



KING EDWARD VI
HANDSWORTH GRAMMAR
SCHOOL FOR BOYS



KING EDWARD VI
ACADEMY TRUST
BIRMINGHAM

Year 11

2024 Mathematics 2025

Unit 25 Booklet – Part 1

HGS Maths



Tasks



Dr Frost Course



Name: _____

Class: _____



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1 Exponential and Trigonometric Graphs

Exponential Graphs

Worked Example

Some money M has been invested in a bank. The value of the money after t years is modelled by the function

$$M(t) = 1750 \times (1.02)^t$$

State the initial amount of money invested.

Your Turn

Some money M has been invested in a bank. The value of the money after t years is modelled by the function

$$M(t) = 3000 \times (1.005)^t$$

State the initial amount of money invested.

Worked Example

Some money M has been invested in a bank. The value of the money after t years is modelled by the function

$$M(t) = 500 \times (1.04)^t$$

Determine the interest rate offered by the bank.

Your Turn

Some money M has been invested in a bank. The value of the money after t years is modelled by the function

$$M(t) = 1250 \times (1.025)^t$$

Determine the interest rate offered by the bank.

Worked Example

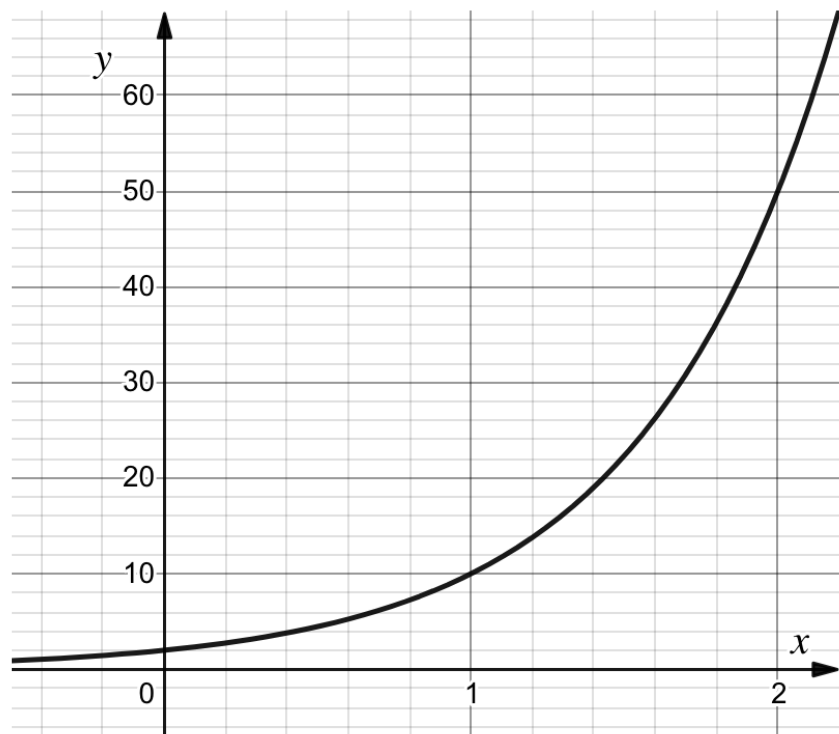
The sketch graph shows a curve with equation $y = ab^x$
The curve passes through the points (0, 3.25) and (3, 87.75).
Calculate the value of a and the value of b .

Your Turn

The sketch graph shows a curve with equation $y = ab^x$
The curve passes through the points (0, 2.75) and (2, 68.75).
Calculate the value of a and the value of b .

Worked Example

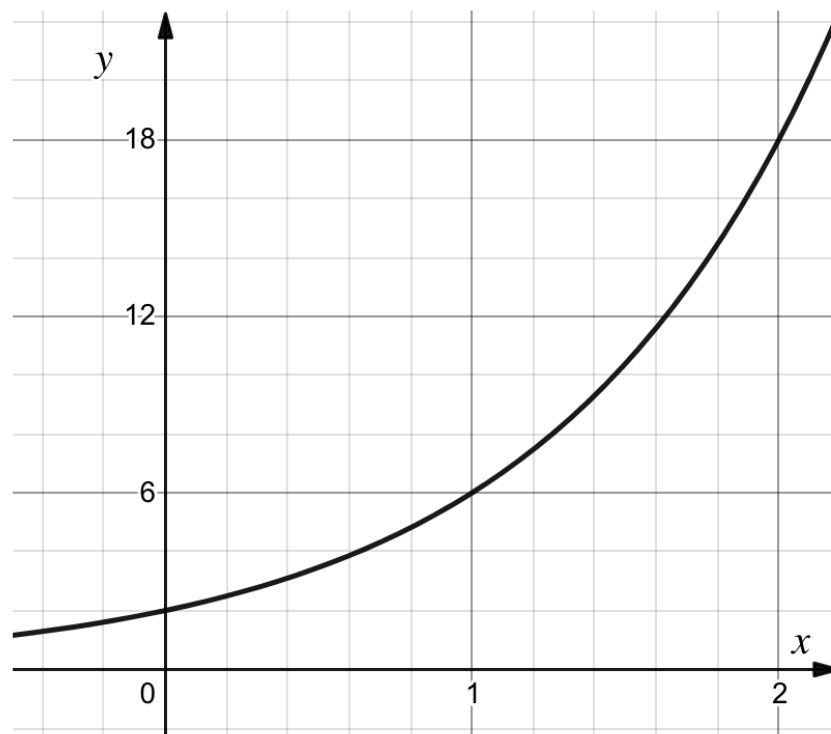
This graph shows a curve with equation $y = pq^x$



Calculate the value of p and q .

Your Turn

This graph shows a curve with equation $y = pq^x$



Calculate the value of p and q .

Worked Example

At the start of an experiment, a petri dish contained 4,000,000 bacteria. After 4 days, there were 6,000,000 bacteria. It is assumed that the number of bacteria is given by the formula $N = ar^t$ where N is the number of bacteria, t days after the start of the experiment. Calculate the number of bacteria 7 days after the start of the experiment, giving your answer to 3 significant figures.

Your Turn

At the start of an experiment, a petri dish contained 4,000,000 bacteria. After 5 days, there were 13,000,000 bacteria. It is assumed that the number of bacteria is given by the formula $N = ar^t$ where N is the number of bacteria, t days after the start of the experiment. Calculate the number of bacteria 11 days after the start of the experiment, giving your answer to 3 significant figures.

Trigonometric Graphs

Angle (θ Degrees)	0°	30°	45°	60°	90°	180°	270°	360°
$\sin(\theta)$								
$\cos(\theta)$								
$\tan(\theta)$								

Worked Example

Sketch the graph $y = \sin(x)$ for $-360^\circ \leq x \leq 360^\circ$

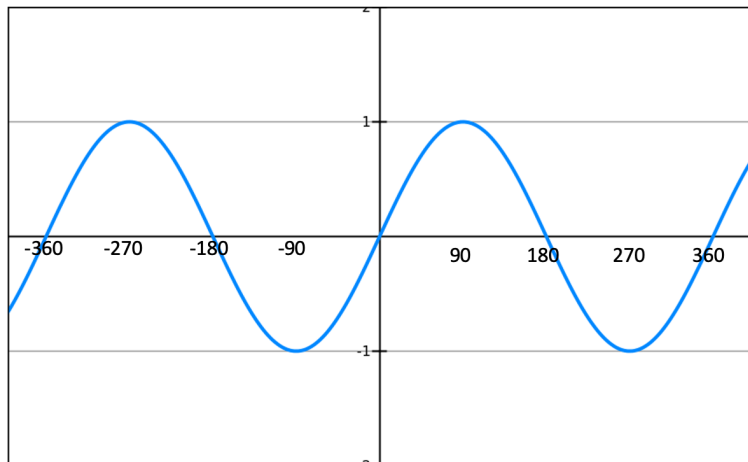
Worked Example

Sketch the graph $y = \cos(x)$ for $-360^\circ \leq x \leq 360^\circ$

Worked Example

Sketch the graph $y = \tan(x)$ for $-360^\circ \leq x \leq 360^\circ$

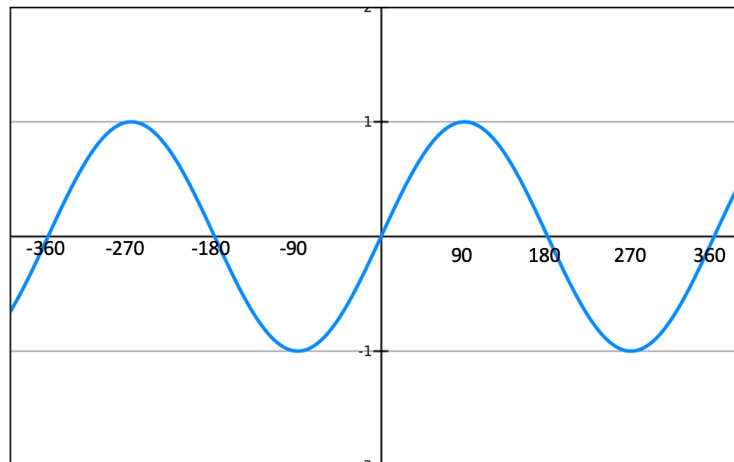
Worked Example



Suppose we know that $\sin(30) = 0.5$. By thinking about symmetry in the graph, work out:

- a) $\sin(150) =$
- b) $\sin(-30) =$
- c) $\sin(210) =$

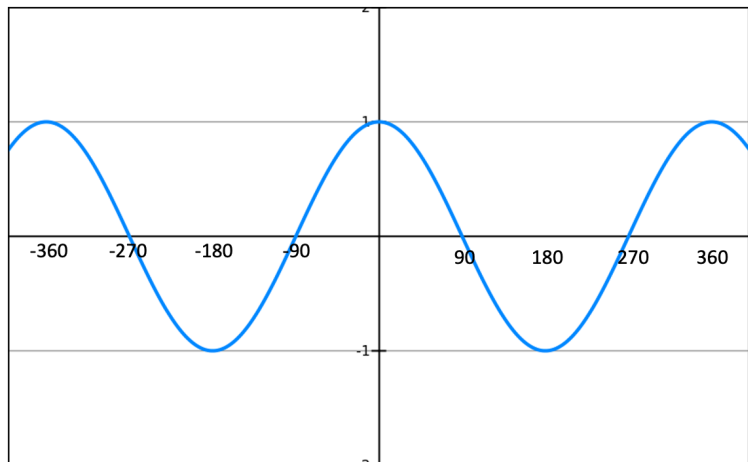
Your Turn



Suppose we know that $\sin(60) = \frac{\sqrt{3}}{2}$. By thinking about symmetry in the graph, work out:

- a) $\sin(240) =$
- b) $\sin(120) =$
- c) $\sin(-60) =$

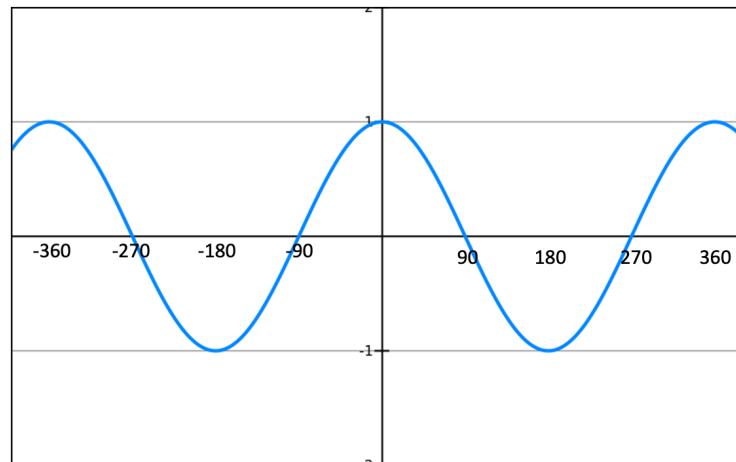
Worked Example



Suppose we know that $\cos(60) = 0.5$. By thinking about symmetry in the graph, work out:

- a) $\cos(120) =$
- b) $\cos(-60) =$
- c) $\cos(240) =$

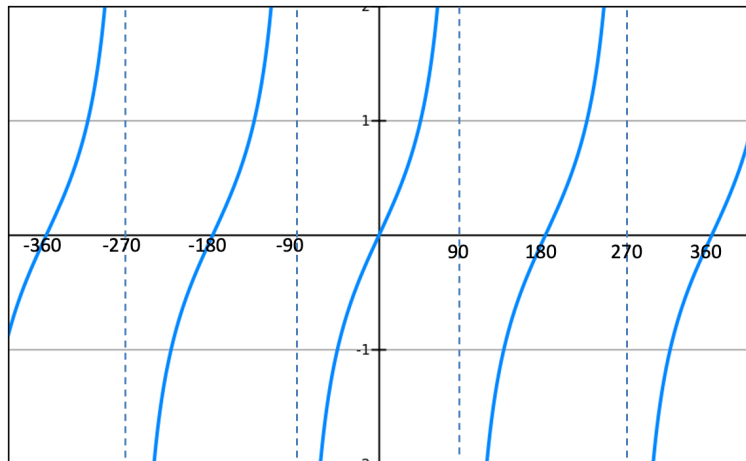
Your Turn



Suppose we know that $\cos(30) = \frac{\sqrt{3}}{2}$. By thinking about symmetry in the graph, work out:

- a) $\cos(-30) =$
- b) $\cos(210) =$
- c) $\cos(150) =$

Worked Example

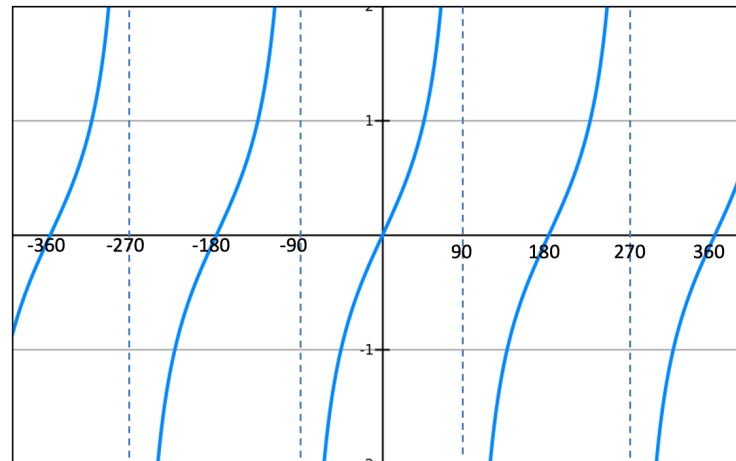


Suppose we know that $\tan(30) = \frac{1}{\sqrt{3}}$. By thinking about symmetry in the graph, work out:

a) $\tan(-30) =$

b) $\tan(150) =$

Your Turn



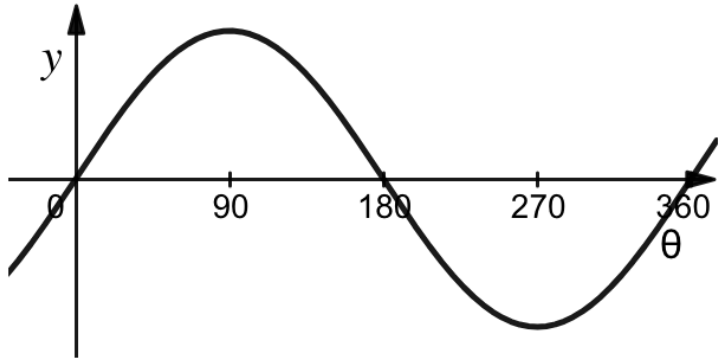
Suppose we know that $\tan(60) = \sqrt{3}$. By thinking about symmetry in the graph, work out:

a) $\tan(120) =$

b) $\tan(-60) =$

Worked Example

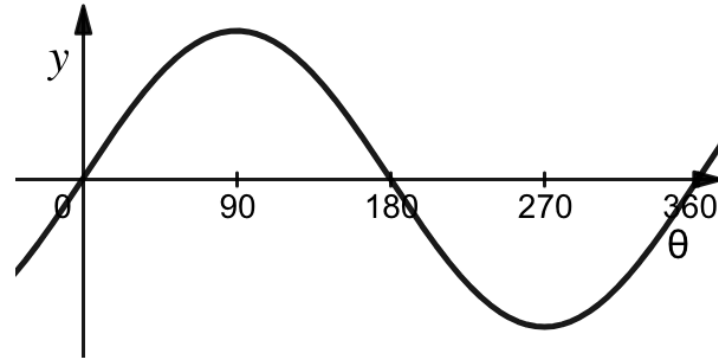
Here is a graph of $y = \sin \theta$ for $0^\circ \leq \theta \leq 360^\circ$.



Solve $\sin \theta = -0.8$ for $0^\circ \leq \theta \leq 360^\circ$.
Give your solutions correct to 2 decimal places.

Your Turn

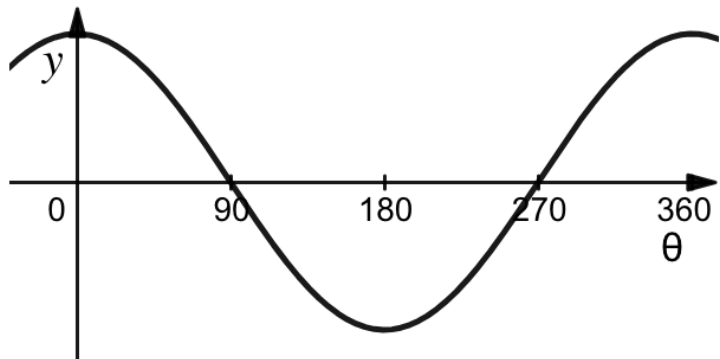
Here is a graph of $y = \sin \theta$ for $0^\circ \leq \theta \leq 360^\circ$.



Solve $\sin \theta = 0.3$ for $0^\circ \leq \theta \leq 360^\circ$.
Give your solutions correct to 2 decimal places.

Worked Example

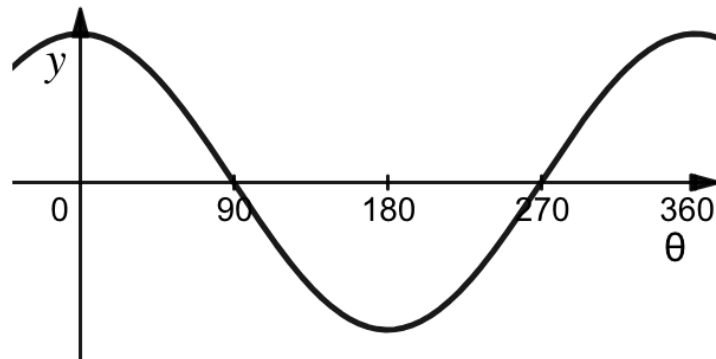
Here is a graph of $y = \cos \theta$ for $0^\circ \leq \theta \leq 360^\circ$.



Solve $\cos \theta = 0.7$ for $0^\circ \leq \theta \leq 360^\circ$.
Give your solutions correct to 2 decimal places.

Your Turn

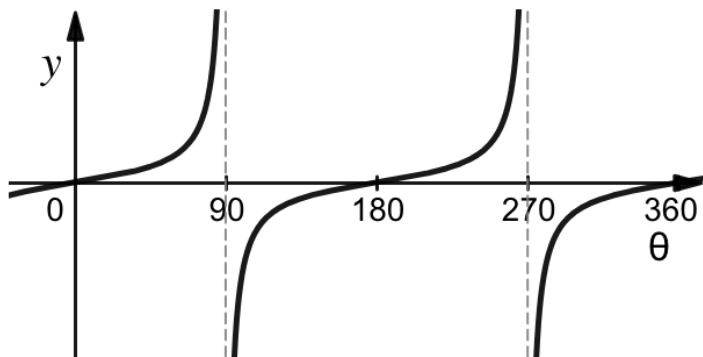
Here is a graph of $y = \cos \theta$ for $0^\circ \leq \theta \leq 360^\circ$.



Solve $\cos \theta = -0.2$ for $0^\circ \leq \theta \leq 360^\circ$.
Give your solutions correct to 2 decimal places.

Worked Example

Here is a graph of $y = \tan \theta$ for $0^\circ \leq \theta \leq 360^\circ$.

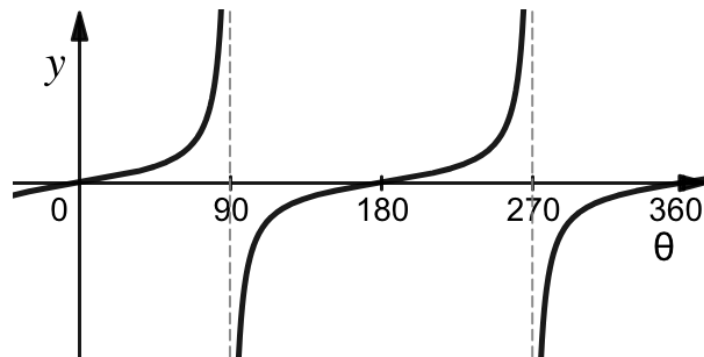


Solve $\tan \theta = -7$ for $0^\circ \leq \theta \leq 360^\circ$.

Give your solutions correct to 2 decimal places.

Your Turn

Here is a graph of $y = \tan \theta$ for $0^\circ \leq \theta \leq 360^\circ$.

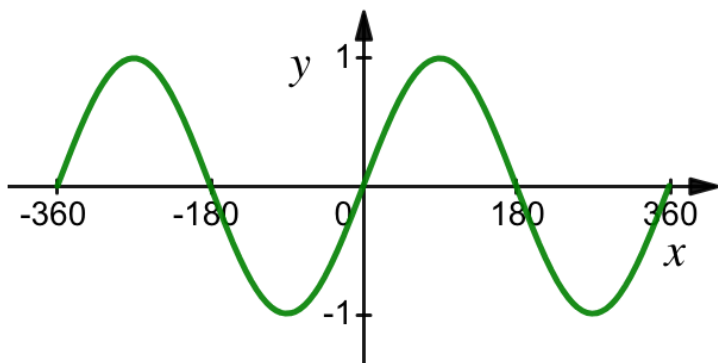


Solve $\tan \theta = 6$ for $0^\circ \leq \theta \leq 360^\circ$.

Give your solutions correct to 2 decimal places.

Worked Example

Here is the graph of $y = \sin x$ for the interval $-360 \leq x \leq 360^\circ$.



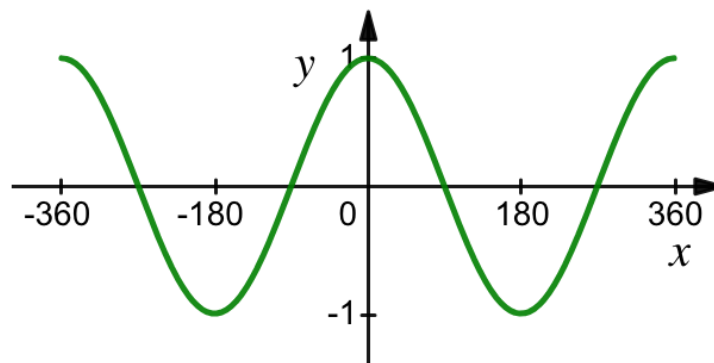
$x = 203.6$ is a solution to the equation $\sin x = -0.4$

Use the graph to find the other solutions to the equation in the interval $-360 \leq x \leq 360^\circ$.

Give your solutions to one decimal place.

Your Turn

Here is the graph of $y = \cos x$ for the interval $-360 \leq x \leq 360^\circ$.



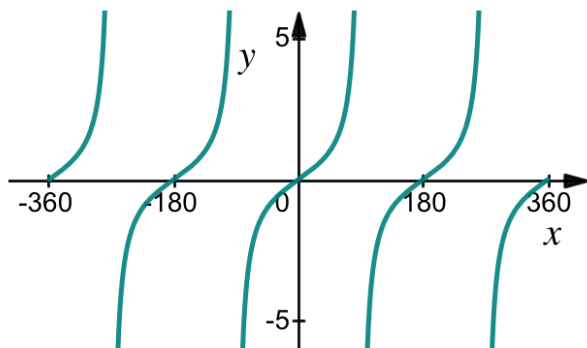
$x = 107.5$ is a solution to the equation $\cos x = -0.3$

Use the graph to find the other solutions to the equation in the interval $-360 \leq x \leq 360^\circ$.

Give your solutions to one decimal place.

Worked Example

Here is the graph of $y = \tan x$ for the interval $-360 \leq x \leq 360^\circ$.



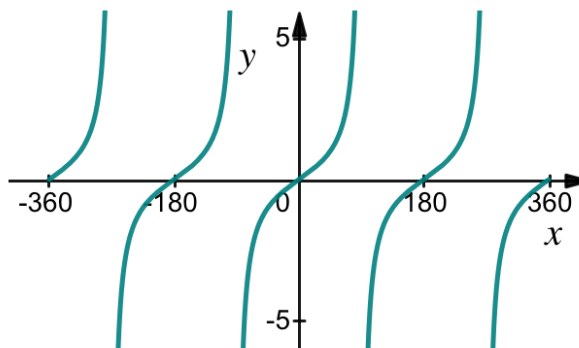
$x = 105.95$ is a solution to the equation $\tan x = -3.5$

Use the graph to find the other solutions to the equation in the interval $-360 \leq x \leq 360^\circ$.

Give your solutions to two decimal places.

Your Turn

Here is the graph of $y = \tan x$ for the interval $-360 \leq x \leq 360^\circ$.



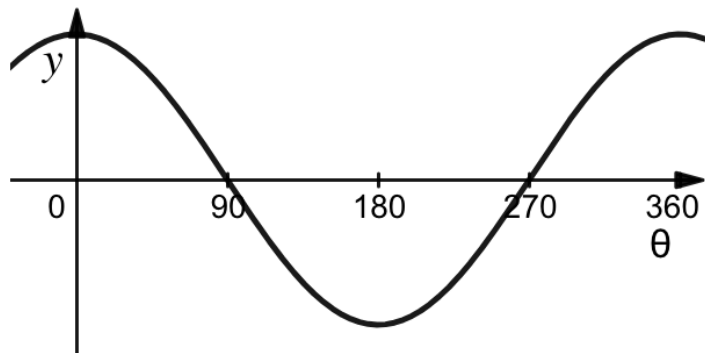
$x = 56.31$ is a solution to the equation $\tan x = 1.5$

Use the graph to find the other solutions to the equation in the interval $-360 \leq x \leq 360^\circ$.

Give your solutions to two decimal places.

Worked Example

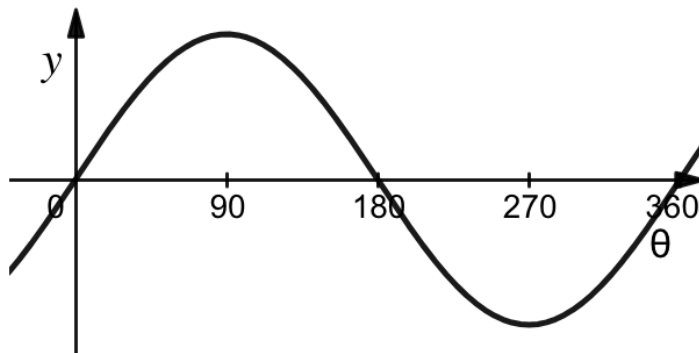
Here is a graph of $y = \cos \theta$ for $0^\circ \leq \theta \leq 360^\circ$.



Solve $\cos \theta = -0.4$ for $0^\circ \leq \theta \leq 720^\circ$.
Give your solutions correct to 2 decimal places.

Your Turn

Here is a graph of $y = \sin \theta$ for $0^\circ \leq \theta \leq 360^\circ$.



Solve $\sin \theta = -0.7$ for $0^\circ \leq \theta \leq 720^\circ$.
Give your solutions correct to 2 decimal places.

Extra Notes

2 Trigonometric Identities and Equations (L2FM Only)

Trigonometric Identities

Worked Example

It is given that α is acute and that $\cos \alpha = \frac{2}{3}$
Find the exact value of $\tan \alpha$

Your Turn

It is given that α is acute and that $\sin \alpha = \frac{4}{5}$
Find the exact value of $\tan \alpha$

Worked Example

Prove that $1 - \frac{\tan \theta \cos^3 \theta}{\sin \theta} \equiv \sin^2 \theta$

Your Turn

Prove that $1 - \tan \theta \sin \theta \cos \theta \equiv \cos^2 \theta$

Worked Example

Prove that $\tan \theta - \frac{1}{\tan \theta} \equiv \frac{1-2 \cos^2 \theta}{\sin \theta \cos \theta}$

Your Turn

Prove that $\tan \theta + \frac{1}{\tan \theta} \equiv \frac{1}{\sin \theta \cos \theta}$

Worked Example

Prove that $\frac{\cos \theta - \cos^3 \theta}{\sin^3 \theta} \equiv \frac{1}{\tan \theta}$

Your Turn

Prove that $\frac{\sin \theta - \sin^3 \theta}{\cos^3 \theta} \equiv \tan \theta$

Worked Example

Prove that $\frac{\sin^4 \theta - \cos^4 \theta}{\sin^2 \theta} \equiv 1 - \frac{1}{\tan^2 \theta}$

Your Turn

Prove that $\frac{\cos^4 \theta - \sin^4 \theta}{\cos^2 \theta} \equiv 1 - \tan^2 \theta$

Worked Example

Prove that $\frac{\frac{\sin x}{\tan x}}{\sqrt{1-\sin^2 x}} \equiv 1$

Your Turn

Prove that $\frac{\tan x \cos x}{\sqrt{1-\cos^2 x}} \equiv 1$

Worked Example

Prove that $\frac{1}{\tan^2 \theta} \equiv \frac{1}{\sin^2 \theta} - 1$

Your Turn

Prove that $\tan^2 \theta \equiv \frac{1}{\cos^2 \theta} - 1$

Trigonometric Equations

Worked Example

Solve $\cos x = -0.8$ in the interval $-180^\circ \leq x \leq 540^\circ$
Give your solution(s) correct to 1 decimal place where appropriate.

Your Turn

Solve $\sin x = -0.4$ in the interval $-180^\circ \leq \theta \leq 360^\circ$
Give your solution(s) correct to 1 decimal place where appropriate.

Worked Example

Solve $\tan x = 0.4$ in the interval $-180^\circ \leq x \leq 180^\circ$
Give your solution(s) correct to 1 decimal place where appropriate.

Your Turn

Solve $\tan x = -0.4$ in the interval $-180^\circ \leq x \leq 180^\circ$
Give your solution(s) correct to 1 decimal place where appropriate.

Worked Example

Solve $\sin^2 x = 0.53$ in the interval $-180^\circ \leq x \leq 360^\circ$
Give your solution(s) correct to 1 decimal place where appropriate.

Your Turn

Solve $\cos^2 x = 0.62$ in the interval $-180^\circ \leq \theta \leq 360^\circ$
Give your solution(s) correct to 1 decimal place where appropriate.

Worked Example

Solve $8 \tan^2 x = -6 \tan x - 1$ in the interval $0^\circ < x < 540^\circ$
Give your solution(s) correct to 1 decimal place where appropriate.

Your Turn

Solve $12 \tan^2 x - \tan x = 1$ in the interval $0^\circ < x < 540^\circ$
Give your solution(s) correct to 1 decimal place where appropriate.

Worked Example

Solve $6 \sin^2 x - 5 \cos x = 2$ in the interval $0^\circ \leq x < 540^\circ$
Give your solution(s) correct to 2 decimal places where appropriate.

Your Turn

Solve $8 \cos^2 x = 2 \sin x + 5$ in the interval $0^\circ \leq x < 540^\circ$
Give your solution(s) correct to 2 decimal places where appropriate.

Extra Notes

3 Domain and Range (L2FM Only)

Worked Example

$$f(x) = 3x^2 - 2$$

The domain of $f(x)$ is $\{1, 2, 3, 4\}$.

What is the range?

Your Turn

$$g(x) = 2x^3 + 1$$

The domain of $g(x)$ is $\{1, 2, 3, 4\}$.

What is the range?

Worked Example

- a) Work out a suitable domain and the range of $f(x) = x^2$
- b) Work out a suitable domain and the range of $f(x) = \sqrt{x}$

Your Turn

- a) Work out a suitable domain and the range of $f(x) = x^3$
- b) Work out a suitable domain and the range of $f(x) = \sqrt[3]{x}$

Worked Example

$$f(x) = \frac{x - 3}{5x - 6}$$

State the value of x that cannot be in the domain of $f(x)$

Your Turn

$$f(x) = \frac{3 - x}{6x - 5}$$

State the value of x that cannot be in the domain of $f(x)$

Worked Example

$g(x) = x^2 - 6x + 5, x \in \mathbb{R}$
Determine the range of $g(x)$

Your Turn

$f(x) = x^2 - 4x + 7, x \in \mathbb{R}$
Determine the range of $f(x)$

Worked Example	Your Turn
<p data-bbox="58 125 503 168">$g(x) = 3x^2 - 2x + 4, x \in \mathbb{R}$</p> <p data-bbox="58 175 493 218">Determine the range of $g(x)$</p>	<p data-bbox="1058 125 1504 168">$f(x) = 2x^2 + 7x - 7, x \in \mathbb{R}$</p> <p data-bbox="1058 175 1493 218">Determine the range of $f(x)$</p>

Worked Example

$g(x) = 14 + 2x - x^2, x \in \mathbb{R}$
Determine the range of $g(x)$

Your Turn

$f(x) = 21 + 4x - x^2, x \in \mathbb{R}$
Determine the range of $f(x)$

Worked Example

$f(x)$ is a function with domain all values of x
 $f(x) = \sqrt{x^2 + 12x - a}$ where a is a constant
Work out the possible values of a

Your Turn

$f(x)$ is a function with domain all values of x
 $f(x) = \sqrt{x^2 + 6x - a}$ where a is a constant
Work out the possible values of a

Worked Example	Your Turn
$g(x) = x^2 + 6x + 5, x \geq 2$ Determine the range of $g(x)$	$f(x) = x^2 + 4x + 3, x \geq 1$ Determine the range of $f(x)$

Worked Example

$f(x) = 23 - 5x$ with domain $-3 < x \leq 1$
Work out the range of $f(x)$

Your Turn

$g(x) = 32 - 3x$ with domain $-5 \leq x < 2$
Work out the range of $g(x)$

Worked Example

Determine the range of:

$$g(x) = \sin x, 180 \leq x < 360^\circ$$

Your Turn

Determine the range of:

$$f(x) = \cos x, 180 < x \leq 360^\circ$$

Worked Example

$$g(x) = \frac{8x-2}{x-1}, x \geq 7$$

Work out the range of g

Your Turn

$$f(x) = \frac{5x+3}{x-4}, x \geq 5$$

Work out the range of f

Worked Example	Your Turn
<p>$g(x)$ is an increasing function with domain $1 \leq x \leq 5$ and range $3 \leq g(x) \leq 11$. Construct a suitable function.</p>	<p>$f(x)$ is a decreasing function with domain $4 \leq x \leq 6$ and range $7 \leq f(x) \leq 19$. Construct a suitable function.</p>

Extra Notes

4 Piecewise Functions (L2FM Only)

Worked Example

$$f(x) = \begin{cases} x^2 + 4, & -8 \leq x \leq 0 \\ 3x + 4, & 0 < x \leq 7 \end{cases}$$

Work out the value of $f(-3)$

Your Turn

$$f(x) = \begin{cases} x^2 + 1, & 0 \leq x \leq 3 \\ 2x + 4, & 3 < x \leq 8 \end{cases}$$

Work out the value of $f(7)$

Worked Example

$$f(x) = \begin{cases} (x-2)^2 + 1, & 0 \leq x < 3 \\ \frac{1}{4}x + \frac{5}{4}, & 3 \leq x \leq 7 \end{cases}$$

Sketch the graph of $y = f(x)$

Your Turn

$$f(x) = \begin{cases} (x-1)^2 + 2, & 0 \leq x < 2 \\ \frac{1}{3}x + \frac{7}{3}, & 2 \leq x \leq 5 \end{cases}$$

Sketch the graph of $y = f(x)$

Worked Example

$$f(x) = \begin{cases} 3, & 0 \leq x < 1 \\ x^2 + 2, & 1 \leq x < 2 \\ 8 - x, & 2 \leq x < 3 \end{cases}$$

Sketch the graph of $y = f(x)$

Your Turn

$$f(x) = \begin{cases} x^2, & 0 \leq x < 1 \\ 1, & 1 \leq x < 2 \\ 3 - x, & 2 \leq x < 3 \end{cases}$$

Sketch the graph of $y = f(x)$

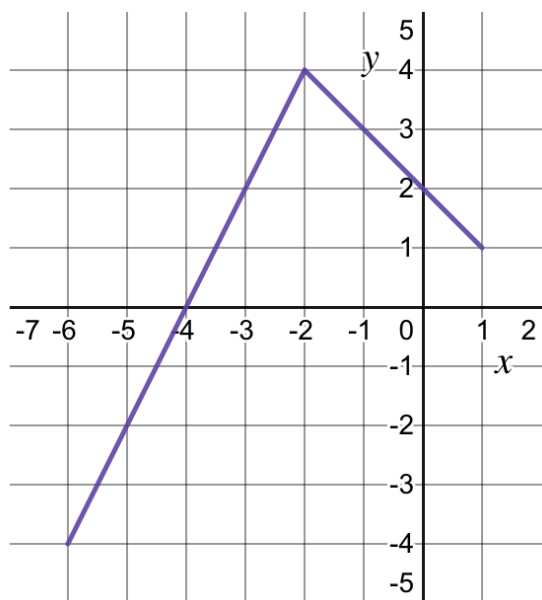
Worked Example

The function $f(x)$ is defined as

$$f(x) = \begin{cases} p, & -6 \leq x \leq -2 \\ q, & -2 < x \leq 1 \end{cases}$$

where p and q are unknown expressions.

The graph of $y = f(x)$ is shown below.



Find the expressions represented by p and q .

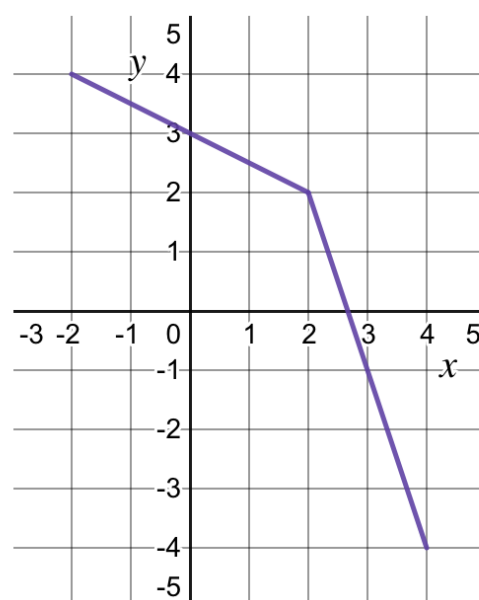
Your Turn

The function $f(x)$ is defined as

$$f(x) = \begin{cases} p, & -2 \leq x \leq 2 \\ q, & 2 < x \leq 4 \end{cases}$$

where p and q are unknown expressions.

The graph of $y = f(x)$ is shown below.



Find the expressions represented by p and q .

Worked Example

$$f(x) = \begin{cases} (x - a)^2 + b, & 0 \leq x < 3 \\ cx + d, & 3 \leq x \leq 7 \end{cases}$$

The graph of $y = f(x)$ passes through the points $(0, 5)$, $(2, 1)$, $(3, 2)$ and $(7, 3)$

Find the values of a , b , c and d

Your Turn

$$f(x) = \begin{cases} (x - a)^2 + b, & 0 \leq x < 2 \\ cx + d, & 2 \leq x \leq 5 \end{cases}$$

The graph of $y = f(x)$ passes through the points $(0, 3)$, $(1, 2)$, $(2, 3)$ and $(5, 3)$

Find the values of a , b , c and d

Worked Example

The function $f(x)$ is defined as

$$f(x) = \begin{cases} x^2 + 7, & -2 \leq x \leq 2 \\ 15 - 2x, & 2 < x \leq 7 \end{cases}$$

Solve $f(x) = 8$

Your Turn

The function $f(x)$ is defined as

$$f(x) = \begin{cases} -2x - 10, & -4 \leq x \leq -2 \\ -x^2 - 2, & -2 < x \leq 2 \end{cases}$$

Solve $f(x) = -3$

Worked Example

The function $f(x)$ is defined for all x :

$$f(x) = \begin{cases} 9, & x < -3 \\ x^2, & -3 \leq x \leq 3 \\ 15 - 2x, & x > 3 \end{cases}$$

Determine the range of $f(x)$

Your Turn

The function $f(x)$ is defined for all x :

$$f(x) = \begin{cases} 4, & x < -2 \\ x^2, & -2 \leq x \leq 2 \\ 12 - 4x, & x > 2 \end{cases}$$

Determine the range of $f(x)$

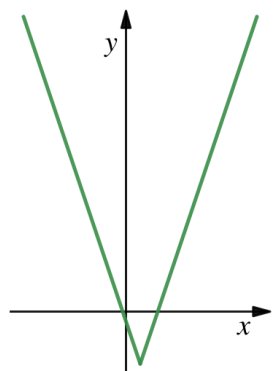
Worked Example

The function $f(x)$ is defined as

$$f(x) = \begin{cases} p, & -7 \leq x \leq 1 \\ q, & 1 < x \leq 9 \end{cases}$$

where p and q are unknown expressions.

The graph of $y = f(x)$ is shown below.



The graph is symmetrical about $x = 1$.

The range of $f(x)$ is $-6 \leq f(x) \leq 34$.

Find the expressions represented by p and q .

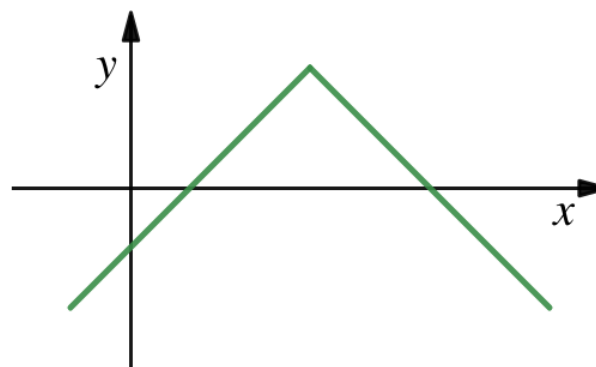
Your Turn

The function $f(x)$ is defined as

$$f(x) = \begin{cases} p, & -1 \leq x \leq 3 \\ q, & 3 < x \leq 7 \end{cases}$$

where p and q are unknown expressions.

The graph of $y = f(x)$ is shown below.



The graph is symmetrical about $x = 3$.

The range of $f(x)$ is $-2 \leq f(x) \leq 2$.

Find the expressions represented by p and q .

Worked Example

The function $f(x)$ is defined as

$$f(x) = \begin{cases} 2, & 0 \leq x \leq 5 \\ 2x - 8, & 5 < x \leq 7 \\ 27 - 3x, & 7 < x \leq 9 \end{cases}$$

Find the area enclosed by the graph of $y = f(x)$, the y -axis and the x -axis.

Your Turn

The function $f(x)$ is defined as

$$f(x) = \begin{cases} 2, & 0 \leq x \leq 5 \\ x - 3, & 5 < x \leq 8 \\ 45 - 5x, & 8 < x \leq 9 \end{cases}$$

Find the area enclosed by the graph of $y = f(x)$, the y -axis and the x -axis.

Extra Notes

5 Graph Transformations

Worked Example

The point $A(2, 5)$ is on the graph of $y = f(x)$. Write the new coordinates of A after the transformation:

- a) $y = f(x) + 3$
- b) $y = f(x + 3)$
- c) $y = -f(x)$
- d) $y = f(-x)$
- e) $y = -f(x) + 3$
- f) $y = f(-x) + 3$

Your Turn

The point $A(3, 4)$ is on the graph of $y = f(x)$. Write the new coordinates of A after the transformation:

- a) $y = f(x) - 4$
- b) $y = f(x - 4)$
- c) $y = f(-x)$
- d) $y = -f(x)$
- e) $y = -f(x) - 6$
- f) $y = -f(-x) - 6$

Worked Example

Sketch $y = \cos x + 1$, $0 \leq x \leq 360^\circ$

Your Turn

Sketch $y = \sin x - 2$, $0 \leq x \leq 360^\circ$

Worked Example

Sketch $y = \sin(x - 45^\circ)$, $0 \leq x \leq 360^\circ$

Your Turn

Sketch $y = \cos(x + 45^\circ)$, $0 \leq x \leq 360^\circ$

Worked Example

Sketch $y = -\sin x$, $0 \leq x \leq 360^\circ$

Your Turn

Sketch $y = -\tan x$, $0 \leq x \leq 360^\circ$

Worked Example

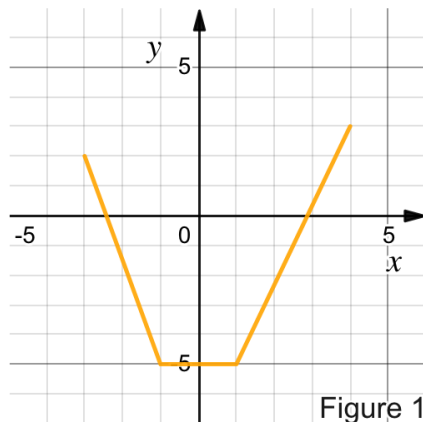
Sketch $y = \cos(-x)$, $0 \leq x \leq 360^\circ$

Your Turn

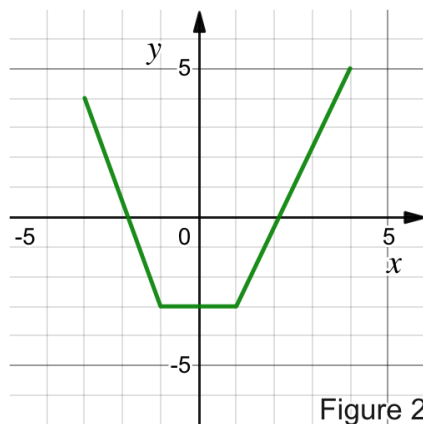
Sketch $y = \tan(-x)$, $0 \leq x \leq 360^\circ$

Worked Example

The graph of $y = f(x)$ is shown in Figure 1.



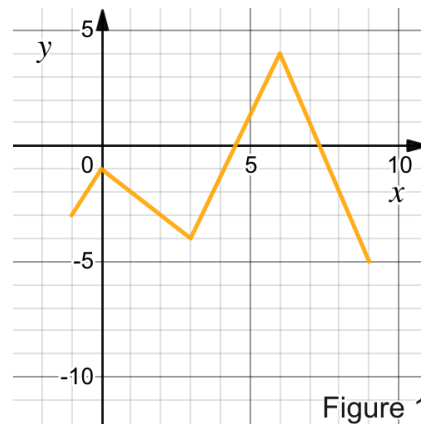
The graph of $y = f(x) + a$ is shown in Figure 2.



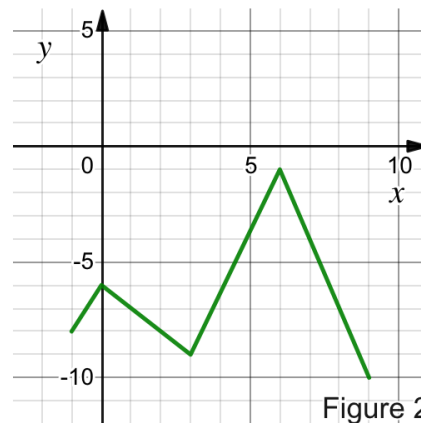
Determine the value of a .

Your Turn

The graph of $y = f(x)$ is shown in Figure 1.



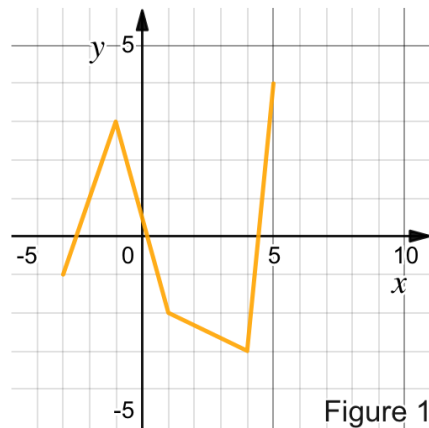
The graph of $y = f(x) + a$ is shown in Figure 2.



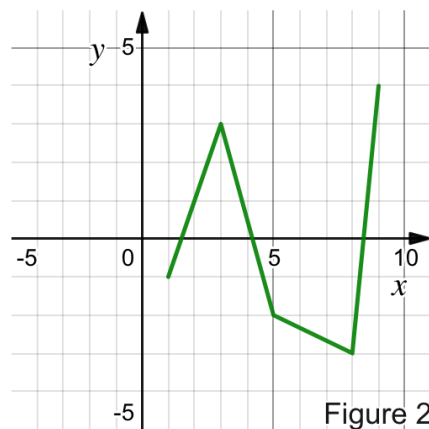
Determine the value of a .

Worked Example

The graph of $y = f(x)$ is shown in Figure 1.



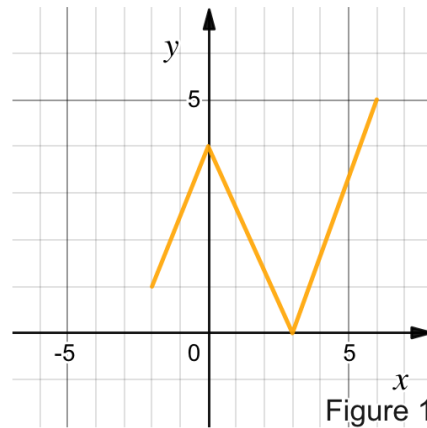
The graph of $y = f(x + a)$ is shown in Figure 2.



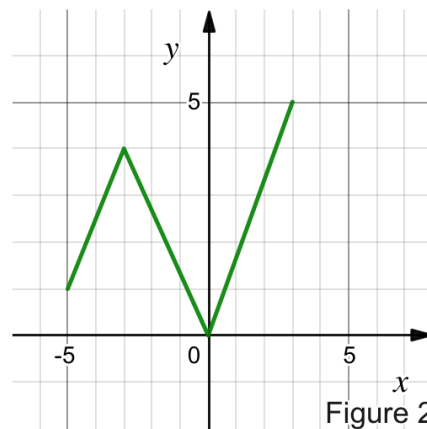
Determine the value of a .

Your Turn

The graph of $y = f(x)$ is shown in Figure 1.



The graph of $y = f(x + a)$ is shown in Figure 2.



Determine the value of a .

Worked Example

- a) The curve $y = \cos(4x + 90)$ is translated by $\begin{pmatrix} 30 \\ 0 \end{pmatrix}$
State the equation of the new curve after this transformation.
- b) The curve $y = \frac{4}{2x-5}$ is translated by $\begin{pmatrix} 0 \\ 3 \end{pmatrix}$
State the equation of the new curve after this transformation.

Your Turn

- a) The curve $y = \tan(3x - 30)$ is translated by $\begin{pmatrix} 0 \\ -3 \end{pmatrix}$
State the equation of the new curve after this transformation.
- b) The curve $y = \frac{1}{3x-3}$ is translated by $\begin{pmatrix} -4 \\ 0 \end{pmatrix}$
State the equation of the new curve after this transformation.

Worked Example	Your Turn
<p>The curve $y = 2x^2 + 3x$ is translated by $\begin{pmatrix} -4 \\ 5 \end{pmatrix}$ State the equation of the new curve after this transformation.</p>	<p>The curve $y = 2x^3 - x^2$ is translated by $\begin{pmatrix} 3 \\ -4 \end{pmatrix}$ State the equation of the new curve after this transformation.</p>

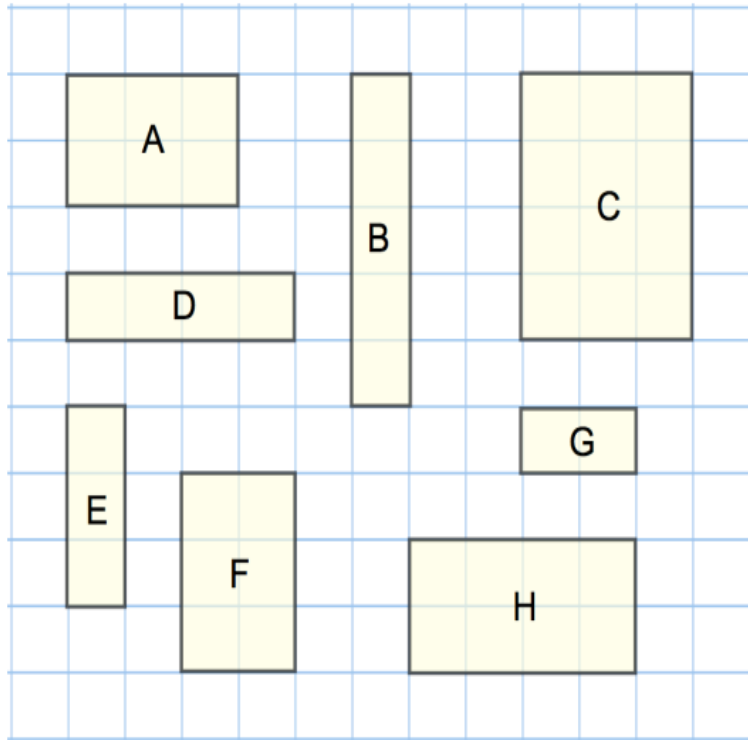
Fill in the Gaps

$f(x)$	Function notation	Description of translation	Vector of translation	New function
$2x + 1$	$f(x - 3)$	3 places right	$\begin{pmatrix} 3 \\ 0 \end{pmatrix}$	$f(x - 3) = 2(x - 3) + 1$ $= 2x - 6 + 1$ $= 2x - 5$
$3x + 1$	$f(x - 2)$			
x^2	$f(x - 1)$			
x^2		2 places left		
$x^2 + 5$			$\begin{pmatrix} -3 \\ 0 \end{pmatrix}$	
				$4(x + 5) + 2$
$x^2 + 2x - 1$		1 place left		
	$f(x - 4)$			

Extra Notes

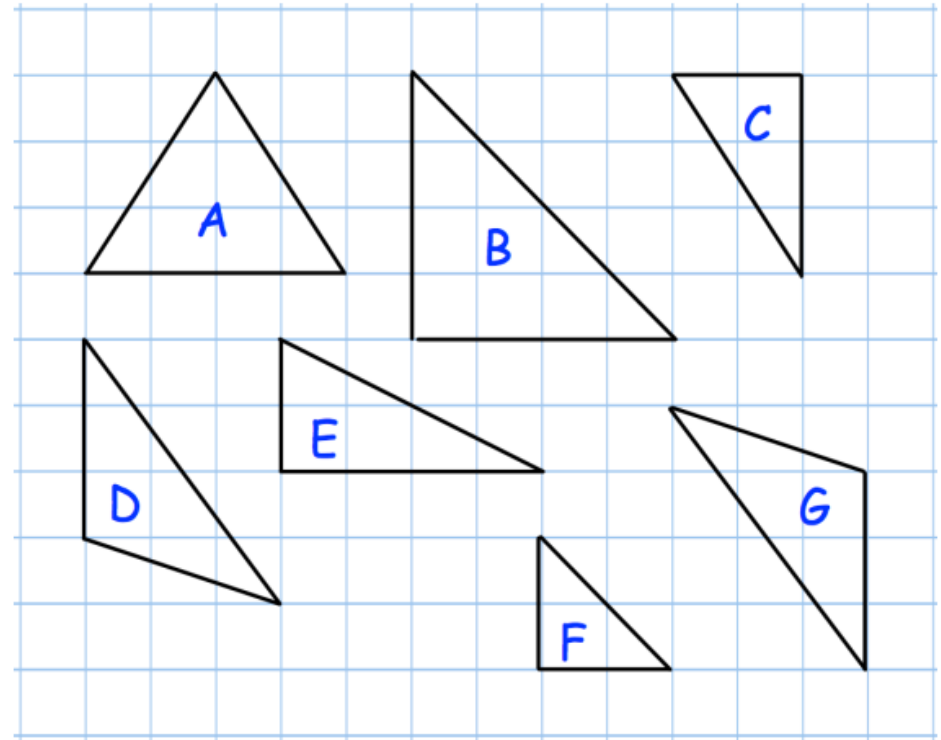
6 Congruency

Worked Example



- Which two shapes are congruent?
- Which two shapes are similar?

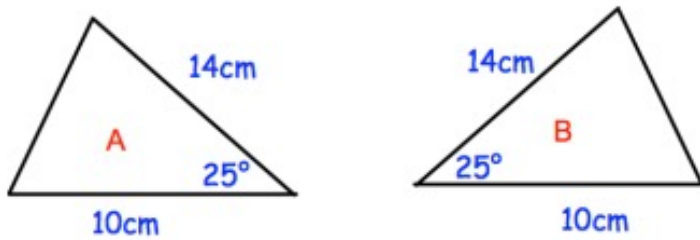
Your Turn



- Which two shapes are congruent?
- Which two shapes are similar?

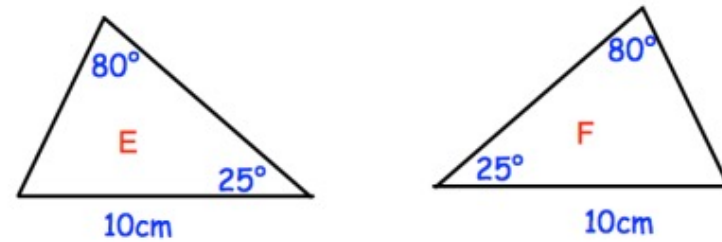
Worked Example

State the condition why these two triangles are congruent.



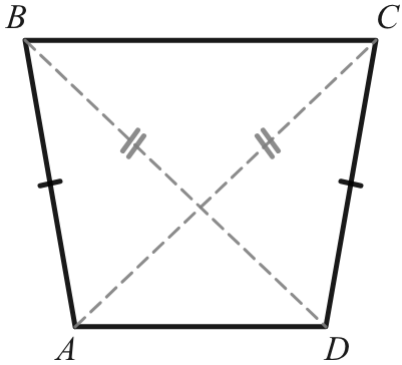
Your Turn

State the condition why these two triangles are congruent.



Worked Example

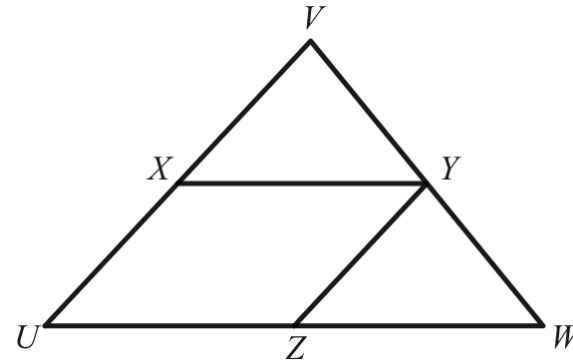
Below is a quadrilateral $ABCD$.



Prove that triangle ABD is congruent to triangle ACD .

Your Turn

The diagram shows triangle UVW .



$UXYZ$ is a parallelogram where

X is the midpoint of UV ,

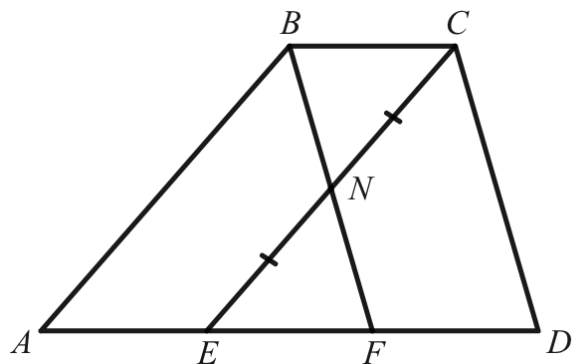
Y is the midpoint of VW ,

and Z is the midpoint of UW .

Prove that triangle XVY and triangle ZYW are congruent.

Worked Example

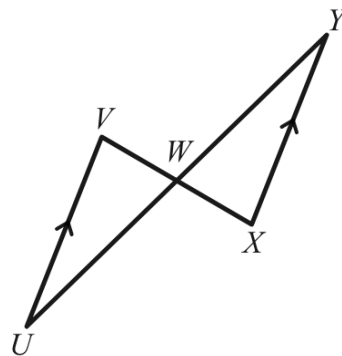
In the diagram below, $ABCE$ and $BCDF$ are parallelograms and N is the midpoint of CE .



Prove that triangle BCN and triangle EFN are congruent.

Your Turn

In the diagram below, UWY and VWX are straight lines.



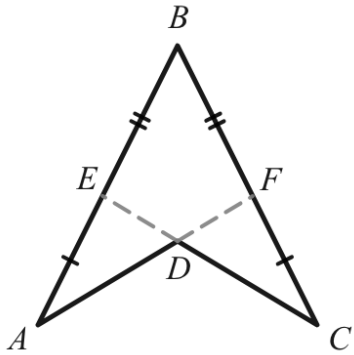
UV and XY are parallel.

W is the midpoint of UWY .

Prove that triangle UVW and triangle WXY are congruent.

Worked Example

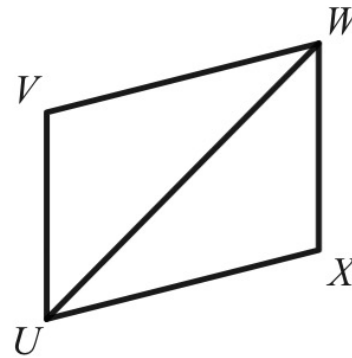
Below is a quadrilateral $ABCD$.



Prove that triangle ABE and triangle CDE are congruent.

Your Turn

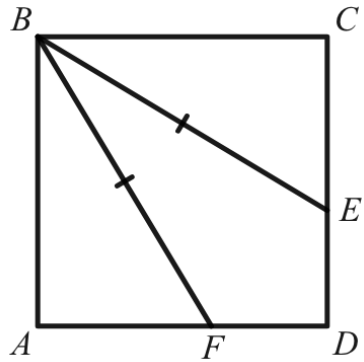
The diagram below shows a parallelogram $UVWX$.



Prove that triangle UVW and triangle UWX are congruent.

Worked Example

Below is a square $ABCD$.

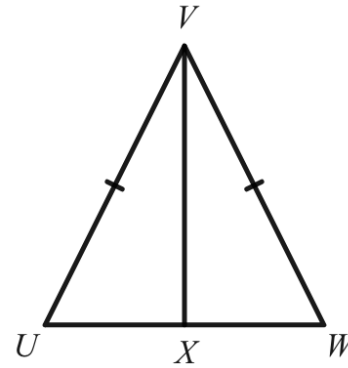


$$BE = BF$$

Prove that triangle ABF and triangle BCE are congruent.

Your Turn

Below is an isosceles triangle UVW .



VX is the perpendicular bisector of UW .

Prove that triangle UVX and triangle VWX are congruent.

Extra Notes

7 Circle Theorem Proofs

Worked Example

Prove angles in a semicircle are 90° .

Worked Example

Prove the angle at the centre of a circle is twice the angle at the circumference.

Worked Example

Prove angles in the same segment are equal.

Worked Example

Prove opposite angles of a cyclic quadrilateral add to 180° .

Worked Example

Prove the alternate segment theorem.

Extra Notes