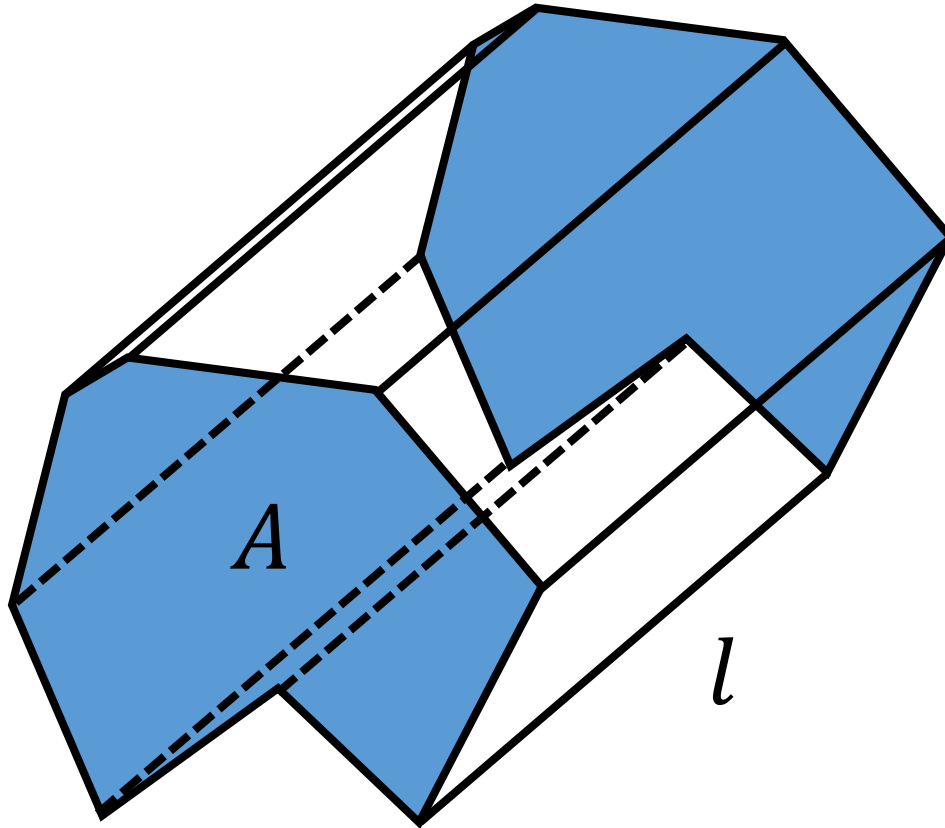
Is there are quick way the find the areas?



Surface Area of Prisms

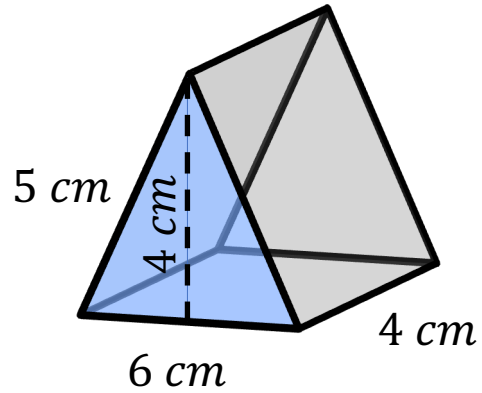
Surface Area of Prism = $2 \times \text{Area of Cross Section} + \text{Length} \times \text{Perimeter of Cross Section}$

Surface Area of Prism = $2A + LP$



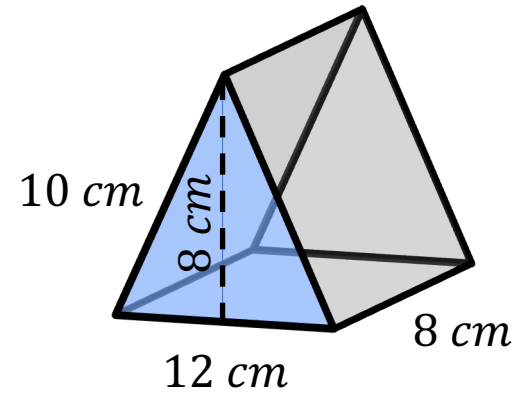
Worked Example

Calculate the surface area of the triangular prism:



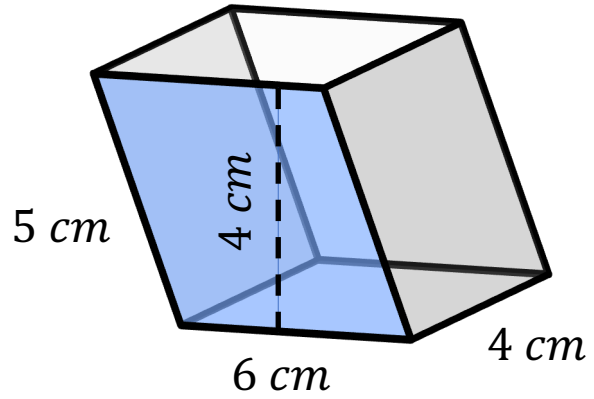
Your Turn

Calculate the surface area of the triangular prism:



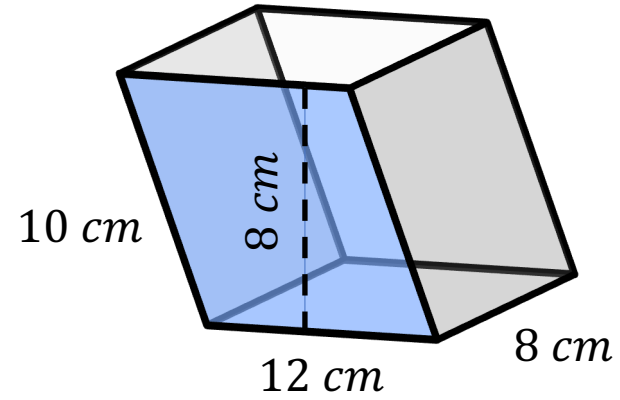
Worked Example

Calculate the surface area of the parallelepiped:



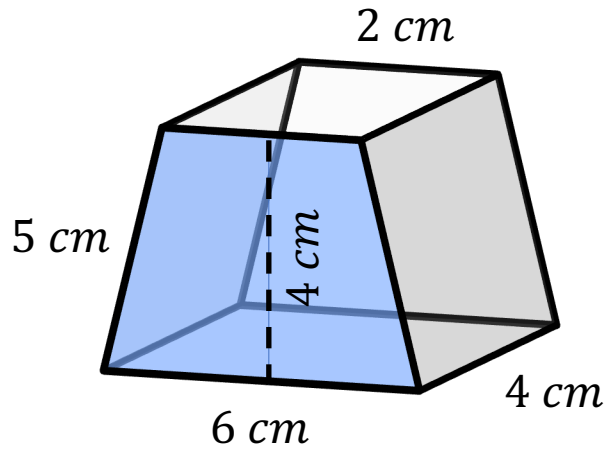
Your Turn

Calculate the surface area of the parallelepiped:



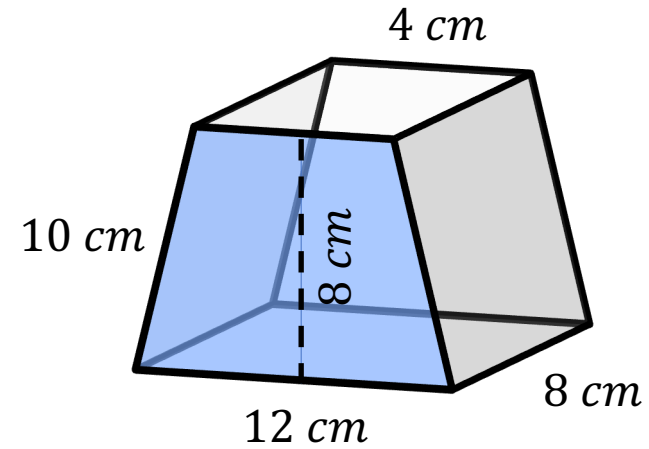
Worked Example

Calculate the surface area of the trapezium prism:



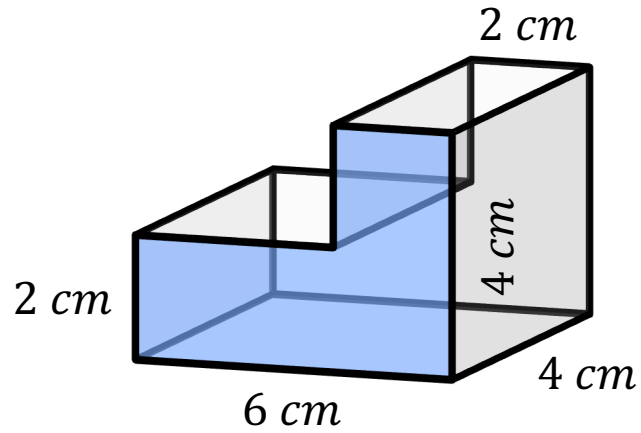
Your Turn

Calculate the surface area of the trapezium prism:



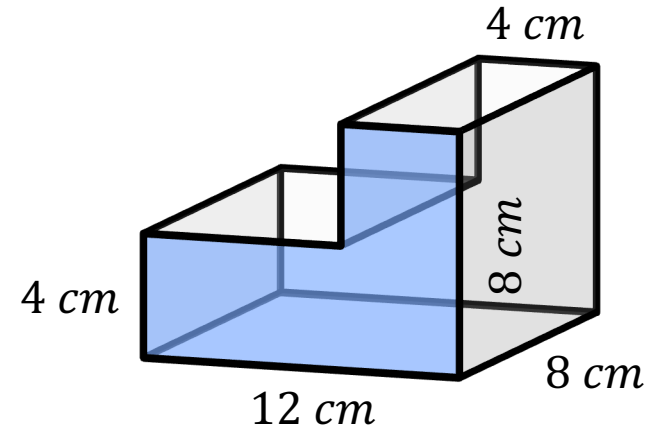
Worked Example

Calculate the surface area of the L-shaped prism:



Your Turn

Calculate the surface area of the L-shaped prism:

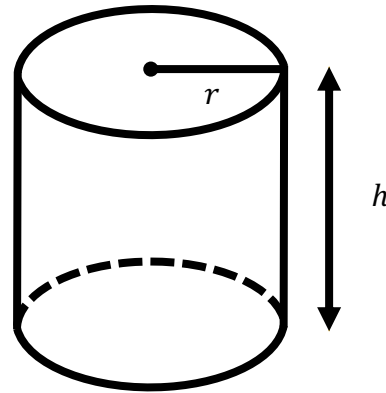


Volume of Cylinders

Volume of Cylinder = Area of circle \times height

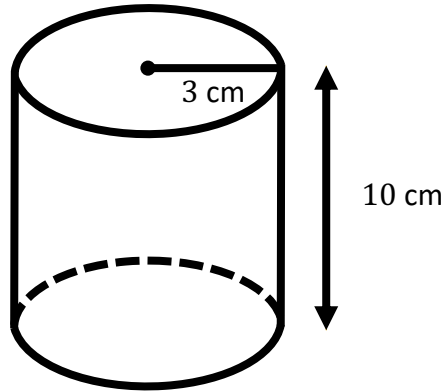
Volume of Cylinder = $\pi \times \text{radius}^2 \times \text{height}$

Volume of Cylinder = $\pi r^2 h$



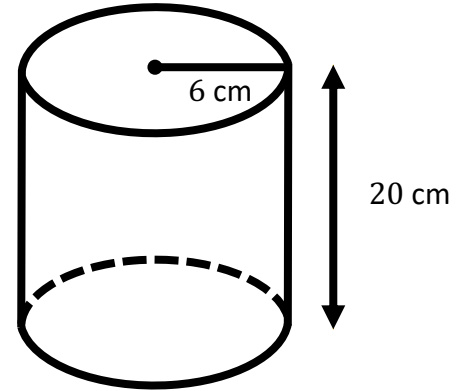
Worked Example

Calculate the volume of the following cylinder. Give your answer in terms of π and to 1 decimal place.



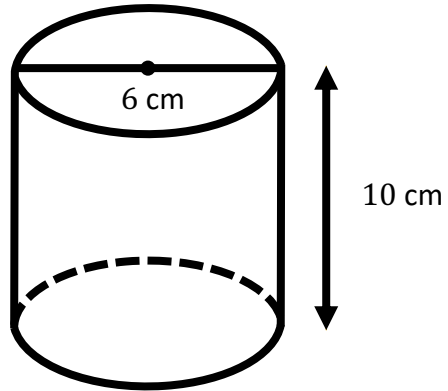
Your Turn

Calculate the volume of the following cylinder. Give your answer in terms of π and to 1 decimal place.



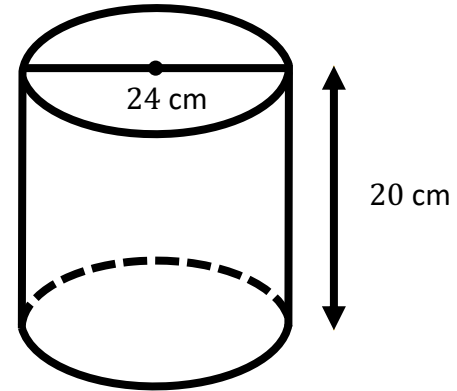
Worked Example

Calculate the volume of the following cylinder. Give your answer in terms of π and to 1 decimal place.



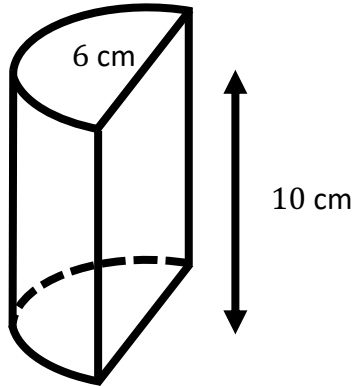
Your Turn

Calculate the volume of the following cylinder. Give your answer in terms of π and to 1 decimal place.



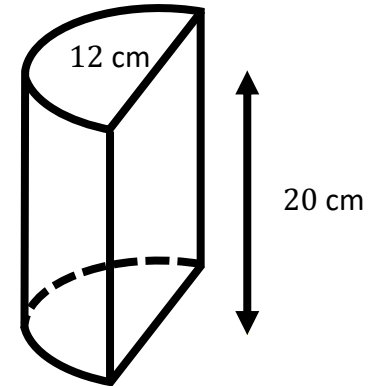
Worked Example

Calculate the volume of the following half cylinder. Give your answer in terms of π and to 1 decimal place.



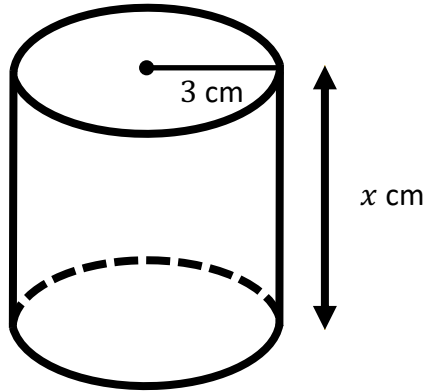
Your Turn

Calculate the volume of the following half cylinder. Give your answer in terms of π and to 1 decimal place.



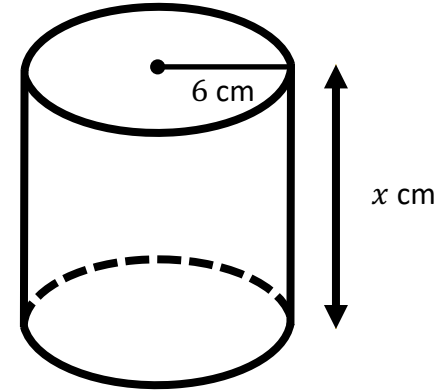
Worked Example

Find the height, x , given that the volume of the following cylinder is 282.7 cm^3 . Give your answer to 1 decimal place.



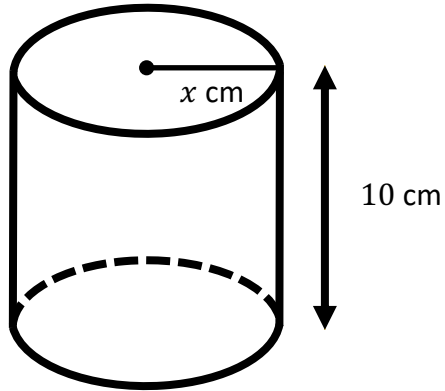
Your Turn

Find the height, x , given that the volume of the following cylinder is 2261.9 cm^3 . Give your answer to 1 decimal place.



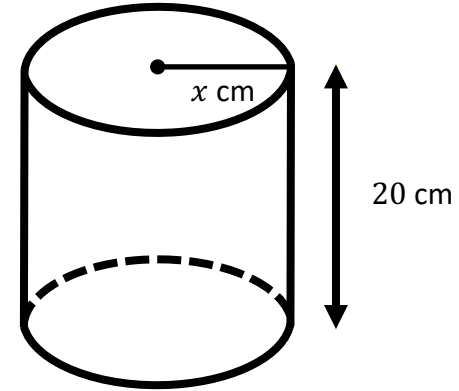
Worked Example

Find the radius, x , given that the volume of the following cylinder is 282.7 cm^3 . Give your answer to 1 decimal place.



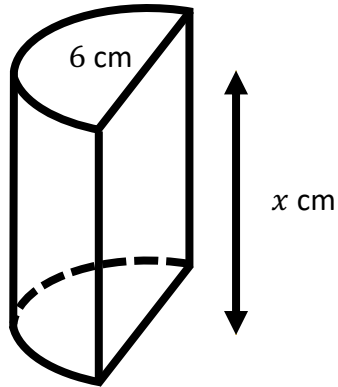
Your Turn

Find the radius, x , given that the volume of the following cylinder is 2261.9 cm^3 . Give your answer to 1 decimal place.



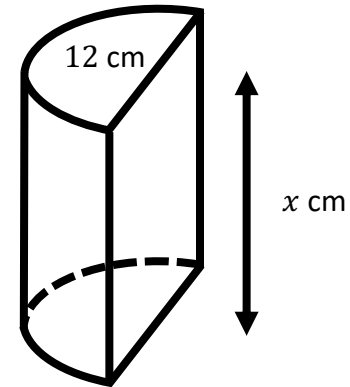
Worked Example

Find the height, x , given that the volume of the following half cylinder is 141.4 cm^3 . Give your answer to 1 decimal place.



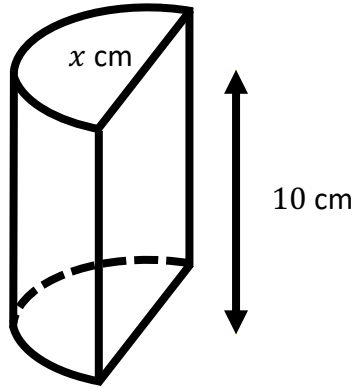
Your Turn

Find the height, x , given that the volume of the following half cylinder is 1131.0 cm^3 . Give your answer to 1 decimal place.



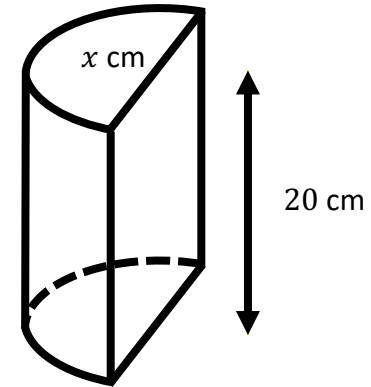
Worked Example

Find the diameter, x , given that the volume of the following half cylinder is 141.4 cm^3 . Give your answer to 1 decimal place.



Your Turn

Find the diameter, x , given that the volume of the following half cylinder is 1131.0 cm^3 . Give your answer to 1 decimal place.



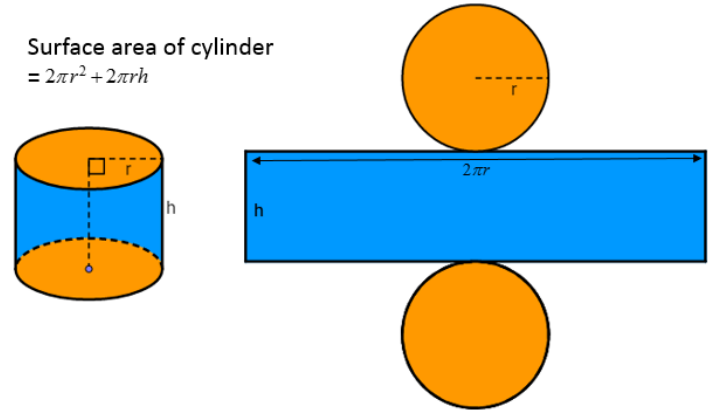
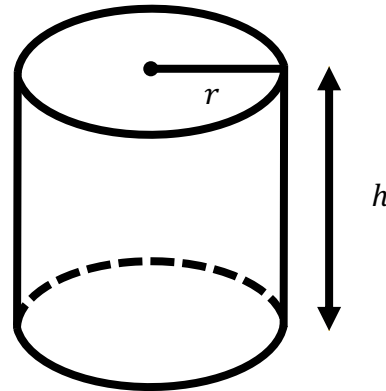
Surface Area of Cylinders

Curved Surface Area of Cylinder = $2 \times \pi \times \text{radius} \times \text{height}$

Curved Surface Area of Cylinder = $2\pi rh$

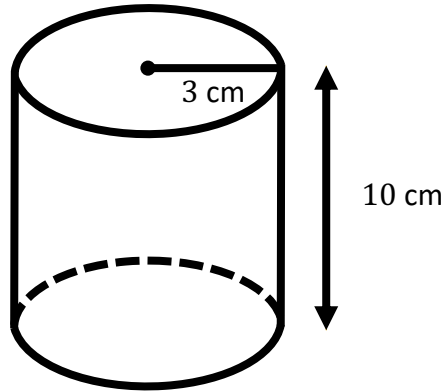
Total Surface Area of Cylinder = $2 \times \pi \times \text{radius} \times \text{height}$
+ $2 \times \pi \times \text{radius}^2$

Total Surface Area of Cylinder = $2\pi rh + 2\pi r^2$



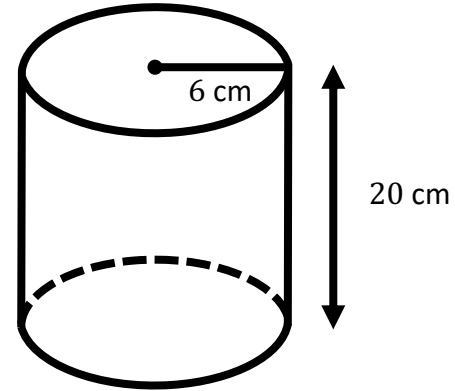
Worked Example

Calculate the curved surface area of the following cylinder.
Give your answer in terms of π and to 1 decimal place.



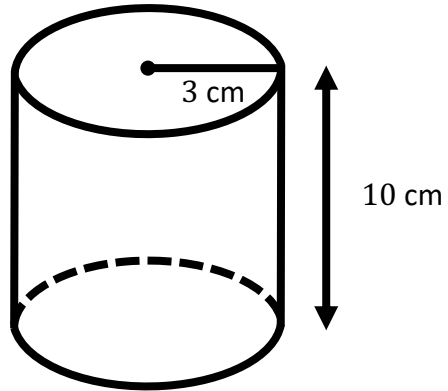
Your Turn

Calculate the curved surface area of the following cylinder.
Give your answer in terms of π and to 1 decimal place.



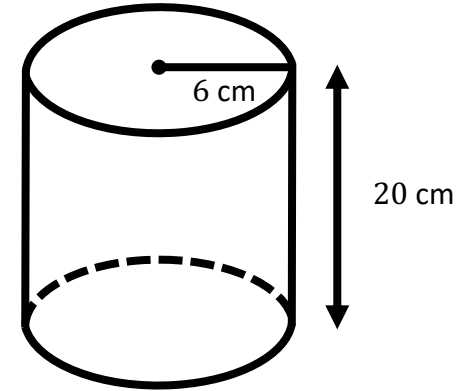
Worked Example

Calculate the total surface area of the following cylinder. Give your answer in terms of π and to 1 decimal place.



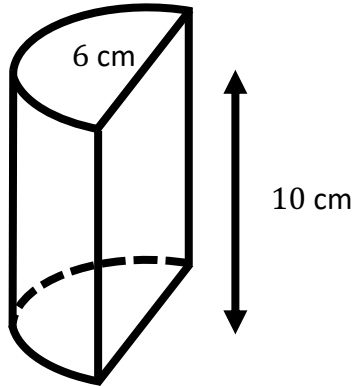
Your Turn

Calculate the total surface area of the following cylinder. Give your answer in terms of π and to 1 decimal place.



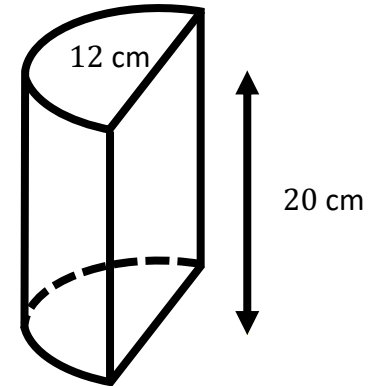
Worked Example

Calculate the curved surface area of the following half cylinder.
Give your answer in terms of π and to 1 decimal place.



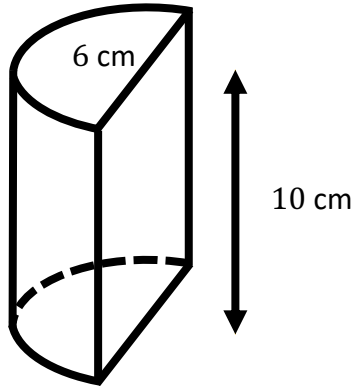
Your Turn

Calculate the curved surface area of the following half cylinder.
Give your answer in terms of π and to 1 decimal place.



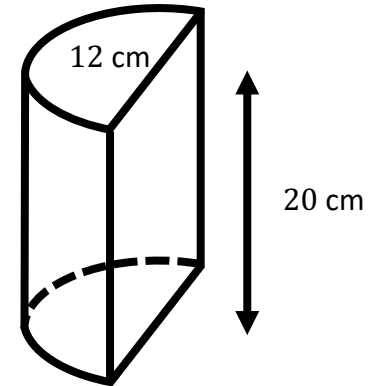
Worked Example

Calculate the total surface area of the following half cylinder.
Give your answer in terms of π and to 1 decimal place.



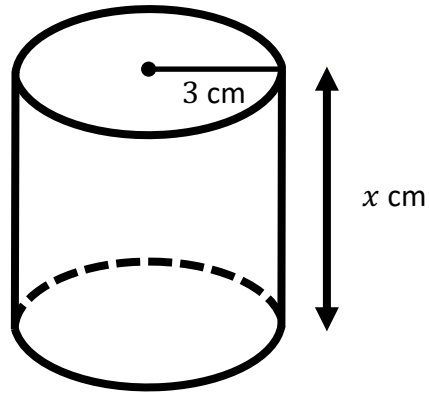
Your Turn

Calculate the total surface area of the following half cylinder.
Give your answer in terms of π and to 1 decimal place.



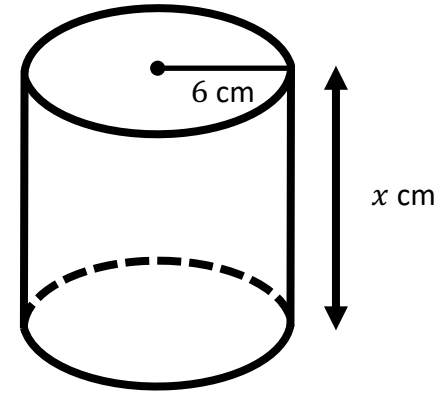
Worked Example

Find the height, x , given that the total surface area of the following cylinder is 245.0 cm^2 . Give your answer to 1 decimal place.



Your Turn

Find the height, x , given that the total surface area of the following cylinder is 980.2 cm^2 . Give your answer to 1 decimal place.



4 Area and Volume Unit Conversions

Units of Length Recap

$$1 \text{ km} = 1,000 \text{ m}$$

$$1 \text{ m} = 100 \text{ cm}$$

$$1 \text{ cm} = 10 \text{ mm}$$

Fill in the Gaps

Q	km	m	cm	mm
1	1			
2		1		
3			1	
4				1
5				10
6			17	
7		1.7		
8	1.07			
9	0.07			
10		0.07		
11			0.07	
12		$\frac{1}{3}$		
13		n		

Units of Area

Let's consider this square.



$4m$

$$\text{Area} = 4 \times 4 = 16m^2$$

Imagine we want to convert the area of this shape into cm^2 . What scale factor would we use?



$400cm$

$$\text{Area} = 400 \times 400$$

$$\text{Area} = 160,000cm^2$$

Is this what we expected?

Our scale factor is not 100, but 10,000. 100^2

Worked Example

Convert:

- a) 7 cm^2 to mm^2
- b) 2500 cm^2 to m^2

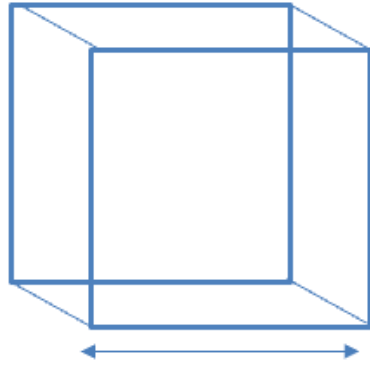
Your Turn

Convert:

- a) 7 km^2 to m^2
- b) 2500 mm^2 to cm^2

Units of Volume

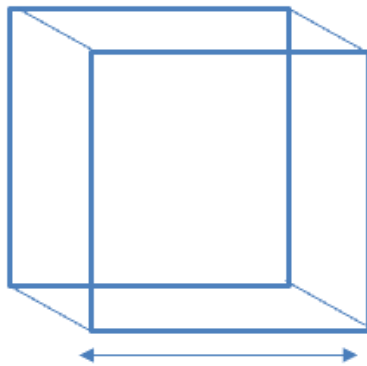
Let's now consider a cube of side 4 m.



$4m$

$$Volume = 4 \times 4 \times 4 = 64m^3$$

Imagine we want to convert the area of this shape into cm^3 . What scale factor would we use?



$400cm$

$$Volume = 400 \times 400 \times 400 = 64,000,000cm^3$$

Our scale factor is not 100, but 1,000,000. 100^3

Worked Example

Convert:

- a) 7 cm^3 to mm^3
- b) 5 mm^3 to cm^3

Your Turn

Convert:

- a) 7 m^3 to cm^3
- b) 5 cm^3 to m^3

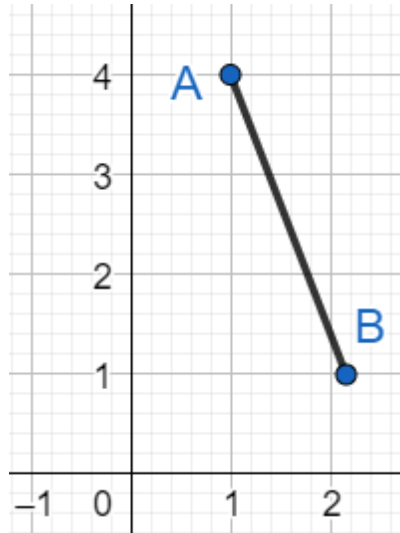
5 Basic Vectors

A vector has magnitude (how long it is) and direction.

Column Vector: $\begin{pmatrix} x \\ y \end{pmatrix}$ where x is movement right or left and y is movement up or down. Right and up are taken to be positive.

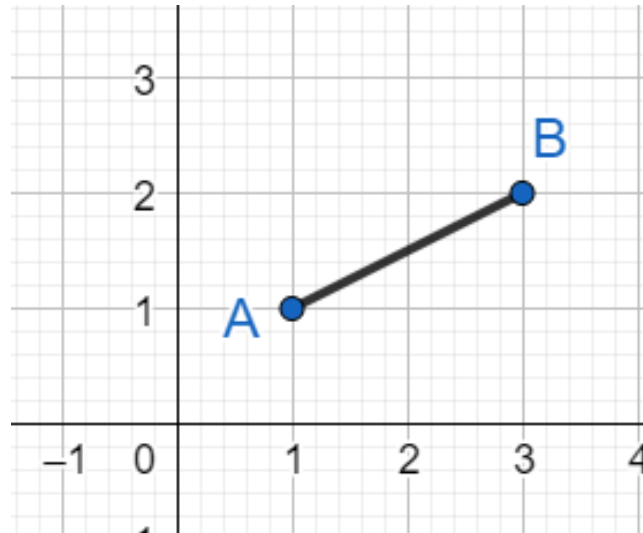
Worked Example

Write the vector \overrightarrow{AB} in column form



Your Turn

Write the vector \overrightarrow{AB} in column form



Fluency Practice

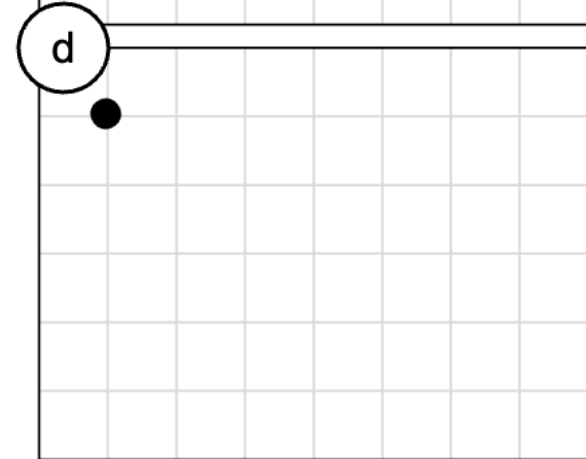
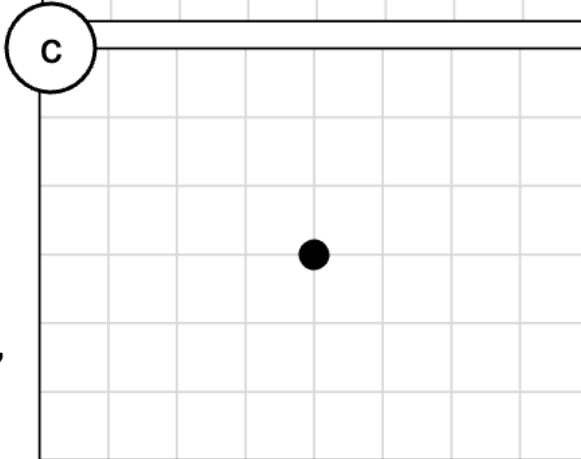
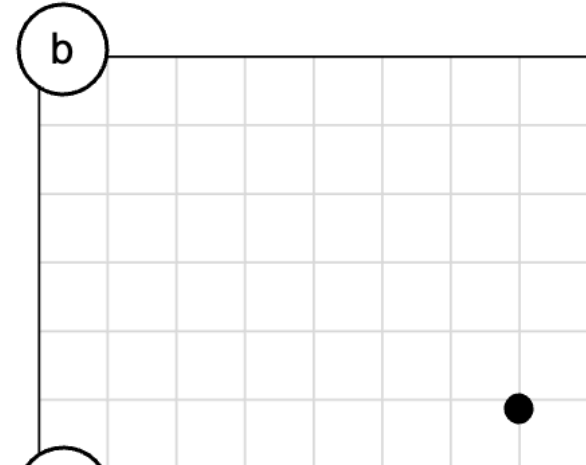
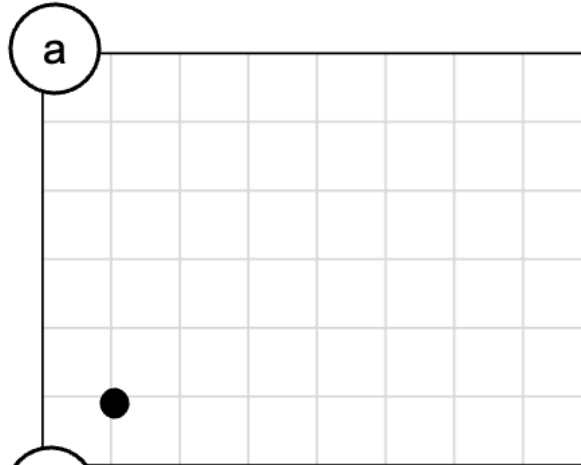
On each grid, start at the dot, then draw each vector in turn.

a) $\begin{pmatrix} 0 \\ 4 \end{pmatrix}, \begin{pmatrix} 3 \\ -2 \end{pmatrix}, \begin{pmatrix} 3 \\ 2 \end{pmatrix}, \begin{pmatrix} 0 \\ -4 \end{pmatrix}$

b) $\begin{pmatrix} -3 \\ 4 \end{pmatrix}, \begin{pmatrix} -3 \\ 0 \end{pmatrix}, \begin{pmatrix} 0 \\ -4 \end{pmatrix},$
 $\begin{pmatrix} 3 \\ 0 \end{pmatrix}, \begin{pmatrix} 0 \\ 2 \end{pmatrix}, \begin{pmatrix} 3 \\ -2 \end{pmatrix}$

c) $\begin{pmatrix} -2 \\ 0 \end{pmatrix}, \begin{pmatrix} 0 \\ 1 \end{pmatrix}, \begin{pmatrix} 1 \\ 0 \end{pmatrix}, \begin{pmatrix} 0 \\ -1 \end{pmatrix},$
 $\begin{pmatrix} 2 \\ 0 \end{pmatrix}, \begin{pmatrix} 0 \\ 1 \end{pmatrix}, \begin{pmatrix} 1 \\ 0 \end{pmatrix}, \begin{pmatrix} 0 \\ -1 \end{pmatrix},$
 $\begin{pmatrix} -2 \\ 0 \end{pmatrix}, \begin{pmatrix} 0 \\ -1 \end{pmatrix}, \begin{pmatrix} -2 \\ 0 \end{pmatrix}, \begin{pmatrix} 4 \\ 0 \end{pmatrix}$

d) $\begin{pmatrix} 0 \\ -2 \end{pmatrix}, \begin{pmatrix} 3 \\ 2 \end{pmatrix}, \begin{pmatrix} -3 \\ -4 \end{pmatrix}, \begin{pmatrix} 0 \\ 6 \end{pmatrix},$
 $\begin{pmatrix} 0 \\ 4 \end{pmatrix}, \begin{pmatrix} -1 \\ -2 \end{pmatrix}, \begin{pmatrix} -2 \\ 0 \end{pmatrix},$
 $\begin{pmatrix} 0 \\ 2 \end{pmatrix}, \begin{pmatrix} -3 \\ 0 \end{pmatrix}$



Worked Example

$$a = \begin{pmatrix} 2 \\ 3 \end{pmatrix}$$

Find $3a$



Your Turn

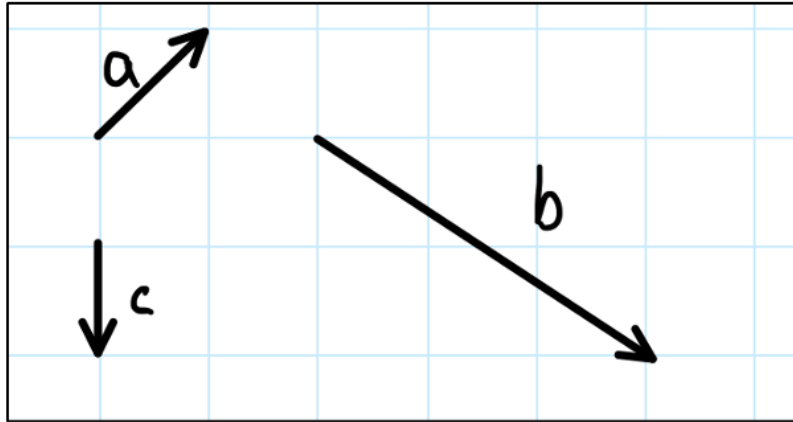
$$a = \begin{pmatrix} 2 \\ 3 \end{pmatrix}$$

Find $-2a$



Fluency Practice

Write each vector in column form



1) $2a$

2) $-4a$

3) $\frac{1}{2}a$

4) $\frac{3}{2}a$

5) $2c$

6) $-2c$

7) $-c$

8) $-b$

9) $-\frac{1}{2}b$

10) $\frac{3}{2}b$

Worked Example

$$\mathbf{a} = \begin{pmatrix} 2 \\ 3 \end{pmatrix} \quad \mathbf{b} = \begin{pmatrix} 5 \\ 7 \end{pmatrix}$$

Find $2\mathbf{a} - \mathbf{b}$

Your Turn

$$\mathbf{a} = \begin{pmatrix} 2 \\ 3 \end{pmatrix} \quad \mathbf{b} = \begin{pmatrix} 5 \\ 7 \end{pmatrix}$$

Find $3\mathbf{a} + 2\mathbf{b}$

Fluency Practice

Write these vectors in column form. Can you spot any links between questions?

$$\mathbf{a} = \begin{pmatrix} 1 \\ 2 \end{pmatrix} \quad \mathbf{b} = \begin{pmatrix} -2 \\ 1 \end{pmatrix} \quad \mathbf{c} = \begin{pmatrix} 9 \\ -5 \end{pmatrix} \quad \mathbf{d} = \begin{pmatrix} -6 \\ 4 \end{pmatrix}$$

1) $\mathbf{a} + \mathbf{b}$	2) $\mathbf{a} - \mathbf{b}$	3) $\mathbf{b} - \mathbf{a}$	4) $\mathbf{c} - \mathbf{d}$	5) $\mathbf{d} - \mathbf{c}$
6) $\mathbf{a} - \mathbf{a}$	7) $\mathbf{b} - \mathbf{b}$	8) $\mathbf{a} + \mathbf{b} + \mathbf{c}$	9) $\mathbf{a} + \mathbf{b} - \mathbf{c}$	10) $\mathbf{a} - \mathbf{b} + \mathbf{c}$
11) $2\mathbf{a} + 2\mathbf{b}$	12) $2\mathbf{a} - 2\mathbf{b}$	13) $2\mathbf{c} - 3\mathbf{d}$	14) $4\mathbf{c} - 6\mathbf{d}$	15) $20\mathbf{c} - 30\mathbf{d}$

6 Reflections

A transformation that flips all points so that they are the same distance from a given mirror line as the original points, but in the opposite direction.

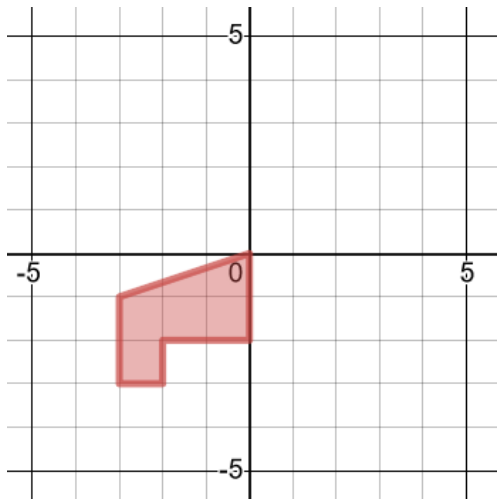
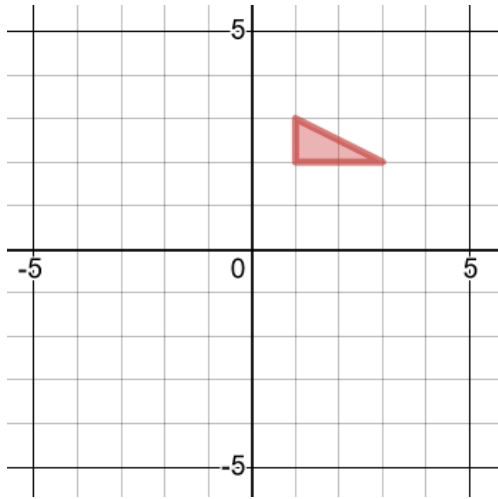
- Shapes flip over a mirror line.
- A shape and its reflection lie perfectly on top of each other if the page is folded in the mirror line.
- Produces a congruent shape.

To fully describe a reflection, you need to give two pieces of information:

1. Type of Transformation: Reflection
2. The Line of Reflection:
 - x – axis or y – axis
 - $y = \text{'a number'}$ or $x = \text{'a number'}$
 - $y = x$ or $y = -x$

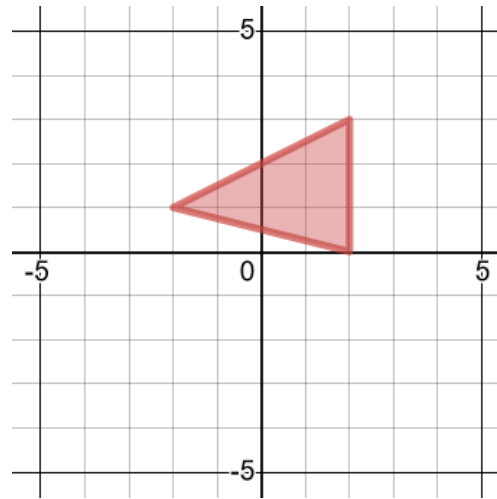
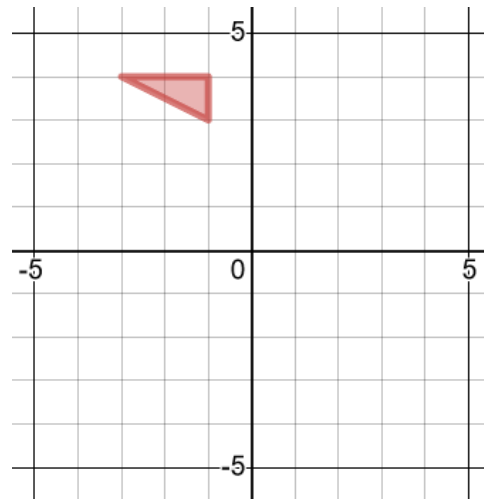
Worked Example

Reflect in the x -axis



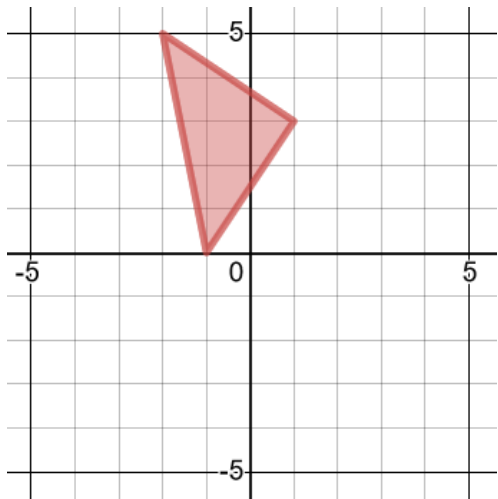
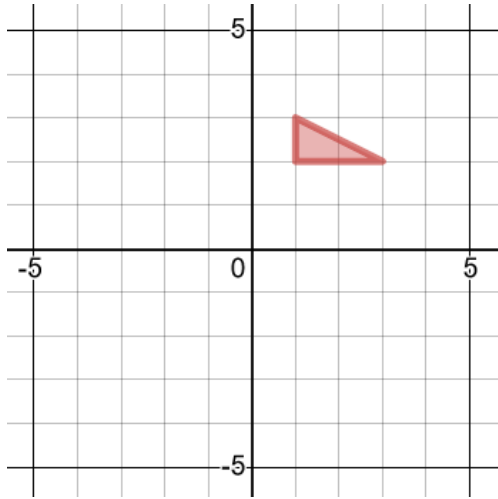
Your Turn

Reflect in the x -axis



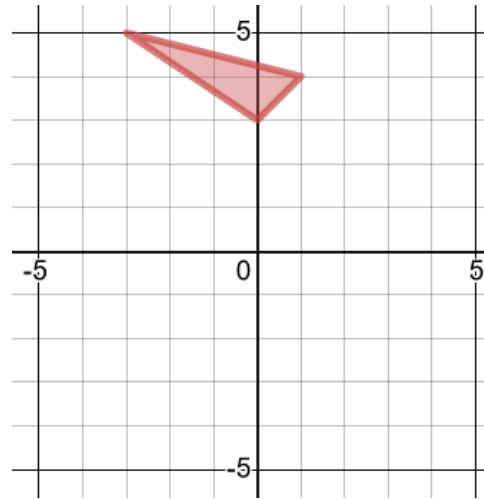
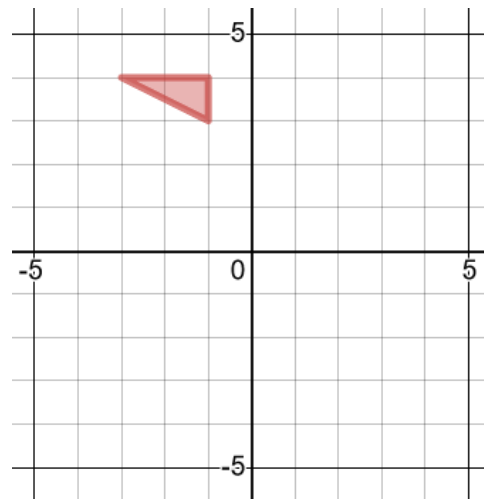
Worked Example

Reflect in the y -axis



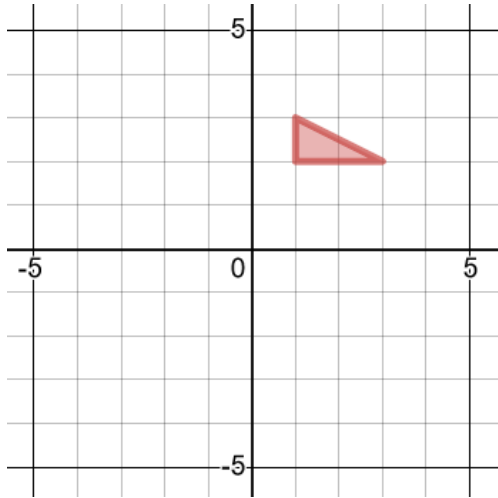
Your Turn

Reflect in the y -axis

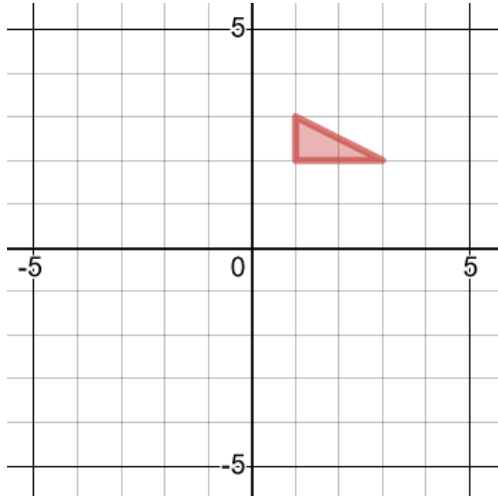


Worked Example

Reflect in the line $y = 1$

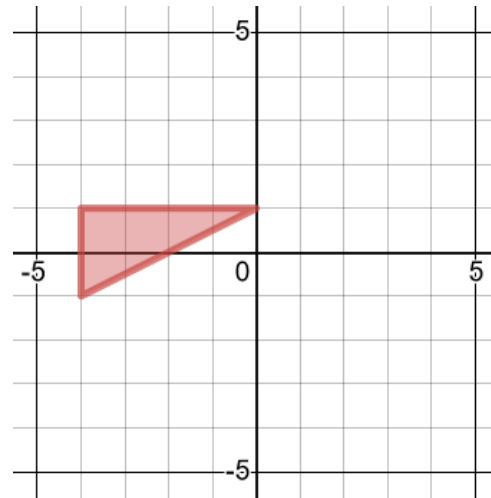


Reflect in the line $x = 3$

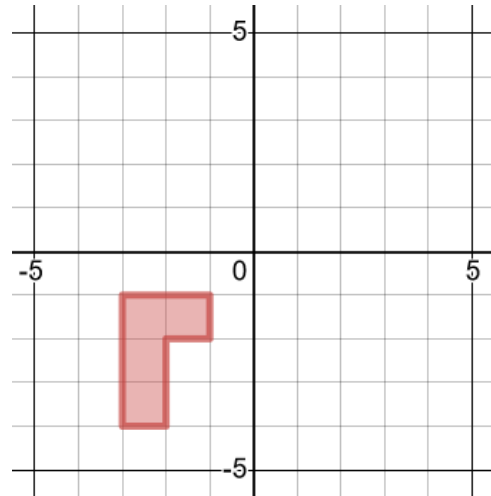


Your Turn

Reflect in the line $y = 2$

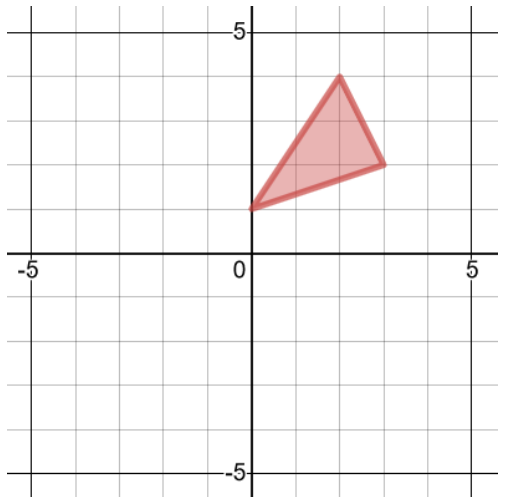
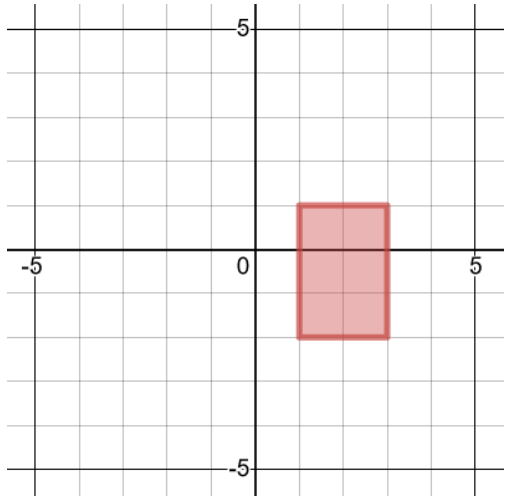


Reflect in the line $x = 1$



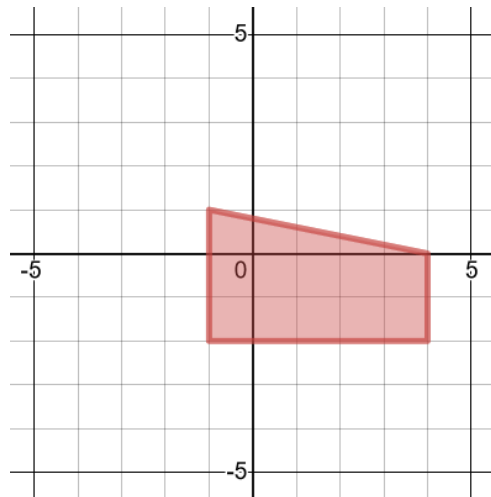
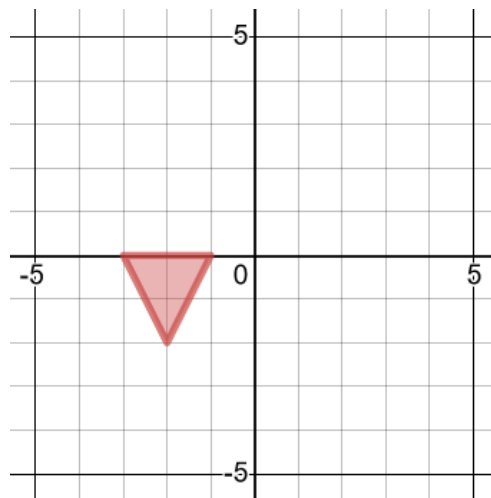
Worked Example

Reflect in the line $y = x$



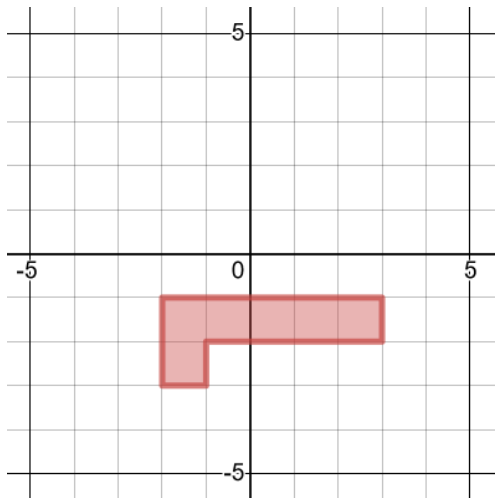
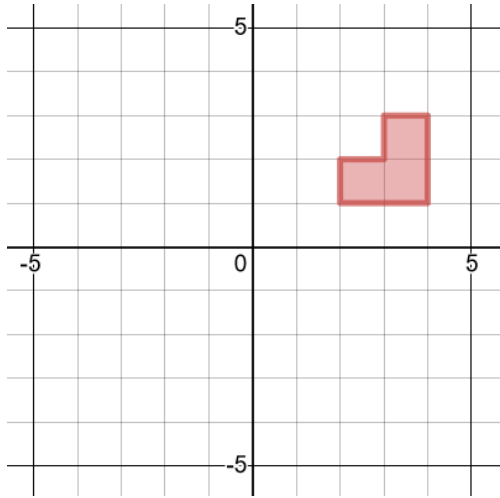
Your Turn

Reflect in the line $y = x$



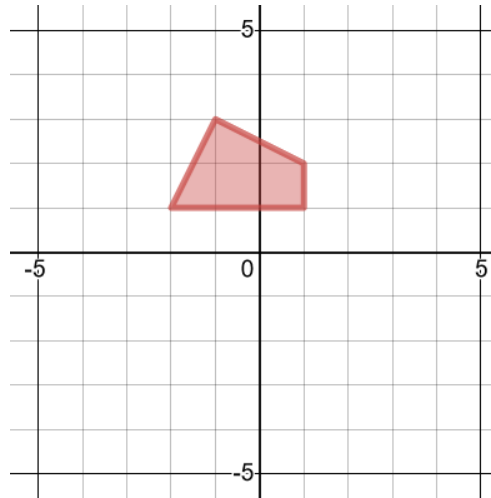
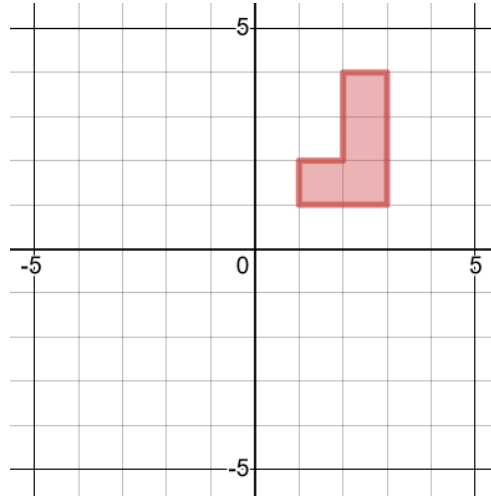
Worked Example

Reflect in the line $y = -x$



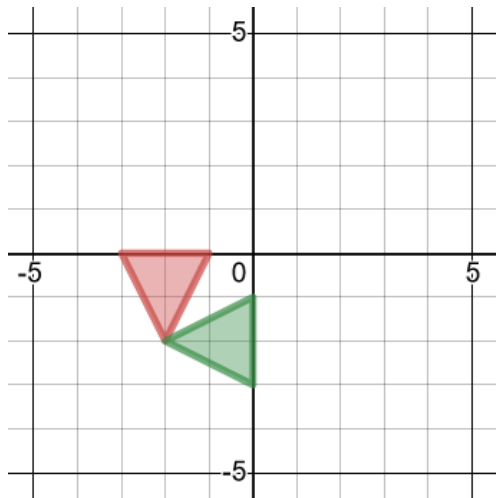
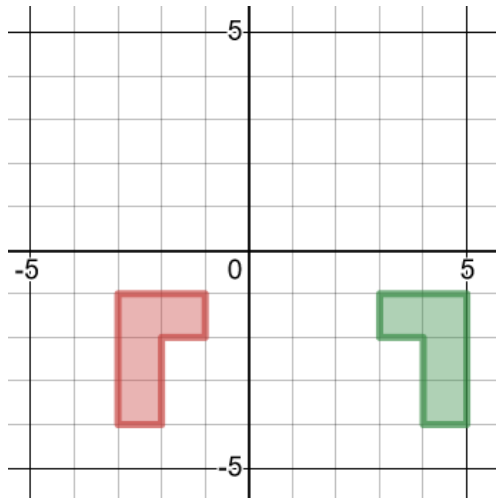
Your Turn

Reflect in the line $y = -x$



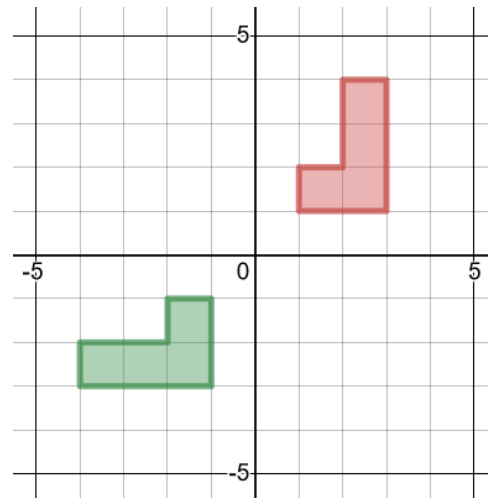
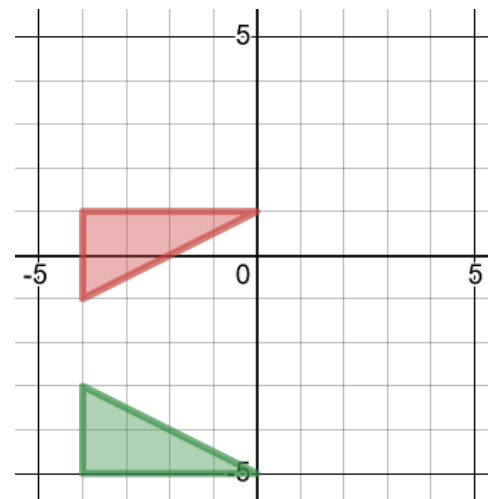
Worked Example

Describe the single transformation of the red object onto the green image



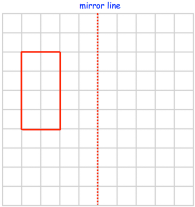
Your Turn

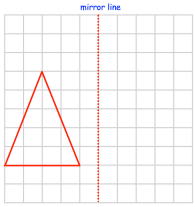
Describe the single transformation of the red object onto the green image

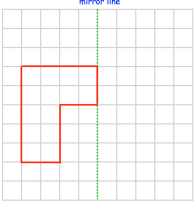


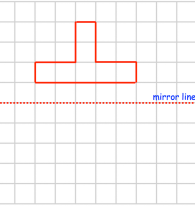
Fluency Practice

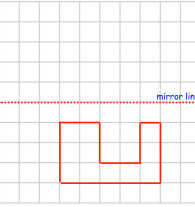
Question 1: Reflect each shape in the mirror line given

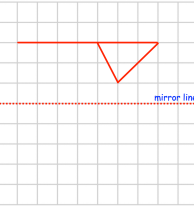
(a) 

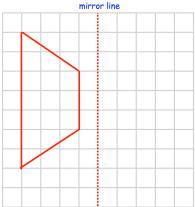
(b) 

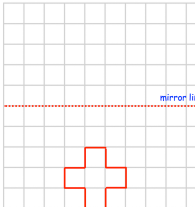
(c) 

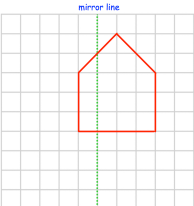
(d) 

(e) 

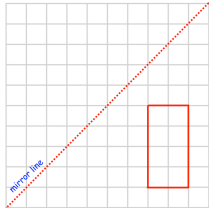
(f) 

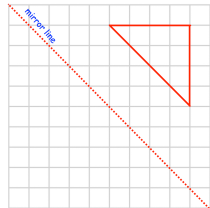
(g) 

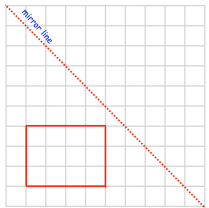
(h) 

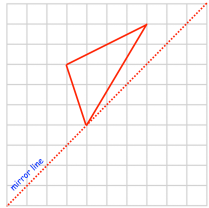
(i) 

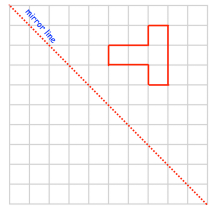
Question 2: Reflect each shape in the mirror line given

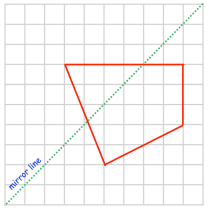
(a) 

(b) 

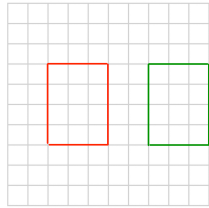
(c) 

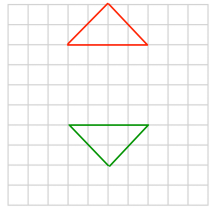
(d) 


(e) 

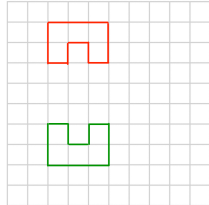
(f) 

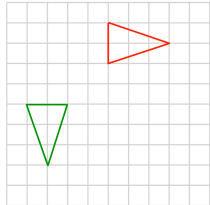
Question 3: Find the mirror line for each of the reflections below.

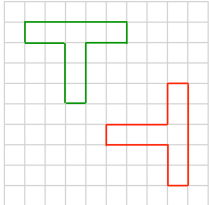
(a) 

(b) 

(c) 

(d) 

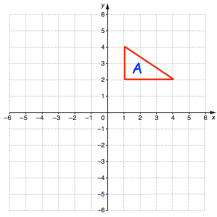
(e) 

(f) 

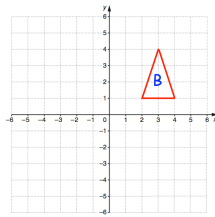
Fluency Practice

Question 4:

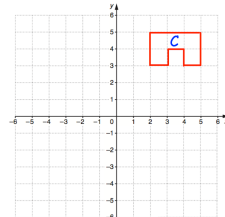
(a) Reflect triangle A in the x-axis



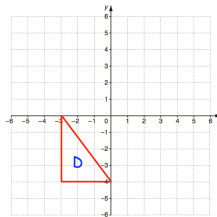
(b) Reflect triangle B in the y-axis



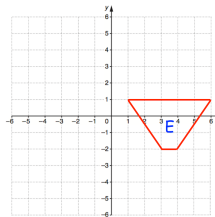
(c) Reflect shape C in the x-axis



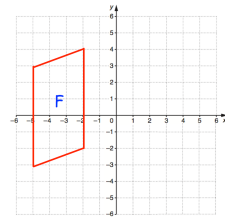
(d) Reflect shape D in the y-axis



(e) Reflect shape E in the y-axis

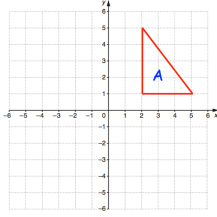


(f) Reflect shape F in the x-axis

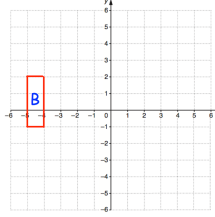


Question 5:

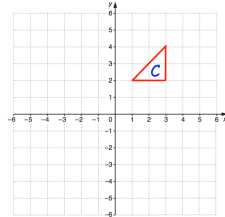
(a) Reflect shape A in the line $x = 1$



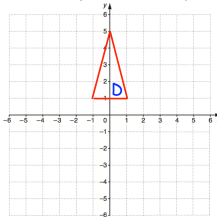
(b) Reflect shape B in the line $x = -2$



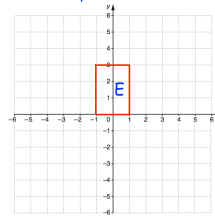
(c) Reflect shape C in the line $y = -1$



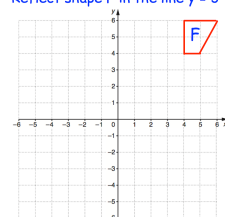
(d) Reflect shape D in the line $y = 2$



(e) Reflect shape E in the line $x = -1$

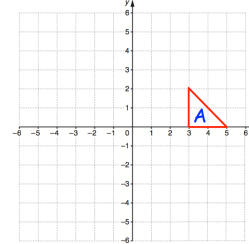


(f) Reflect shape F in the line $y = 3$

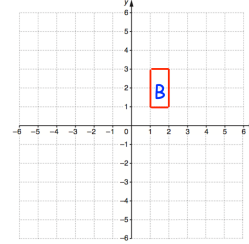


Question 6:

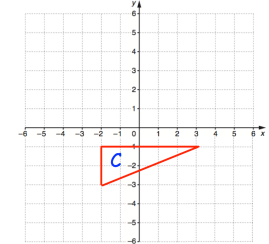
(a) Reflect shape A in the line $y = x$



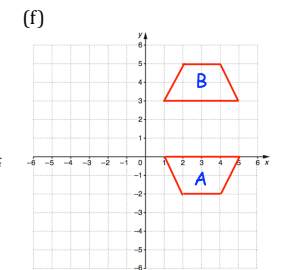
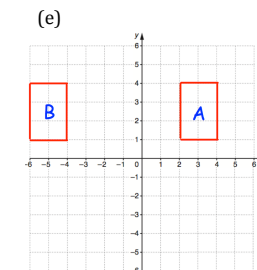
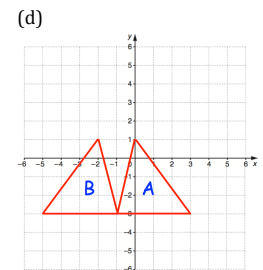
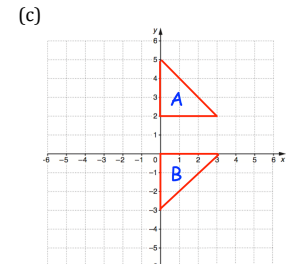
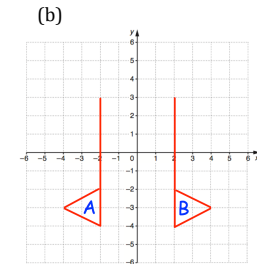
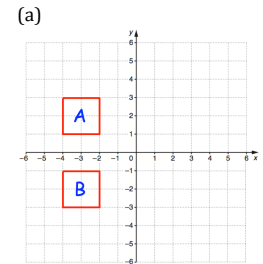
(b) Reflect shape B in the line $y = -x$



(c) Reflect shape C in the line $y = x$

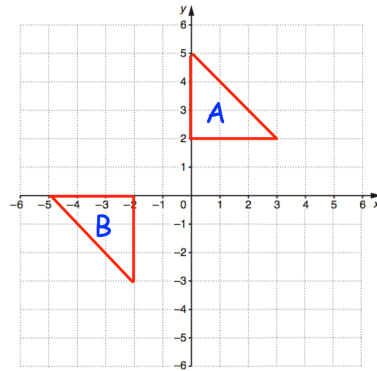


Question 7: Describe fully the single transformation that takes shape A to shape B.



Fluency Practice

(g)



(h)

